

▼ Importing data and creating table

Attributes:

X1 : Login Hours

X2 : Break time duration

Y (*Label*) : Productivity

```
1 import numpy as np
2 import pandas as pd
3
4 temp={"X1":[8.1,7.3,7.8,8.9,9.2,8.5,8.4,7.2,9.1,7.6,7.8,7.9],
5       "X2":[1.25,1.38,1.57,1.27,1.67,1.08,1.22,1.37,1.25,1.40,1.27,1.63],
6       "Y":[9.03,8.65,8.94,9.42,9.58,9.19,9.17,8.99,9.57,8.80,8.88,8.90]}
7 df=pd.DataFrame(temp)
8 df
```

	X1	X2	Y
0	8.1	1.25	9.03
1	7.3	1.38	8.65
2	7.8	1.57	8.94
3	8.9	1.27	9.42
4	9.2	1.67	9.58
5	8.5	1.08	9.19
6	8.4	1.22	9.17
7	7.2	1.37	8.99
8	9.1	1.25	9.57
9	7.6	1.40	8.80
10	7.8	1.27	8.88
11	7.9	1.63	8.90

▼ Calculating Means

```
1 X1bar = df["X1"].sum(axis=0)/len(df["X1"])
2 X1bar
```

8.149999999999999

```
1 X2bar = df["X2"].sum(axis=0)/len(df["X2"])
2 X2bar
```

1.3633333333333333

```
1 Ybar = df["Y"].sum(axis=0)/len(df["Y"])
2 Ybar
```

9.093333333333332

▼ Calculating $(X_i - \bar{X})$ and $(X_i - \bar{X})^2$

```
1 X1_err = df["X1"]-X1bar
2 df["X1i-X1bar"] = X1_err
3 df
```

	X1	X2	Y	X1i-X1bar
0	8.1	1.25	9.03	-0.05
1	7.3	1.38	8.65	-0.85
2	7.8	1.57	8.94	-0.35
3	8.9	1.27	9.42	0.75
4	9.2	1.67	9.58	1.05
5	8.5	1.08	9.19	0.35
6	8.4	1.22	9.17	0.25
7	7.2	1.37	8.99	-0.95
8	9.1	1.25	9.57	0.95
9	7.6	1.40	8.80	-0.55
10	7.8	1.27	8.88	-0.35
11	7.9	1.63	8.90	-0.25

```
1 X1_err2 = df["X1i-X1bar"]*df["X1i-X1bar"]
2 df["(X1i-X1bar)^2"] = X1_err2
3 df
```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2
0	8.1	1.25	9.03	-0.05	0.0025
1	7.3	1.38	8.65	-0.85	0.7225
2	7.8	1.57	8.94	-0.35	0.1225
3	8.9	1.27	9.42	0.75	0.5625

```

1 X2_err = df["X2"]-X2bar
2 df["X2i-X2bar"] = X2_err
3 df

```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2	X2i-X2bar
0	8.1	1.25	9.03	-0.05	0.0025	-0.113333
1	7.3	1.38	8.65	-0.85	0.7225	0.016667
2	7.8	1.57	8.94	-0.35	0.1225	0.206667
3	8.9	1.27	9.42	0.75	0.5625	-0.093333
4	9.2	1.67	9.58	1.05	1.1025	0.306667
5	8.5	1.08	9.19	0.35	0.1225	-0.283333
6	8.4	1.22	9.17	0.25	0.0625	-0.143333
7	7.2	1.37	8.99	-0.95	0.9025	0.006667
8	9.1	1.25	9.57	0.95	0.9025	-0.113333
9	7.6	1.40	8.80	-0.55	0.3025	0.036667
10	7.8	1.27	8.88	-0.35	0.1225	-0.093333
11	7.9	1.63	8.90	-0.25	0.0625	0.266667

```

1 X2_err2 = df["X2i-X2bar"]*df["X2i-X2bar"]
2 df["(X2i-X2bar)^2"] = X2_err2
3 df

