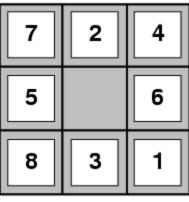
## **Advanced Search**

#### Admissible heuristics

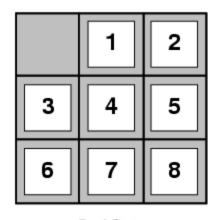
#### E.g., for the 8-puzzle:

- $h_1(n)$  = number of misplaced tiles
- $h_2(n)$  = total Manhattan distance

(i.e., no. of squares from desired location of each tile)



Start State



Goal State

• 
$$h_1(S) = ?$$

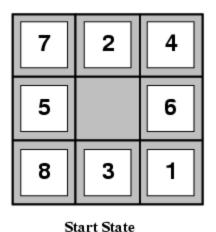
• 
$$h_2(S) = ?$$

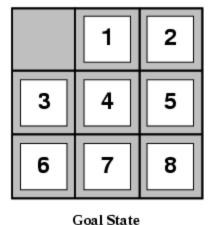
#### Admissible heuristics

E.g., for the 8-puzzle:

- $h_1(n)$  = number of misplaced tiles
- $h_2(n)$  = total Manhattan distance

(i.e., no. of squares from desired location of each tile)





- $h_1(S) = ?8$
- $h_2(S) = ? 3+1+2+2+3+3+2 = 18$

#### Relaxed problems

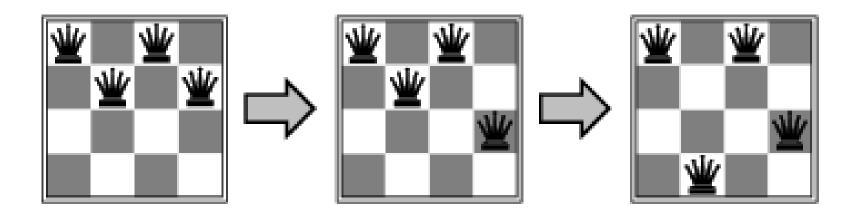
- A problem with fewer restrictions on the actions is called a relaxed problem
- The cost of an optimal solution to a relaxed problem is an admissible heuristic for the original problem
- If the rules of the 8-puzzle are relaxed so that a tile can move anywhere, then  $h_1(n)$  gives the shortest solution
- If the rules are relaxed so that a tile can move to any adjacent square, then  $h_2(n)$  gives the shortest solution

#### Local search algorithms

- In many optimization problems, the path to the goal is irrelevant; the goal state itself is the solution
- State space = set of "complete" configurations
- Find configuration satisfying constraints, e.g., n-queens
- In such cases, we can use local search algorithms that keep a single "current" state, try to improve it

## Example: *n*-queens

 Put n queens on an n × n board with no two queens on the same row, column, or diagonal



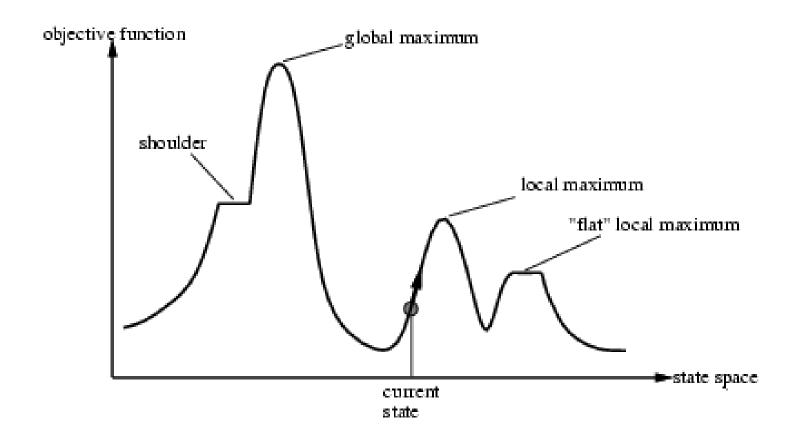
#### Hill-climbing search

"Like climbing Everest in thick fog with amnesia"

```
function Hill-Climbing (problem) returns a state that is a local maximum inputs: problem, a problem local variables: current, a node neighbor, \text{ a node} current \leftarrow \text{Make-Node}(\text{Initial-State}[problem]) loop do neighbor \leftarrow \text{a highest-valued successor of } current if \text{Value}[\text{neighbor}] \leq \text{Value}[\text{current}] then \text{return State}[current] current \leftarrow neighbor
```

