

Topic: **Clustering Analysis** (distance matrices)

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### Problem Statement:

Given two objects represented by the tuples (22, 1, 42, 10) and (20, 0, 36, 8):

(a) Compute the *Euclidean distance* between the two objects.

(b) Compute the *Manhattan distance* between the two objects.

(c) Compute the *Minkowski distance* between the two objects, using  $q = 3$ .

### Formulae:

1. Minkowski distance:

$$\left( \sum_{i=1}^n |x_i - y_i|^q \right)^{(1/q)}$$

2. Manhattan distance (Special case of Minkowski distance, with  $q=2$ )

$$\left( \sum_{i=1}^n |x_i - y_i| \right)$$

3. Euclidean distance (Special case of Minkowski distance, with  $q=2$ )

$$\left( \sum_{i=1}^n |x_i - y_i|^2 \right)^{(1/2)}$$

### Solution.

X	Y	Manhattan distance	Euclidean distance	Minkowski distance
$x_i$	$y_i$	$ x_i - y_i $	$ x_i - y_i ^2$	$ x_i - y_i ^3$
22	20	2	4	8
1	0	1	1	1
42	36	6	36	216
10	8	2	4	8
Sum =		11	45	233
Sum <sup>(1/q)</sup> =		11	6.708203932	6.153449494

Ans.

Manhattan distance

= 11 unit

Euclidean distance

= 6.70820393 unit

Minkowski distance with q=3

$$= \left( \sum_{i=1}^n |x_i - y_i|^3 \right)^{(1/3)}$$

= 6.153449494 unit