```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2	X2i-X2bar	(X2i-X2bar)^2
0	8.1	1.25	9.03	-0.05	0.0025	-0.113333	0.012844
1	7.3	1.38	8.65	-0.85	0.7225	0.016667	0.000278
2	7.8	1.57	8.94	-0.35	0.1225	0.206667	0.042711
3	8.9	1.27	9.42	0.75	0.5625	-0.093333	0.008711
4	9.2	1.67	9.58	1.05	1.1025	0.306667	0.094044
5	8.5	1.08	9.19	0.35	0.1225	-0.283333	0.080278
6	8.4	1.22	9.17	0.25	0.0625	-0.143333	0.020544
7	7.2	1.37	8.99	-0.95	0.9025	0.006667	0.000044
8	9.1	1.25	9.57	0.95	0.9025	-0.113333	0.012844
9	7.6	1.40	8.80	-0.55	0.3025	0.036667	0.001344
10	7.8	1.27	8.88	-0.35	0.1225	-0.093333	0.008711

▼ Calculating (Xi - Xbar) * (Yi - Ybar)

```

1 Y_err = df["Y"]-Ybar
2 df["Yi-Ybar"] = Y_err
3 df

```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2	X2i-X2bar	(X2i-X2bar)^2	Yi-Ybar
0	8.1	1.25	9.03	-0.05	0.0025	-0.113333	0.012844	-0.063333
1	7.3	1.38	8.65	-0.85	0.7225	0.016667	0.000278	-0.443333
2	7.8	1.57	8.94	-0.35	0.1225	0.206667	0.042711	-0.153333
3	8.9	1.27	9.42	0.75	0.5625	-0.093333	0.008711	0.326667
4	9.2	1.67	9.58	1.05	1.1025	0.306667	0.094044	0.486667
5	8.5	1.08	9.19	0.35	0.1225	-0.283333	0.080278	0.096667
6	8.4	1.22	9.17	0.25	0.0625	-0.143333	0.020544	0.076667
7	7.2	1.37	8.99	-0.95	0.9025	0.006667	0.000044	-0.103333
8	9.1	1.25	9.57	0.95	0.9025	-0.113333	0.012844	0.476667
9	7.6	1.40	8.80	-0.55	0.3025	0.036667	0.001344	-0.293333
10	7.8	1.27	8.88	-0.35	0.1225	-0.093333	0.008711	-0.213333

```

1 X1Y_err = df["X1i-X1bar"]*df["Yi-Ybar"]
2 df["(X1i-X1bar)*(Yi-Ybar)"] = X1Y_err
3 df

```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2	X2i-X2bar	(X2i-X2bar)^2	Yi-Ybar	(X1i-X1bar)*(Yi-Ybar)
0	8.1	1.25	9.03	-0.05	0.0025	-0.113333	0.012844	-0.063333	0.003167
1	7.3	1.38	8.65	-0.85	0.7225	0.016667	0.000278	-0.443333	0.376833

```

1 X2Y_err = df["X2i-X2bar"]*df["Yi-Ybar"]
2 df["(X2i-X2bar)*(Yi-Ybar)"] = X2Y_err
3 df

```

	X1	X2	Y	X1i-X1bar	(X1i-X1bar)^2	X2i-X2bar	(X2i-X2bar)^2	Yi-Ybar	(X1i-X1bar)*(Yi-Ybar)	(X2i-X2bar)*(Yi-Ybar)
0	8.1	1.25	9.03	-0.05	0.0025	-0.113333	0.012844	-0.063333	0.003167	0.007167
1	7.3	1.38	8.65	-0.85	0.7225	0.016667	0.000278	-0.443333	0.376833	-0.007167
2	7.8	1.57	8.94	-0.35	0.1225	0.206667	0.042711	-0.153333	0.053667	-0.031667
3	8.9	1.27	9.42	0.75	0.5625	-0.093333	0.008711	0.326667	0.245000	-0.030667
4	9.2	1.67	9.58	1.05	1.1025	0.306667	0.094044	0.486667	0.511000	0.149667
5	8.5	1.08	9.19	0.35	0.1225	-0.283333	0.080278	0.096667	0.033833	-0.027667
6	8.4	1.22	9.17	0.25	0.0625	-0.143333	0.020544	0.076667	0.019167	-0.010667
7	7.2	1.37	8.99	-0.95	0.9025	0.006667	0.000044	-0.103333	0.098167	-0.000667
8	9.1	1.25	9.57	0.95	0.9025	-0.113333	0.012844	0.476667	0.452833	-0.054667
9	7.6	1.40	8.80	-0.55	0.3025	0.036667	0.001344	-0.293333	0.161333	-0.010667