#### Hill-climbing search

 Problem: depending on initial state, can get stuck in local maxima

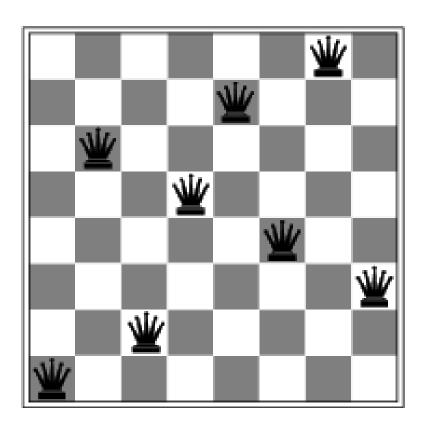


## Hill-climbing search: 8-queens problem

18	12	14	13	13	12	14	14
14	16	13	15	12	14	12	16
14	12	18	13	15	12	14	14
15	14	14	♛	13	16	13	16
₩	14	17	15	₩	14	16	16
17	₩	16	18	15	₩	15	₩
18	14	₩	15	15	14	₩	16
14	14	13	17	12	14	12	18

- h = number of pairs of queens that are attacking each other, either directly or indirectly
- h = 17 for the above state

## Hill-climbing search: 8-queens problem



• A local minimum with h = 1

#### Simulated annealing search

 Idea: escape local maxima by allowing some "bad" moves but gradually decrease their frequency

```
function Simulated-Annealing (problem, schedule) returns a solution state inputs: problem, a problem schedule, a mapping from time to "temperature" local variables: current, a node next, a node T, a "temperature" controlling prob. of downward steps  \begin{array}{c} current \leftarrow \text{Make-Node}(\text{Initial-State}[problem]) \\ \text{for } t \leftarrow 1 \text{ to } \infty \text{ do} \\ T \leftarrow schedule[t] \\ \text{if } T = 0 \text{ then return } current \\ next \leftarrow \text{a randomly selected successor of } current \\ \Delta E \leftarrow \text{Value}[next] - \text{Value}[current] \\ \text{if } \Delta E > 0 \text{ then } current \leftarrow next \\ \text{else } current \leftarrow next \text{ only with probability } e^{\Delta E/T} \\ \end{array}
```

#### Properties of simulated annealing search

 One can prove: If T decreases slowly enough, then simulated annealing search will find a global optimum with probability approaching 1

Widely used in VLSI layout, airline scheduling, etc

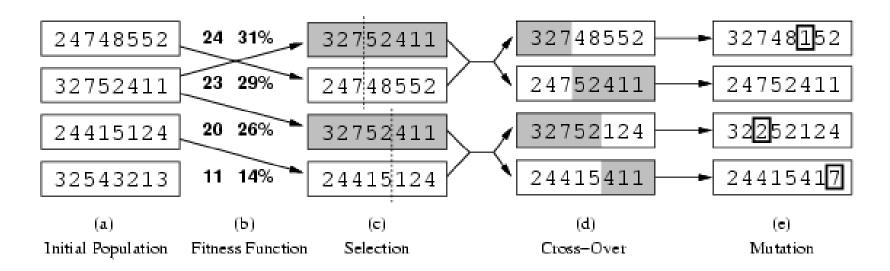
#### Local beam search

- Keep track of *k* states rather than just one
- Start with *k* randomly generated states
- At each iteration, all the successors of all k states are generated
- If any one is a goal state, stop; else select the *k* best successors from the complete list and repeat.

#### Genetic algorithms

- A successor state is generated by combining two parent states
- Start with k randomly generated states (population)
- A state is represented as a string over a finite alphabet (often a string of 0s and 1s)
- Evaluation function (fitness function). Higher values for better states
- Produce the next generation of states by selection, crossover, and mutation

#### Genetic algorithms



- Fitness function: number of non-attacking pairs of queens (min = 0, max =  $8 \times 7/2 = 28$ )
- 24/(24+23+20+11) = 31%
- 23/(24+23+20+11) = 29% etc

# Genetic algorithms

