## MCMT Homework 8

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## Exercise 8.1

For any non-negative constant c, define  $\{\tau \leq t\} = 1_{|\{X_0,\cdots,X_t\}|=c}$ . Then  $\tau = c$  is a stopping time.

Suppose there are two stopping times  $\tau_1$  and  $\tau_2$ . We can make  $\{X_0, \cdots, X_s\}$  satisfy  $\{s \leq \tau_1\}$  and  $\{X_s, \cdots, X_t\}$  satisfy  $\{t - s \leq \tau_2\}$ . That is,  $\{\tau_1 + \tau_2 \leq t\} = \{\tau_1 \leq s\} \land \{\tau_2 \leq t - s, X_0 = y\}$ , where y is the state when  $\{\tau_1 \leq s\}$  is true. So  $\tau_1 + \tau_2$  is a stopping time.