

Object Capability Patterns: Policies and Specifications

SHU-PENG LOH

Imperial College London
shu.loh16@imperial.ac.uk

SOPHIA DROSSOPOULOU

Imperial College London
s.drossopoulou@imperial.ac.uk

Abstract

We propose a set of higher-order predicate logic to formally specify object-to-object interactions which can then be used to describe reference dynamics in an object-oriented computational model. Using these predicates, we attempt to formally specify the policies of well-established Object-Capability (OCap) patterns within the OCap literature which we have implemented in the capability-safe language Pony. We also offer some preliminary insights on how such specifications can be used in the context of a non-OCap model by describing the security properties of a pattern built on the Ethereum smart contract programming language Solidity, which we argue implements a form of stack-based access control.

1 Introduction

Recent widespread adoption of distributed ledger technology (blockchain) has created multiple decentralized, distributed computational platforms where millions of dollars are transacted over codified constructs called smart contracts¹. The power of distributed modern computing hence lies in facilitating cooperation between multiple agents, but it comes with risk as an agent is vulnerable to *unexpected* outcomes² from participating in these smart contracts. This might generally arise from two issues:

- oversight or misconception of the outcomes of executing a piece of *known* code
- failure to defend against malicious execution of *unknown* code components

These two issues are often closely intertwined in any system of execution that has both trusted and untrusted code components (the second issue is often a result of the first).

In recent years the Object-Capability (OCap) model has received increasing attention as a

compelling approach to building robust, distributed systems that promote what Miller[?] calls *cooperation without vulnerability*. The OCap model attempts to address these two issues by alleviating security as a separate concern from the mind of the programmer, by leveraging the object-oriented programming paradigm and imposing certain prohibitions.

2 OCap Model

The OCap model uses the reference graph of the objects as the access graph, and strictly requires objects to interact with each other only by sending messages on object references[?].

2.1 From Capability to Object-Capability

2.2 OCap Languages

- Joe-E (inspired by Java)
- Emily (inspired by OCaml)
- Caja (inspired by JavaScript)
- E
- Pony

2.2.1 Language Restrictions

2.3 OCap Patterns

An OCap pattern is a concrete representation of the OCap model and comprises a set of objects

¹For example, as of 10 Aug 2017, Ethereum is a US\$28 billion blockchain platform with an in-built Turing-complete programming language that can be used to create and deploy such contracts.

²Representing in general any outcome arising from a piece of code execution that has deviated from an agent's original intention or objective independent from code.

connected to each other by capabilities. Objects interact with each other by sending messages on capabilities. An OCap pattern may be visualised as a directed graph—nodes represent objects, and each edge from an object o to another o' represents o holding a capability that allows it to directly access o' .

3 Formal specifications

3.1 Definitions

We borrow liberally the definitions of runtime state, module and arising configurations from the appendix of [?].

Runtime state: σ consists of a stack frame φ , and a heap χ . A stack frame is a mapping from receiver (*this*) to its address, and from the local variables (*VarId*) and parameters (*ParId*) to their values. Values are integers, the booleans true or false, addresses, or null. The heap maps addresses to objects. Objects are tuples consisting of the class of the object, and a mapping from field identifiers onto values.

$\sigma \in \text{state} = \text{frame} \times \text{heap}$
 $\varphi \in \text{frame} = \text{StackId} \rightarrow \text{val}$
 $\chi \in \text{heap} = \text{addr} \rightarrow \text{object}$
 $v \in \text{val} = \{\text{null}, \text{true}, \text{false}\} \cup \text{addr} \cup \mathbb{N}$
 $\text{StackId} = \{\text{this}\} \cup \text{VarId} \cup \text{ParId}$
 $\text{object} = \text{ClassId} \times (\text{FieldId} \rightarrow \text{val})$

Module:

$M \in \text{Module} = \text{ClassId} \cup \text{SpecId}$
 \rightarrow
 $(\text{ClassDescr} \cup \text{Specification})$

Reach and Execution:

Arising Configurations

Domination:

3.1.1 MayAccess Definitions

We define in total four flavours of *MayAccess* predicates that describe the relation between two entities in a system (of arity 2 that represent the identifiers of these entities). These four flavours represent a combination of space (distance) and time (state):

- distance: directly (*Dir*) or indirectly (*Ind*)
- state: now (*Now*) or eventually (*Eve*)

and are broad enough to describe both non-OCap and OCap models:

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{Dir, Now}(x, e) &\iff \\ \exists f. [x.f]_\sigma &= [e]_\sigma \vee \\ (\sigma(\text{this}) = [x]_\sigma \wedge \exists y. \sigma(y) &= [e]_\sigma) \end{aligned}$$

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{Dir, Eve}(x, e) &\iff \\ \exists \sigma' \in \text{Arising}(M, \sigma). & \\ M, \sigma' \models \text{MayAccess}^{Dir, Now}(x, e) & \end{aligned}$$

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{Ind, Now}(x, e) &\iff \\ \exists \tilde{f}. [x.\tilde{f}]_\sigma &= [e]_\sigma \vee \\ (\sigma(\text{this}) = [x]_\sigma \wedge \exists y. \sigma(y.\tilde{f}) &= [e]_\sigma) \end{aligned}$$

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{Ind, Eve}(x, e) &\iff \\ \exists \sigma' \in \text{Arising}(M, \sigma). & \\ M, \sigma' \models \text{MayAccess}^{Ind, Now}(x, e) & \end{aligned}$$

A note on f and \tilde{f} : While f can be considered as a field, it can also represent a method that returns a val. Similarly \tilde{f} can be considered a series of fields, or methods that return a val, or a combination of both.

