MCMT Homework 11

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Exercise 11.1

Suppose there are n cards in total and m cards in the left hand. Consider the next card to be dropped from the bottom of left-right deck or the right-hand deck.

Following the first model, the number of cases that the next card is from Following the first model, the number of cases that the next card is from the left hand is $\binom{n}{m} - \binom{n-1}{m} = \binom{n-1}{m-1}$. The number of cases that the next card is from the right hand: $\binom{n-1}{m}$. The ratio of probability of the next card being from the left hand versus the right hand is $\binom{n-1}{m-1}/\binom{n-1}{m} = m/(n-m)$. Following the second model, the ratio of probability of the next card being from the left hand versus the right hand is $\frac{m}{n}/\frac{n-m}{n} = m/(n-m)$. So they have the same probability distribution on the next card to be

dropped. This is applied to each step. So these two characterizations are equivalent.