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Human vs. Computer

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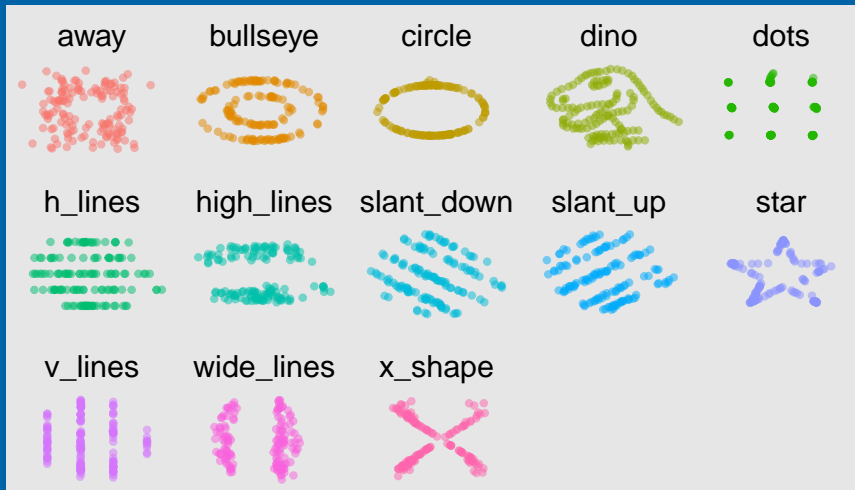
5/28/2018

Teach the computer to read residual plots

A major component used to diagnose model fits is a plot of the residuals. Residual plots are used to assess:

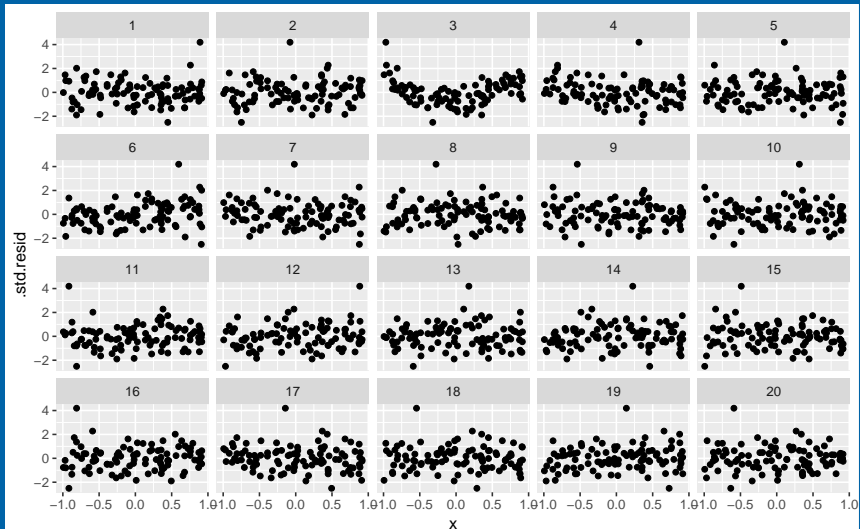
- Gauss-Markov assumption
- Heteroskedasticity
- Clumps of outliers

Why plots?



$$E(x) = 54.3, E(y) = 47.8, sd(x) = 16.8, sd(y) = 26.9, r = -0.06$$

Visual inference



Visual inference

- Plot of data is a test statistic
- Type of plot determines null hypothesis, e.g. residuals vs fitted scatterplot would imply H_o : no relationship, vs H_a : some relationship
- Human visual system evaluates lineup of data plot in field of null plots
- If data plot is “identified” as different from null, H_o is rejected
- Combining results from multiple observers enables p -value calculation

Deep learning

- Computer vision has advanced substantially
- Computer vision underlying self-driving cars, robotics
- Computer vision is being build on deep learning models
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- If we can train a computer to read residual plots we can have it process a lot more data, than a human can manage.

Aside: Volvo admits its self-driving cars are confused by kangaroos

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Volvo's self-driving car is unable to detect kangaroos because hopping confounds its systems, the Swedish carmaker says.