We summarise the relationships between the four flavours of *MayAccess* in ??:

Table 1: $\text{MayAccess}^{*,*}(x, e)$ Relations

	Now		Eventually
Direct	$\text{MayAccess}^{Dir, Now}$	\implies \nLeftarrow	$\text{MayAccess}^{Dir, Eve}$
	$\Downarrow \Uparrow$		$\Downarrow \Uparrow$
Indirect	$\text{MayAccess}^{Ind, Now}$	\implies \nLeftarrow	$\text{MayAccess}^{Ind, Eve}$

Let us assume that both x and e are well-defined. Note that without imposing any further assumptions (such as those from the OCap model), we have defined *both* $\text{MayAccess}^{Dir, Now}(x, e)$ and

$\text{MayAccess}^{\text{Ind,Now}}(x,e)$ to mean forms of very weak access—that a directed path exists from x to e , but we do *not* imply that such a path is traverseable by x (it might or might not be traverseable). Indeed, these definitions by themselves represent mere *possibilities* of interaction (or possible authorities), they do *not* represent that interaction (or authority) would succeed. The difference between $\text{MayAccess}^{\text{Dir,Now}}(x,e)$ and $\text{MayAccess}^{\text{Ind,Now}}(x,e)$ is only the computational distance between x and e on the reference graph, where the latter involves possibly intermediate entities (or objects in an object-oriented model).

What do the definitions mean then for non-OCap and OCap models in an object-oriented world? Again, let us assume both o and o' are well-defined, valid object references. In non-OCap models, the possible presence of a global ambient authority means the predicates above say *nothing* about whether any interaction between an object o and o' would succeed. This is true even if o possesses directly the reference of o' , where $\text{MayAccess}^{\text{Dir,Now}}(o,o')$ holds. For all we know, we could easily have in a non-OCap language a feature to completely restrict access to o' using a global ambient authority, such that any object in the programming world which possesses references of o' cannot use them, and all paths leading to o' represent merely possibilities of interaction, but from which no authority can possibly arise.

Could we say more about OCap systems? In OCap systems, there can be no global ambient authority so that an object reference by itself represents both the designation and the authority to use the object. This therefore leads us to be able to make a crucial distinction between $\text{MayAccess}^{\text{Ind,Now}}(o,o')$ and $\text{MayAccess}^{\text{Dir,Now}}(o,o')$ in the OCap model:

- $\text{MayAccess}^{\text{Ind,Now}}(o,o')$ means—*only*
 1. a directed path from o to o' exists (possible authority)
- $\text{MayAccess}^{\text{Dir,Now}}(o,o')$ means—*both*
 1. a directed path from o to o' exists (possible authority) *and*
 2. o 's authority to use o' *will* succeed

We elaborate the distinction with the following OCap example where there is a particular state σ of the system where, $o_1.\text{next}$ points to o_2 , and $o_2.\text{next}$ points to o_3 . $o_2.\text{next}$ is a private method that can only be called internally by o_2 . In this example, $M, \sigma \models \text{MayAccess}^{\text{Ind,Now}}(o_1, o_3)$ holds, regardless of whether $o_2.\text{next}$ is traverseable by o_1 . We say here that a path from o_1 to o_3 exists, but is not traverseable by o_1 . On the other hand, $\text{MayAccess}^{\text{Dir,Now}}(o_1, o_3)$ does not hold true, because o_3 is not reachable from o_1 in a single step— o_2 sits between them on the reference graph as an intermediate object, and can possibly prevent or allow traversal from o_1 to o_3 (in this example, o_2 prevents such a traversal).

What does it mean then for $\text{MayAccess}^{\text{Dir,Now}}(*,*)$ to hold in an OCap model? From the same example, $\text{MayAccess}^{\text{Dir,Now}}(o_1, o_2)$ holds and implies a stronger form of access—it means that a path exists from o_1 to o_2 , and that such a path *is* traverseable. This is because, by the definition of the predicate and configuration of the example, the object reference of o_2 exists within o_1 's state. Therefore, o_2 is guaranteed therefore to be accessible, and its authority exercisable, by o_1 , without the interference of any ambient authority. Notice how this o_1 - o_2 relationship differs from the o_1 - o_3 relationship, where o_1 cannot guarantee that it can exercise the authority of $o_2.\text{next}$ which points to o_3 , since $o_2.\text{next}$ does not exist within o_1 's state—it is possible that $o_2.\text{next}$ is protected by x_2 through encapsulation and data-hiding.

Within an OCap model, we can now be convinced that the stronger

$\text{MayAccess}^{\text{Dir,Now}}(o_1, o_2) \simeq$
 $o_1 \text{ has the capability of } o_2$

while the weaker $\text{MayAccess}^{\text{Ind,Now}}(o_1, o_3)$ does not say anything about whether o_1 has the capability of o_3 , but that only a directed path exists. It does however, represent a necessary condition for capability.

