# Survey on Hierarchical and Modular Reinforcement Learning

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September 26, 2014

## Markov Decision Process

#### MDP:

• State: *S*.

• Action: A.

• Transition:  $P: S \times A \times S \rightarrow \mathcal{R}$ .

• Reward:  $R: S \times A \times S \rightarrow \mathcal{R}$ .

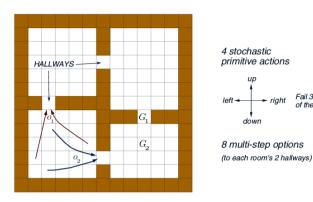
• Aggregate states: feature extraction.

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- Decompose transition: factored MDP.
- Decompose value (abstract MDP): HAM, hierarchical RL, modular RL.

# MDP with Option



• Option: (start state, policy, termination condition).

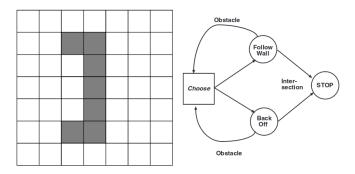
Fail 33% of the time

# MDP with Option

#### MDP:

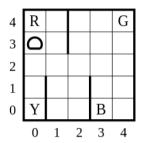
- State: S.
- Action: *A*, *O*.
- Transition:  $P: S \times \{A, O\} \times S \rightarrow \mathcal{R}$ .
- Reward:  $R: S \times \{A, O\} \times S \rightarrow \mathcal{R}$ .

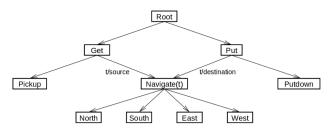
# Hierarchies of Abstract Machines (HAM)



• State machine of MDPs.

# Hierarchical RL





# Hierarchical RL

#### MDP:

• State: S.

• Action: A.

• Transition:  $\mathcal{T}$ .

• Reward: R.

## Modular RL

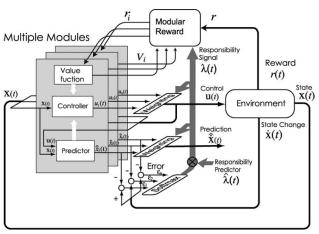


Fig. 1. MMRL.

## Modular RL

#### MDP:

• State:  $S_1 \times S_2 \cdots \times S_M$ .

• Action: A.

• Transition:  $P_1 \times P_2 \cdots \times P_M$ .

• Reward:  $R_1 \times R_2 \cdots \times R_M$ .

# Topics for Future Work

- Credit assignment.
- Learning task hierarchies.
- Dynamic abstraction.
- Integrating Deep Learning.