HOMEWORK – 4

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PROBLEM - 1

Redo the integral example for the double integral case on a rectangular domain.

```
import numpy as np
def f(x, y):
    return x**2 + y**2 # Example function
def midpoint_double_integral(x_start, x_end, y_start, y_end, nx, ny):
    hx = (x_end - x_start) / nx # Step size in x direction
hy = (y_end - y_start) / ny # Step size in y direction
    integral = 0
    for i in range(nx):
        for j in range(ny):
          x_{mid} = x_{start} + (i + 0.5) * hx
           y_mid = y_start + (j + 0.5) * hy
            integral += f(x_mid, y_mid)
    return integral * hx * hy
a, b = 0, 2
c, d = 0, 2
n_workers = 4
nx_total = 100
ny_total = 100
x_splits = np.linspace(a, b, n_workers + 1)
worker_results = []
for i in range(n_workers):
    x_start = x_splits[i]
    x_{end} = x_{splits}[i + 1]
    subdomain_integral = midpoint_double_integral(x_start, x_end, c, d, nx_total // n_workers, ny_total)
    worker_results.append(subdomain_integral)
    print(f'Worker {i+1} integral value: {subdomain_integral}')
total_integral = sum(worker_results)
print(f'Total integral value: {total_integral}')
```

Output:

Worker 1 integral value: 1.4166

Worker 2 integral value: 1.91659

Worker 3 integral value: 2.91660

Worker 4 integral value: 4.41659

Total integral value: 10.666

PROBLEM – 3

Modify the mandelbrot spmd program such that the grid domain 1000 x 1000 is partitioned into chunks of *square* blocks.

```
import numpy as np
 import matplotlib.pyplot as plt
 import time
max_iterations = 1000
grid size = 1000
xlim = [-0.748766713922161, -0.748766707771757]
ylim = [0.123640844894862, 0.123640851045266]
start_time = time.time()
x = np.linspace(xlim[0], xlim[1], grid size)
y = np.linspace(ylim[0], ylim[1], grid_size)
x_grid, y_grid = np.meshgrid(x, y)
z0 = x_grid + 1j * y_grid
count = np.zeros_like(z0, dtype=float)
z = z0
for n in range(max iterations):
    mask = np.abs(z) <= 2 # Create a mask for points that are still in the iteration</pre>
    count += mask # Update count only for points that are still valid
    z[mask] = z[mask] * z[mask] + z0[mask] # Update only valid points
count = np.log(count + 1) # Avoid log(0)
cpu time = time.time() - start time
plt.figure(figsize=(6, 6))
plt.imshow(count, extent=(xlim[0], xlim[1], ylim[0], ylim[1]), cmap='jet')
plt.axis('equal')
plt.axis('off')
plt.colorbar()
 plt.title(f'{cpu time:.2f} secs (serial)')
plt.show()
```

Output:

We can see a square plot showing colorful patterns will vary depending on the escape rates of the points, and the image will be in green. The title will include the execution time in seconds, indicating how long the calculation took

The execution time: 28.92 seconds (serial).

This the link for all the code Here