$\text{MayAccess}^{\text{Ind,Now}}(o_1, o_3) \simeq$
 there is a directed path from o_1 to o_2

$o_1 \text{ has the capability of } o_3 \implies$
 $\text{MayAccess}^{\text{Ind,Now}}(o_1, o_3)$

3.1.2 MayAffect Definitions

With our access predicates in place, we introduce a set of predicates that describe changes to the state of a system. Again, we highlight that these predicates are broad enough to describe both non-OCap and OCap models.

$$M, \sigma \models \text{MayAffect}^{\text{Now}}(x, e) \iff \exists \bar{m}, \bar{a}, \sigma'. x.\bar{m}(\bar{a}) \rightsquigarrow \sigma' \wedge [e]_{\sigma} \neq [e]_{\sigma'}$$

$$M, \sigma \models \text{MayAffect}^{\text{Eve}}(x, e) \iff \begin{aligned} &\exists \sigma \in \text{Arising}(M, \sigma). \\ &\exists \bar{m}, \bar{a}, \sigma'. x.\bar{m}(\bar{a}) \rightsquigarrow \sigma' \wedge [e]_{\sigma} \neq [e]_{\sigma'} \end{aligned}$$

If e is an object:

$$\forall e \in \text{Object}. [e]_{\sigma} \neq [e]_{\sigma'} \iff \exists f. [e.f]_{\sigma} \neq [e.f]_{\sigma'}$$

Table 2: $\text{MayAffect}(o, o')$ Relations in OCap

$\text{MayAffect}^{\text{Now}}$	\implies	$\text{MayAffect}^{\text{Eve}}$
	\nLeftarrow	

3.2 OCap Security Implications

3.2.1 What is protection?

In an object-oriented world³, security concerns between objects are often a question of whether what one object can do to another object in *any* eventual state of a system. Because an object encapsulates both internal state and behaviour, strictly speaking, security of an object should govern over both the integrity of the object's fields (internal state) and whether the objects' methods can be called (behaviour). Our predicates are broad enough to enable a discussion of both protection of state ($\text{MayAffect}^{\text{Eve}}$) and behaviour ($\text{MayAccess}^{\text{Dir, Eve}}$)⁴. We emphasize however that protecting either state or behaviour of an object, does *not* necessarily imply the other. In fact, a common feature in OCap patterns is being able to protect a sensitive object's behaviours (they cannot be called directly by untrusted objects), but at the

³ To simplify our discussion, we work with the variables $\{o, o'\} \in \text{Object}$ for this entire section.

⁴ Our $\text{MayAccess}^{\text{Dir, Eve}}$ is not weak enough to reason specifically which behaviours can be called. This is however not a big issue in *pure* OCap systems, where often giving away the capability of an object typically means allowing *all* public behaviours of the object to be called without distinction.

some allowing the same untrusted objects to modify the object's state in some controlled way.

There are however, some flexibility in working with objects, that allows us to simplify our discussion and work with only a broad definition of state protection in terms of our $\text{MayAffect}^{\text{Eve}}$ predicate, *without* thinking too much about specific fields of the object we want to protect or the protection of behaviour. Moving away from our broad definition of whether an object may be affected (we defined it as being able to change at least one field of the object), to more precise specifications of which particular field(s) of the object may be affected, should be trivial. We can in theory also stay and reason within our framework by separating the particular concerned field(s) of the object into separately encapsulated objects. We merely have to be careful as to *which* object's state we want to protect. Furthermore, in theory one can easily introduce a field within an object that behaves like a 'signal' which would be modified whenever a specified behaviour is called. Preventing a particular behaviour to be called by an untrusted object then becomes equivalent to denying the untrusted object the ability to modify the particular state of the signal field of the object.

With these simplifications, protection for us then becomes solely a matter of whether we can allow or deny an object to modify the state of another. In the following ?? below we build the necessary conditions for $\text{MayAffect}^{\text{Eve}}$, where $\text{MayAffect}^{\text{Eve}}$ is placed in the antecedent, and we examine which of the family of MayAccess predicates is placed in the consequent. To help us achieve this, we also formalize our assumptions and the rules of OCap, using our predicates, to help guide us in constructing our necessary conditions in ??.

3.3 Formal specifications of OCap Rules

Rule 1: Objects can only interact with each other through sending messages on capabilities. We begin our reasoning of protection in our OCap model, by first re-asserting the necessary but not sufficient path condition of

capability, and calling it PEC. By definition of our predicates, an object having a capability of o' implies object o having a path to o' , but not vice-versa:

$$\begin{aligned} &\text{*PATH-EXECUTION CONNECTIVITY (PEC)} \\ &M, \sigma \models \text{MayAccess}^{Dir, Now}(o, o') \implies \\ &\quad \text{MayAccess}^{Ind, Now}(o, o') \end{aligned}$$

By contraposition,

$$M, \sigma \models \neg \text{MayAccess}^{Indir, Now}(o, o') \implies \neg \text{MayAccess}^{Dir, Now}(o, o')$$

Note also that PEC is a direct interpretation from Rule 1, since rule 1 says owning a capability is the only way of sending messages to another object, and therefore implies a path between the objects.

Rule 2: Objects cannot forge capabilities, and only connectivity begets connectivity.

$$\begin{aligned} &\text{*GLOBAL PATH EXISTENCE (GPE)} \\ &M, \sigma \models [\exists Y^* \in \text{Obj. } \text{MayAccess}^{Ind, Now}(Y^*, o')] \\ &\quad \iff \\ &\quad [\exists X^* \in \text{Obj. } \text{MayAccess}^{Dir, Now}(X^*, o')] \end{aligned}$$

By contraposition,

$$M, \sigma \models [\forall X^* \in \text{Obj. } \neg \text{MayAccess}^{Dir, Now}(X^*, o')] \iff [\forall Y^* \in \text{Obj. } \neg \text{MayAccess}^{Ind, Now}(Y^*, o')]$$

In addition to path being a necessary condition for capability, GPE gives us an additional new relation between the two concepts over the entire system. GPE says that in a given system of objects, *iff* there exists an object Y^* which has a path to o' , then there exists an object X^* that has the capability of o' . Looking from the left to right direction, since the path from Y^* to o' exists, then there must exist an object X^* with a capability of o' so that the path from Y^* to o' is well-established. Moving from the right to left direction, GPE says that if an object X^* has a capability then there exist an object Y^* with a path to o' , and this can be proven from PEC or by definition when $(X^* == Y^*)$.

