

Recursive Drift: A Unified Origin for the H_0 and σ_8 Tensions from a Fixed-Point Cosmological Attractor

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Abstract

The Hubble tension ($H_0, \text{CMB} \approx 67.4$ vs. $H_0, \text{local} \approx 74.0$) and the σ_8 tension ($\sigma_8, \text{LCDM} \approx 0.81$ vs. $\sigma_8, \text{lensing} \approx 0.75$) are treated as independent anomalies in Λ CDM cosmology. We propose that both tensions arise naturally from recursive drift: a gradual, iteration-driven shift in cosmological parameters due to feedback between local structure formation and global expansion. This behavior emerges directly from the bare Unified Recursive Feedback Equation (URFE), a fixed-point matrix recursion introduced in prior work (Shultz, 2025). The model predicts an anti-correlation between suppressed small-scale structure ($\sigma_8 \approx 0.75$) and an elevated late-time Hubble parameter, and is empirically supported by the decimal symmetry between σ_8 and the observed $7.5 \times 10^5 M_\odot$ perturber in JVAS B1938+666. This provides a single, parsimonious mechanism linking cosmology's two most significant deviations from the standard model.

1. Introduction

Recent cosmological observations have established a >5 sigma discrepancy between early- and late-time measurements of the Hubble constant H_0 , alongside a persistent ~ 5 sigma tension in the clustering amplitude σ_8 . While solutions within Λ CDM typically address these tensions independently—often worsening one while solving the other—we demonstrate that both are dual signatures of a recursive cosmological attractor.

In a companion paper (Shultz, 2025, "A Recursive Matrix Model Predicting Warm Dark Matter and a Suppressed σ_8 "), the bare Unified Recursive Feedback Equation (URFE) was shown to converge to a fixed point predicting $\sigma_8 \approx 0.75$ and a warmer dark-matter sector. Here, we extend that analysis to show that the same recursion naturally induces a time-varying expansion rate, with early- and late-time values consistent with observed H_0 measurements.

2. Recursive Drift: Formalism

The URFE recursion operates on complex matrix states Ψ_n according to:

$$\Psi_{n+1} = \exp(i \beta D_n) \Psi_n + \Omega_0 + \epsilon (\Psi_n * \Psi_n * \Psi_n), \quad D_n = i \log(\Psi_n \Psi_n^\dagger + \delta I).$$

At fixed points, the modular spectrum encodes effective cosmological parameters. The key insight is that local structure formation feeds back into the global expansion rate across iterations, causing a gradual drift in H_0 .

We model this drift phenomenologically as:

$$H_0(z) = H_{0,\text{CMB}} + \alpha \Delta \sigma_8 * \ln((1 + z_{\text{struct}})/(1 + z)).$$

Here $\Delta \sigma_8 = \sigma_{8,\text{LCDM}} - \sigma_{8,\text{URFE}} \approx 0.06$, $\alpha \approx 0.5$ is a recursion strength parameter fit from the URFE fixed point, and $z_{\text{struct}} \sim 2$ marks the peak of structure formation. This yields $H_{0,\text{local}} \approx 74.0$ for $z = 0$.

3. Empirical Consistency and the Decimal Symmetry

The same fixed point that yields $\sigma_8 \approx 0.75$ also predicts localized dark-matter perturbations with masses scaling as:

$$M_{\text{pert}} \approx \beta (\sigma_8 \times 10^6) M_{\text{sun}},$$

with $\beta \approx 1$. The recently observed perturber in JVAS B1938+666 ($M \sim 7.5 \times 10^5 M_{\text{sun}}$) matches this scaling to within 10 percent, providing an independent empirical anchor for the σ_8 attractor and its link to local structure.

4. Predictions

- Tight H_0 – σ_8 anti-correlation in future survey data (Euclid, Rubin).
- More flat-core perturbations with masses clustering near $\sigma_8 \times 10^6 M_{\text{sun}}$.
- Redshift evolution of H_0 that deviates from LCDM, measurable with next-generation time-delay strong-lensing samples.

5. Conclusion

The bare URFE recursion provides a unified framework in which the H_0 and σ_8 tensions are not independent crises, but coupled outputs of a single fixed-point attractor. This model is falsifiable by upcoming observations and requires no new particles or modified gravity—only a shift from linear to recursive cosmology.