

4. (8 points) Composition

- (a) (4 pt) Implement `compose`, which takes a positive integer `n`. It returns a function that, when called repeatedly on n one-argument functions f_1, f_2, \dots, f_n , returns a one-argument function of `x` that returns $f_1(f_2(\dots f_n(x) \dots))$. You may **not** call the `compose1` function from the Midterm 1 Study Guide.

```
def compose(n):
    """Return a function that, when called n times repeatedly on unary
    functions f1, f2, ..., fn, returns a function g(x) equivalent to
    f1(f2( ... fn(x) ... )).

    >>> add1 = lambda y: y + 1
    >>> compose(3)(abs)(add1)(add1)(-4)  # abs(add1(add1(-4)))
    2
    >>> compose(3)(add1)(add1)(abs)(-4)  # add1(add1(abs(-4)))
    6
    >>> compose(1)(abs)(-4)               # abs(-4)
    4
    """
    assert n > 0

    if n == 1:

        return lambda f: f

    def call(f):

        def on(g):

            return compose(n-1)(lambda x: f(g(x)))

        return on

    return call
```

- 1.5 Write a procedure `merge(n1, n2)` which takes numbers with digits in decreasing order and returns a single number with all of the digits of the two, in decreasing order. Any number merged with 0 will be that number (treat 0 as having no digits). Use recursion.

Hint: If you can figure out which number has the smallest digit out of both, then we know that the resulting number will have that smallest digit, followed by the merge of the two numbers with the smallest digit removed.

```
def merge(n1, n2):
    """ Merges two numbers
    >>> merge(31, 42)
    4321
    >>> merge(21, 0)
    21
    >>> merge (21, 31)
    3211
    """

    if n1 == 0:
        return n2
    elif n2 == 0:
        return n1
    elif n1 % 10 < n2 % 10:
        return merge(n1 // 10, n2) * 10 + n1 % 10
    else:
        return merge(n1, n2 // 10) * 10 + n2 % 10
```