However, GPE only postulates the existence of some object with some capability iff there exists some object with some path, and says nothing about how the objects are connected. From the connectivity begets connectivity rule, PEC, and GPE, we construct global path-execution

and execution-execution relationships over the entire system:

$$\begin{aligned} &\text{*GLOBAL PATH-EXECUTION CONNECT. (GPEC)} \\ &M, \sigma \models \text{MayAccess}^{Ind, Now}(o, o') \\ &\quad \iff \\ &\quad \exists X^* \in \text{Obj. } [\text{MayAccess}^{Ind, Now}(o, X^*) \wedge \text{MayAccess}^{Dir, Now}(X^*, o')] \end{aligned}$$

By contraposition,

$$M, \sigma \models \forall X^* \in \text{Obj. } \neg [\text{MayAccess}^{Ind, Now}(o, X^*) \wedge \text{MayAccess}^{Dir, Now}(X^*, o')] \iff \neg \text{MayAccess}^{Ind, Now}(o, o')$$

GPEC introduces an intermediate object X^* between o and o' that makes explicit the missing connection in GPE.

The power in GPEC lies in the recursive predicate $\text{MayAccess}^{Ind, Now}(o, X^*)$ that can eventually be expanded into a set of $\text{MayAccess}^{Dir, Now}$ predicates that finishes with terminating predicate $\text{MayAccess}^{Ind, Now}(o, o)$, where the terminating predicate will always be true. We now look for a relation between a path configuration at a state σ (*Now*) and eventual path configurations arising from σ (*Eve*).

$$\begin{aligned} &\text{*EVENTUAL PATH CONNECTIVITY 1 (EPC1)} \\ &M, \sigma \models \text{MayAccess}^{Ind, Eve}(o, o') \\ &\quad \implies \\ &\quad \exists X^* \in \text{Obj. } [(\text{MayAccess}^{Ind, Now}(o, X^*) \vee \text{MayAccess}^{Dir, Now}(X^*, o)) \wedge \text{MayAccess}^{Ind, Eve}(X^*, o')] \end{aligned}$$

By contraposition,

$$M, \sigma \models \forall X^* \in \text{Obj. } [\neg \text{MayAccess}^{Ind, Now}(o, X^*) \wedge \neg \text{MayAccess}^{Dir, Now}(X^*, o)] \vee \neg [\text{MayAccess}^{Ind, Eve}(X^*, o')] \implies \neg \text{MayAccess}^{Ind, Eve}(o, o')$$

EPC1 has the meaning that if an object o has an eventual path to o' in some arising state σ' , then there must exist an object X^* that has an eventual path to o' , and there must exist a way for o to have a path to X^* in σ' . o either must already have a path to X^* in σ , or that it will eventually receive the capability of X^* in EPC1 is a representation of connectivity begets connectivity across time:

- **Initial Conditions or Endowment:** o has an existing path to o' in σ , therefore X^* refers to o'
- **Parenthood:** o will create o' in some arising σ' , therefore X^* refers to o
- **Introduction:** o will only obtain the path to o' in some arising σ' , therefore X^* refers to an object that is not the same object as o ($X^* \neq o$).

Note that for o to have an eventual path to o' , we require only o to have an eventual path to X^* since we have stated that X^* will have an eventual path to o' . If o already has a path to X^* in σ then we know o can reach X^* in σ' . If not, the capability of X^* must be introduced to o . For X^* to introduce itself, X^* must have the capability of o in σ' . Well, what if the capability of X^* is introduced by some *other* object \tilde{X}^* ? Note that in such a case, \tilde{X}^* will have the capability of X^* , and will therefore also be able to eventually have a path to o' . Also \tilde{X}^* must also be able to introduce itself to o . There is hence no logical difference between \tilde{X}^* and X^* in our formal description and \tilde{X}^* might simply be referred to as X^* .

The contraposition result of EPC1 says there can be no eventual paths from o to o' . This can be achieved from:

- Global two-way path isolation of o in present state σ , where there are no paths leading to o and no paths originating from o in σ
- Global one-way path isolation to o' in all possible states σ'

There is a final critical result from EPC1. Notice how, there is a 'recursive' $\text{MayAccess}^{\text{Ind,Eve}}(X^*, o')$ in our condition for $\text{MayAccess}^{\text{Ind,Eve}}(o, o')$. This allows us to recursively 'expand' the condition to incorporate *all* X^* intermediate objects in the path leading to o' that gives us both $\text{MayAccess}^{\text{Dir,Now}}$ and $\text{MayAccess}^{\text{Ind,Now}}$ predicates, where the terminating $\text{MayAccess}^{\text{Ind,Eve}}(o', o')$ always returns true. This result allows us to define $\text{MayAccess}^{\text{Ind,Eve}}(X^*, o')$ in a configuration completely based in σ .