Final Dataset

```

1 print(df)

```

	X1	X2	Y	...	Yi-Ybar	(X1i-X1bar)*(Yi-Ybar)	(X2i-X2bar)*(Yi-Ybar)
0	8.1	1.25	9.03	...	-0.063333	0.003167	0.007167
1	7.3	1.38	8.65	...	-0.443333	0.376833	-0.007167
2	7.8	1.57	8.94	...	-0.153333	0.053667	-0.031667
3	8.9	1.27	9.42	...	0.326667	0.245000	-0.030667
4	9.2	1.67	9.58	...	0.486667	0.511000	0.149667
5	8.5	1.08	9.19	...	0.096667	0.033833	-0.027667
6	8.4	1.22	9.17	...	0.076667	0.019167	-0.010667
7	7.2	1.37	8.99	...	-0.103333	0.098167	-0.000667
8	9.1	1.25	9.57	...	0.476667	0.452833	-0.054667
9	7.6	1.40	8.80	...	-0.293333	0.161333	-0.010667
10	7.8	1.27	8.88	...	-0.213333	0.074667	0.019667
11	7.9	1.63	8.90	...	-0.193333	0.048333	-0.051667

[12 rows x 10 columns]

▼ Calculating summations, w1, w2 and w0

```
1 sum_mul_X1 = df["(X1i-X1bar)*(Yi-Ybar)".sum(axis=0)
2 sum_mul_X1
```

```
2.07799999999999985
```

```
1 sum_sq_X1 = df["(X1i-X1bar)^2"].sum(axis=0)
2 sum_sq_X1
```

```
4.9899999999999998
```

```
1 sum_mul_X2 = df["(X2i-X2bar)*(Yi-Ybar)".sum(axis=0)
2 sum_mul_X2
```

```
-0.04863333333333311
```

```
1 sum_sq_X2 = df["(X2i-X2bar)^2"].sum(axis=0)
2 sum_sq_X2
```

```
0.35346666666666654
```

Formulae

$$y = w_0 + w_1 * x_1 + w_2 * x_2$$

$$w_1 = \text{sum_mul_X1} / \text{sum_sq_X1}$$

$$w_2 = \text{sum_mul_X2} / \text{sum_sq_X2}$$

```
1 w1 = sum_mul_X1 / sum_sq_X1
2 w2 = sum_mul_X2 / sum_sq_X2
3
4 print("w1 = ", w1)
5 print("w2 = ", w2)
```

```
w1 = 0.41643286573146276
w2 = -0.13758958883440153
```

```
1 w0 = Ybar - w1*X1bar - w2*X2bar
2 w0
```

```
5.886985950399478
```

Results

$$w_1 = 0.41643286573146276$$

$$w_2 = -0.13758958883440153$$

▼ Predicting values

Calculating y_{pred} for $x_1 = 9.5$ and $x_2 = 1.67$

```
1 x1 = 9.5
2 x2 = 1.67
3 Y_pred = w0 + w1*x1 + w2*x2
4 Y_pred
```

9.613323561494925

Calculating y_{pred} for $x_1 = 7$ and $x_2 = 1.15$

```
1 x1 = 7
2 x2 = 1.15
3 Y_pred = w0 + w1*x1 + w2*x2
4 Y_pred
```

↗ 8.643787983360157