

Definition 12 (Validity of one-state assertions). *Given an oracle $\mathcal{O} \subseteq \text{Module} \times \text{ClassId}$, the validity of an assertion A , is defined through the partial judgments:*

$$\begin{aligned} \models &\subseteq \text{Module} \times \text{state} \times \text{Oracle} \times \text{Assertion} \\ \not\models &\subseteq \text{Module} \times \text{state} \times \text{Oracle} \times \text{Assertion} \end{aligned}$$

using the notations $M, \sigma \models_{\mathcal{O}} A$ and $M, \sigma \not\models_{\mathcal{O}} A$:

- $M, \sigma \models_{\mathcal{O}} e$, if $\lfloor e \rfloor_{M, \sigma} = \mathbf{true}$,
 $M, \sigma \not\models_{\mathcal{O}} e$, if $\lfloor e \rfloor_{M, \sigma} = \mathbf{false}$,
undefined, otherwise.
- $M, \sigma \models_{\mathcal{O}} e_1 \geq e_2$, if $\lfloor e_1 \rfloor_{M, \sigma} \geq \lfloor e_2 \rfloor_{M, \sigma}$,
 $M, \sigma \not\models_{\mathcal{O}} e$, $\lfloor e_1 \rfloor_{M, \sigma} < \lfloor e_2 \rfloor_{M, \sigma}$,
undefined, if $\lfloor e_1 \rfloor_{M, \sigma}$ or $\lfloor e_1 \rfloor_{M, \sigma}$ is undefined, or not a number.
- $M, \sigma \models_{\mathcal{O}} Q(e_0, e_1, \dots, e_n)$, if
 $M, \sigma \models_{\mathcal{O}} A[e_0/\text{this}, e_1/p_1, \dots, e_n/p_n]$
 $M, \sigma \not\models_{\mathcal{O}} Q(e_0, e_1, \dots, e_n)$, if
 $M, \sigma \not\models_{\mathcal{O}} A[e_0/\text{this}, e_1/p_1, \dots, e_n/p_n]$
if $\mathcal{P}(M, \lfloor e_0 \rfloor_{\sigma} \downarrow_1, Q) = \mathbf{predicate } Q(p_1 \dots p_n) \{ A \}$,