What about capabilities? Using GPEC, we can always expand $\text{MayAccess}^{\text{Ind,Now}}(o, X^*)$

into a set of $\text{MayAccess}^{\text{Dir,Now}}$ predicates that terminate with $\text{MayAccess}^{\text{Ind,Now}}(o, o)$ which is always true. The final result we will get is a configuration based purely on $\text{MayAccess}^{\text{Dir,Now}}$ predicates!!!

*EVENTUAL PATH CONNECTIVITY 2 (EPC2)

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{\text{Ind,Eve}}(o, o') \\ \implies \\ \exists X^* \in \text{Obj}. \{ [\text{MayAccess}^{\text{Ind,Now}}(o, X^*) \vee \\ \text{MayAccess}^{\text{Dir,Now}}(X^*, o)] \\ \vee \\ \exists Y^* \in \text{Obj}. [\text{MayAccess}^{\text{Ind,Eve}}(X^*, Y^*) \wedge \\ \text{MayAccess}^{\text{Dir,Eve}}(Y^*, o')] \} \end{aligned}$$

By contraposition and De Morgan rules

$$\begin{aligned} M, \sigma \models \forall X^* \in \text{Obj}. \{ [\neg \text{MayAccess}^{\text{Ind,Now}}(o, X^*) \wedge \\ \neg \text{MayAccess}^{\text{Dir,Now}}(X^*, o)] \\ \vee \\ \neg \exists Y^* \in \text{Obj}. [\text{MayAccess}^{\text{Ind,Eve}}(X^*, Y^*) \wedge \\ \text{MayAccess}^{\text{Dir,Eve}}(Y^*, o')] \} \\ \implies \\ \neg \text{MayAccess}^{\text{Ind,Eve}}(o, o') \end{aligned}$$

The results of EPC2 are identical to EPC1, with the second condition of EPC1 expanded in EPC2 to say global one-way path isolation to o in all possible states σ' to mean there does not exist any eventual path from any object to an object Y^* that has the eventual capability of o' .

So far we have developed results for paths, but what about execution? We construct EEC from EPC1, the only difference being we now require all those paths in EPC1 to be traversable.

*EVENTUAL EXECUTION CONNECTIVITY (EEC)

$$\begin{aligned} M, \sigma \models \text{MayAccess}^{\text{Dir,Eve}}(o, o') \\ \implies \\ \exists X^* \in \text{Obj}. [(\text{MayAccess}^{\text{Dir,Now}}(o, X^*) \vee \\ \text{MayAccess}^{\text{Dir,Now}}(X^*, o)) \\ \wedge \\ \text{MayAccess}^{\text{Dir,Eve}}(X^*, o')] \end{aligned}$$

By contraposition,

$$\begin{aligned} M, \sigma \models \forall X^* \in \text{Obj}. \{ [\neg \text{MayAccess}^{\text{Dir,Now}}(o, X^*) \wedge \\ \neg \text{MayAccess}^{\text{Dir,Now}}(X^*, o)] \\ \vee \\ \neg [\text{MayAccess}^{\text{Dir,Eve}}(X^*, o')] \} \\ \implies \\ \neg \text{MayAccess}^{\text{Dir,Eve}}(o, o') \end{aligned}$$

The power of EEC is similar to EPC in that it allows an arbitrary recursive expansion of the $\text{MayAccess}^{\text{Dir,Eve}}(X^*, o')$ till the terminating $\text{MayAccess}^{\text{Dir,Eve}}(o', o')$ that is always true. We now turn our attention formalizing Ocap state changes rules in the system.

Rule 3: Objects may have private encapsulation of state and behaviour

*GLOBAL STATE CHANGE EXISTENCE (GSCE)

$$\begin{aligned} M, \sigma \models [\exists X^* \in \text{Obj. } \text{MayAffect}^{\text{Now}}(X^*, o')] \\ \implies \\ [\exists Y^* \in \text{Obj. } \text{MayAccess}^{\text{Dir,Now}}(Y^*, o')] \\ \implies \\ [\exists Z^* \in \text{Obj. } \text{MayAccess}^{\text{Ind,Now}}(Z^*, o')] \end{aligned}$$

By contraposition,

$$\begin{aligned} M, \sigma \models [\forall Z^* \in \text{Obj. } \neg \text{MayAccess}^{\text{Ind,Now}}(Z^*, o')] \\ \implies \\ [\forall Y^* \in \text{Obj. } \neg \text{MayAccess}^{\text{Dir,Now}}(Y^*, o')] \\ \implies \\ [\forall X^* \in \text{Obj. } \neg \text{MayAffect}^{\text{Dir,Now}}(X^*, o')] \end{aligned}$$

GSCE can be derived from our predicate definitions. The first implication states that if an object can change the state of o' , then there must exist an object in the system that holds the capability of o' . The second implication is that there must exist an object in the system that holds a path to o' . We view reasoning about state change as reasoning about protection, which we elaborate in the next subsection.