Aside: Computers can't tell difference between blueberry muffins and chihuahuas



Figure 1: Computers can't tell difference between blueberry muffins and chihuahuas

Experiment

- 1 Simulate data from the different models
- 2 Fit a linear model to the data, extract standardized residuals and fitted values
- 3 Save residual plots as fixed-sized images
- 4 Train a deep learning classifier to recognise the departures from assumptions
- 5 Test the model's performance on new data and compute the accuracy

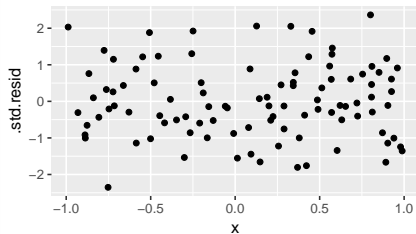
Data simulation

These factors are being controlled in the data simulation

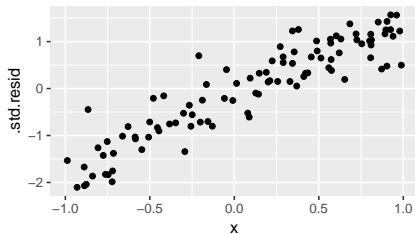
- Type of relationship: none, linear, nonlinear or heteroskedasticity
- Explanatory variables: $X \sim N(0, 3)$ and intercept $\beta_0 = 0$
- Sample size: randomly generated between 20-1500
- Image size: fixed 150x150

Type of relationship

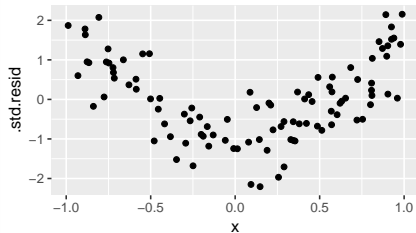
None



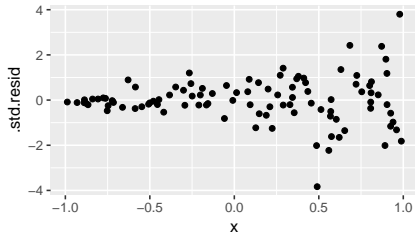
Linear



Non-linear



Heteroskedastic



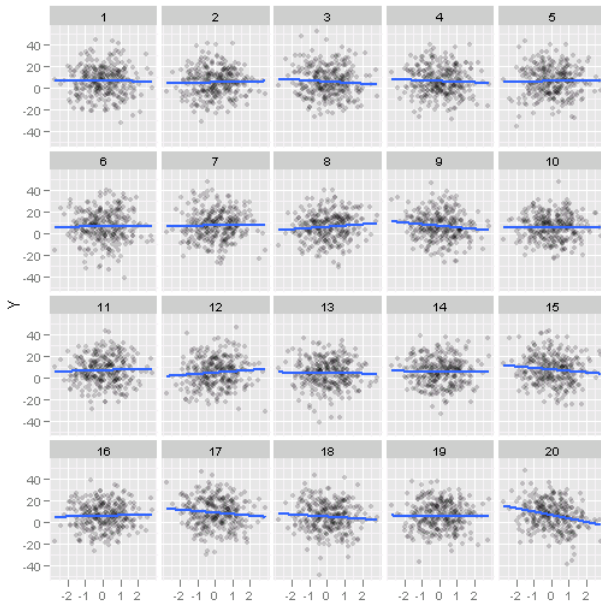
Simchoni's analysis

- Simulate data from linear relationship with $\rho = -0.9$ to $\rho = 0.9$
- Separate into two groups: significant/insignificant by t-test
- Train deep learning model with these two groups
- Test the model on lineup
- Successful in detecting linear relationship but fail in non-linear
- Simchoni's blog

Comparison with human subject experiments

- Majumder et al (2013) conducted a large study to compare the performance of the lineup protocol, assessed by human evaluators, in comparison to the classical test
- Experiment 2 examined $H_o : \beta_k = 0$ vs $H_a : \beta_k \neq 0$ assessing the importance of including variable k in the linear model, conducted with a t -test, and also lineup protocol
- 70 lineups of size 20 plots
- 351 evaluations by human subjects
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- Trained deep learning model will be used to classify plots from this study. Accuracy will be compared with results by human subjects.

Example lineup from experiment 2



Timeline

Date	Component
Apr 27	Deep learning model trained
May 4	Classification of new residual plots with model and results summarised
May 18	Comparison with Turk studies
May 24	Refinements made, final summaries written
May 31	Thesis finalised

- The thesis, code and data is available on the github repository <https://github.com/shuofan18/ETF5550>
- Software used to conduct this research is R, Tensorflow, keras, tidyverse