3.4 Protection

To reason about enforcing protection, we focus on finding the necessary conditions for the weaker predicate $\text{MayAffect}^{\text{Eve}}$ rather than $\text{MayAffect}^{\text{Now}}$ in the antecedent. This is because negation on both sides of the implication, would yield a stronger $\neg \text{MayAffect}^{\text{Eve}}$ in the consequent, which is our area of interest (since it represents state protection). In practical terms, if we are concerned with the protection of o' from o , it is also often not very useful to have a policy where $\neg \text{MayAffect}^{\text{Now}}(o, o')$ holds but $\neg \text{MayAffect}^{\text{Eve}}(o, o')$ does not. Furthermore, by ensuring $\neg \text{MayAffect}^{\text{Eve}}(o, o')$ holds, we can also ensure $\neg \text{MayAffect}^{\text{Now}}(o, o')$ holds since by contraposition:

$$\begin{aligned} [\text{MayAffect}^{\text{Now}}(o, o') \implies \text{MayAffect}^{\text{Eve}}(o, o')] \\ \implies \\ [\neg \text{MayAffect}^{\text{Eve}}(o, o') \implies \neg \text{MayAffect}^{\text{Now}}(o, o')] \end{aligned}$$

Furthermore, in building the necessary conditions for the predicate $\text{MayAffect}^{\text{Eve}}$, we are also more concerned with finding some structure that contains the configuration of $\text{MayAccess}^{*,\text{Now}}$, rather than $\text{MayAccess}^{*,\text{Eve}}$. This is because it is much easier to prove a configuration of relations that holds in *one* specific state than think about whether a configuration holds in *all* possible eventual states, which makes the former much easier to implement.

To begin, we simplify our reasoning, we introduce the assumption that all fields in our objects can only be declared private. Consequently, this implies the necessary condition that an object's state can only be modified if one of it's behaviour is called, and therefore require at least one other object in the system that holds its capability. We do not think this is restrictive in any case, the programmer merely has to write explicitly a method to return an object's field.

*PRIVATE FIELDS ASSUMPTION (PFA)

$$M, \sigma \models \exists X^* \in \text{Obj. } \text{MayAffect}^{\text{Now}}(X^*, o') \implies \exists Y^* \in \text{Obj. } \text{MayAccess}^{\text{Dir,Now}}(Y^*, o')$$

By contraposition,

$$M, \sigma \models \forall Y^* \in \text{Obj. } \neg \text{MayAccess}^{\text{Dir,Now}}(Y^*, o') \implies \forall X^* \in \text{Obj. } \neg \text{MayAffect}^{\text{Now}}(X^*, o')$$

PFA means that in order for an object X^* 's state to change, it must be done through some object Y^* calling its behaviour (Y^* can refer to the same object as X^*). Equivalently, denying all objects in the system the ability to call an object's behaviour implies that no object can modify the object's state.

3.4.1 Protection through possible paths

We now divert our attention to reasoning about the relationship between protection of state (MayAffect) and paths ($\text{MayAccessInd}, *$). The question we ask is what is the relation between state protection in eventual outcomes, and present path configurations? We build this relationship from the basics by progressively finding stronger conditions of MayAffect . We begin with the first condition, which says that

for an object to affect another, an *eventual* path has to exist. This can be derived from the definitions of our predicates.

***NECESSARY PATH CONDITION 1 (NPC1)**

$$M, \sigma \models \text{MayAffect}^{Eve}(o, o') \implies \text{MayAccess}^{Ind, Eve}(o, o')$$

By contraposition,

$$M, \sigma \models \neg \text{MayAccess}^{Ind, Eve}(o, o') \implies \neg \text{MayAffect}^{Eve}(o, o')$$

Here, we immediately see a first defensive outcome of the OCap model. Having no eventual paths from object o to o' guarantees that the state of object o' cannot be modified by object o .

So far our results serve as a good base to enforce $\neg \text{MayAffect}^{Eve}(o, o')$ but we require *stronger* necessary conditions, because enforcing protection of an object's state with just these conditions require the impractical configuration that o is eventually path-isolated from o' on the reference graph. Cooperation between objects imply that there needs to be some path established between the objects for interaction to take place. Therefore, we can expect neither $\neg \text{MayAccess}^{Ind, Now}(o, o')$ nor $\neg \text{MayAccess}^{Ind, Eve}(o, o')$ to hold in a system that allows cooperation between o and o' .

What about present path configurations? Using NPC1 and the results of EPC1, we derive NPC2 below which is a relation between protection of o' in eventual states, and *present* path configurations between o and o' .

***NECESSARY PATH CONDITION 2 (NPC2)**

$$\begin{aligned} M, \sigma \models \text{MayAffect}^{Eve}(o, o') &\implies \\ &\exists X^* \in \text{Obj}. [(\text{MayAccess}^{Ind, Now}(o, X^*) \vee \\ &\quad \text{MayAccess}^{Dir, Now}(X^*, o)) \wedge \\ &\quad \text{MayAccess}^{Ind, Eve}(X^*, o')] \end{aligned}$$

By contraposition and De Morgan rules,

$$\begin{aligned} M, \sigma \models \forall X^* \in \text{Obj}. [\neg \text{MayAccess}^{Ind, Now}(o, X^*) \wedge \\ \neg \text{MayAccess}^{Dir, Now}(X^*, o)] &\implies \\ \neg \text{MayAccess}^{Ind, Eve}(X^*, o') &\implies \\ \neg \text{MayAffect}^{Eve}(o, o') &\end{aligned}$$

The interpretation of NPC2 is identical to EPC1, with protection of state being made an explicit

consequent from the conditions of EPC1.

We now examine whether it is possible to build a relation between MayAffect^{Eve} and $\text{MayAccess}^{Dir, Eve}$. Similarly, NPC2 can be augmented by EPC2 which results in NPC3:

***NECESSARY PATH CONDITION 3 (NPC3)**

$$\begin{aligned} M, \sigma \models \text{MayAffect}^{Eve}(o, o') &\implies \\ &\exists X^* \in \text{Obj}. \{ [\text{MayAccess}^{Ind, Now}(o, X^*) \vee \\ &\quad \text{MayAccess}^{Dir, Now}(X^*, o)] \\ &\quad \vee \\ &\quad \exists Y^* \in \text{Obj}. [\text{MayAccess}^{Ind, Eve}(X^*, Y^*) \wedge \\ &\quad \text{MayAccess}^{Dir, Eve}(Y^*, o')] \} \end{aligned}$$

By contraposition and De Morgan rules

$$\begin{aligned} M, \sigma \models \forall X^* \in \text{Obj}. \{ [\neg \text{MayAccess}^{Ind, Now}(o, X^*) \wedge \\ \neg \text{MayAccess}^{Dir, Now}(X^*, o)] \\ \vee \\ \neg \exists Y^* \in \text{Obj}. [\text{MayAccess}^{Ind, Eve}(X^*, Y^*) \wedge \\ \text{MayAccess}^{Dir, Eve}(Y^*, o')] \} &\implies \\ \neg \text{MayAffect}^{Eve}(o, o') &\end{aligned}$$

We are at the finishing line. The Ind,Now predicates can be expanded using GPEC to obtain direct capabilities. Ind,Eve can be expanded using EPC2. Dir,Eve can be expanded using EEC.

3.4.2 A note on execution and protection

$$M, \sigma \models \text{MayAffect}^{Eve}(o, o') \not\Rightarrow \text{MayAccess}^{Dir, Eve}(o, o')$$

$$M, \sigma \models \text{MayAffect}^{Eve}(o, o') \implies \text{MayAccess}^{Ind, Eve}(o, o')$$

***NECESSARY EXECUTION CONDITION 1 (NEC1)**

$$M, \sigma \models \text{MayAffect}^{Eve}(o, o') \implies \exists X^* \in \text{Obj}. \text{MayAccess}^{Dir, Eve}(X^*, o')$$

By contraposition and quantifier equivalence,

$$M, \sigma \models [\forall X^* \in \text{Obj}. \neg \text{MayAccess}^{Dir, Eve}(X^*, o')] \implies \neg \text{MayAffect}^{Eve}(o, o')$$

NEC1 is a stronger version of NPC1 and says that in order for an object o to modify the state of o' , there must exist an object X^* that has a direct path to o' , and that X^* can traverse such a path. This is derived trivially from our PFA assumption in the beginning. Consequently,

in our contraposition result, we can deny *all* objects in our system capability of o' to enforce the protection of o' from o . NEC1 does not yield a very useful result, as this is just another way of implementing protection of o' from o through denying all paths to o' in the system reference graph. To see why denying all objects the capability of o' is equivalent to denying all paths to o' , see the contraposition result from GPE.

In NEC1, if X^* refers to the same object as o , then we have a straightforward configuration where object o has the capability of o' and can therefore affect o' . However, very crucially, o having the capability of o' is *not* a sufficient condition—denying o the capability of o' does *not* deny o the ability to affect o' , since X^* can refer to an object that is *not* o . NEC2 below is an expansion of NEC1 to illustrate this crucial point.

***NECESSARY EXECUTION CONDITION 2 (NEC2)**

$$\begin{aligned} M, \sigma \models \text{MayAffect}^{Eve}(o, o') &\implies \\ &[\text{MayAccess}^{Dir, Eve}(o, o') \vee \\ &\exists X^* \in \text{Obj}, X^* \neq o. \text{MayAccess}^{Dir, Eve}(X^*, o')] \end{aligned}$$

By contraposition,

$$\begin{aligned} M, \sigma \models [\neg \text{MayAccess}^{Dir, Eve}(o, o') \wedge \\ \forall X^* \in \text{Obj}, X^* \neq o. \neg \text{MayAccess}^{Dir, Eve}(X^*, o')] \\ \implies \neg \text{MayAffect}^{Eve}(o, o') \end{aligned}$$

We now examine the second half of the necessary condition in NEC2:

$[\exists X^* \in \text{Object}, X^* \neq o. \text{MayAccess}^{Dir, Eve}(X^*, o')]$ which means that there exists object X^* that is *not* object o , that must have the capability of o' . But this does not say anything about o and X^* . We need to connect o to X^* , because NPC1 says $\text{MayAffect}^{Eve}(o, o')$ implies that o must have some indirect path to o' .

***NECESSARY EXECUTION CONDITION 3 (NEC3)**

$$\begin{aligned} M, \sigma \models \text{MayAffect}^{Eve}(o, o') \\ \implies \\ \text{MayAccess}^{Dir, Eve}(o, o') \vee \\ [\exists X^* \in \text{Obj}, X^* \neq o. \text{MayAccess}^{Dir, Eve}(o, X^*) \wedge \\ \text{MayAccess}^{Dir, Eve}(X^*, o')] \end{aligned}$$

By contraposition,

$$\begin{aligned} M, \sigma \models \neg \text{MayAccess}^{Dir, Eve}(o, o') \wedge \\ \neg [\exists X^* \in \text{Obj}, X^* \neq o. \text{MayAccess}^{Dir, Eve}(o, X^*) \wedge \\ \text{MayAccess}^{Dir, Eve}(X^*, o')] \\ \implies \end{aligned}$$

$$\neg \text{MayAffect}^{Eve}(o, o')$$

NEC3 is not very useful because we do not have any knowledge of how the system's path or capability configuration should look like at σ for us to enable protection of o' in all possible states arising from σ . We now incorporate our results of EEC to expand $\text{MayAccess}^{Dir, Eve}$ that will give us the present configuration of paths and capabilities.

***NECESSARY EXECUTION CONDITION 4 (NEC4)**

$$\begin{aligned} M, \sigma \models \text{MayAffect}^{Eve}(o, o') &\implies \\ &\exists X^* \in \text{Obj}. [(\text{MayAccess}^{Dir, Now}(o, X^*) \vee \\ &\quad \text{MayAccess}^{Dir, Now}(X^*, o)) \\ &\quad \wedge \\ &\quad \text{MayAccess}^{Dir, Eve}(X^*, o')] \\ &\vee \\ &\{\exists X^* \in \text{Obj}, X^* \neq o. \\ &\quad \exists X^1 \in \text{Obj}. [(\text{MayAccess}^{Dir, Now}(o, X^1) \vee \\ &\quad \text{MayAccess}^{Dir, Now}(X^1, o)) \\ &\quad \wedge \\ &\quad \text{MayAccess}^{Dir, Eve}(X^1, X^*)] \\ &\quad \wedge \\ &\quad \exists X^2 \in \text{Obj}. [(\text{MayAccess}^{Dir, Now}(X^*, X^2) \vee \\ &\quad \text{MayAccess}^{Dir, Now}(X^2, X^*)) \\ &\quad \wedge \\ &\quad \text{MayAccess}^{Dir, Eve}(X^2, o')] \} \end{aligned}$$

By contraposition,

...

From NEC4 we see the power of OCap patterns hence lies in providing concrete examples of a system of cooperation that allows the existence of paths between objects for cooperation while still dictating the degree of control of one object can have over another. The logics we have developed so far illuminate the power of attenuating objects X^* that can enable protection. Indeed attenuating objects feature prominently in the literature of OCap patterns which we shall see in the next section.

3.5 Pattern 1: The JavaScript DOM Tree

We use a JavaScript DOM Tree OCap pattern largely inspired by the example in Devriese et al.[?] where they use a Kripke worlds framework to reason about the pattern. We define the following variables throughout our pattern:

- $o, o' \in \text{Object}$

- $\text{Node}, \text{ReNode} \subseteq \text{Object}$
- $n, n' \in \text{Node}$
- $rn, rn' \in \text{ReNode}$

***NODE VULNERABILITY**

$$\begin{aligned} &\forall o, n. \text{MayAccess}^{Dir, Now}(o, n) \\ &\quad \implies \\ &\quad \text{MayAffect}^{Now}(o, n) \wedge \\ &\quad \forall n'. \text{MayAccess}^{Dir, Now}(o, n') \end{aligned}$$

The vulnerability of a node lies in the fact that it contains a public method `setProperty(key, value)` that will modify an internal mapping data structure. A node also has a public field `parent` that will return the capability of its parent node. Consequently, this allows an object which has the capability of any one node in the tree to navigate up to the root node (Document), and consequently navigate to all other nodes in the tree.

***POLICY 1: NECESSARY CONDITION**

$$\begin{aligned} &\forall n, o, RN \subseteq \text{ReNode}. \\ &\quad \text{Dom}(RN, n) \wedge \text{MayAffect}^{Eve}(o, n) \\ &\quad \implies \\ &\quad \exists rn \in RN. \text{MayAccess}^{Dir, Now}(o, rn) \\ &\quad \wedge \text{MayAccess}^{Dir, Now}(rn, n) \end{aligned}$$

This policy states that if an Object o may affect the state of a Node n , and that n is dominated(protected) by a set of ReNodes RN , then it implies that a path exists from o to some rn in RN , and that rn has strong access to n . From Policy 1, using contraposition, we derive the relation:

$$\begin{aligned} &\forall n, o, RN \subseteq \text{ReNode}. \\ &\quad [\forall rn \in RN. \neg \text{MayAccess}^{Ind, Eve}(o, rn) \vee \\ &\quad \forall rn \in RN. \neg \text{MayAccess}^{Dir, Eve}(rn, n)] \\ &\quad \implies \neg \text{MayAffect}^{Eve}(o, n) \vee \neg \text{Dom}(RN, n) \end{aligned}$$

Note that without prescribing any rules to ReNode, we can deny object o the ability to affect node n by enforcing that no path exists from o to any rn in the set RN that dominates n , which by implication is another way of saying isolation from o to n , since:

$$\begin{aligned} &\forall n, o. \text{Dom}(RN, n) \wedge \\ &\forall rn \in RN. \neg \text{MayAccess}^{Ind, Eve}(o, rn) \implies \\ &\quad \neg \text{MayAccess}^{Ind, Eve}(o, n). \end{aligned}$$

Another implication is that we can also deny object o the ability to affect node n by enforcing $\forall rn \in RN. \neg \text{MayAccess}^{Dir, Eve}(rn, n)$. This is

however, *not* enforceable. This is because by definition a ReNode rn holds a field containing the capability of the node n it is meant to protect when the ReNode is constructed, and field that holds the capability of the node is private and constant, that cannot be subsequently changed or removed. Consequently, there must exist at least one ReNode rn in the dominating RN set that holds the capability of n :

$$\begin{aligned} &\exists rn \in RN. \text{Dom}(RN, n) \wedge \text{MayAccess}^{Dir, Eve}(rn, n) \\ &\quad \implies \\ &\quad \neg(\forall rn \in RN. \neg \text{MayAccess}^{Dir, Eve}(rn, n)) \end{aligned}$$

POLICY 2: DOMINATION OF NODES

3.6 Pattern 2: Caretaker

3.7 Pattern 3: Membrane

Policy 1:

References

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