

In 2020, published an article claiming that “**Women in Singapore earn 6% less than men for similar work: MOM study**”. This indicates that women are getting S\$342 less in median monthly salary than men who are holding similar jobs. However, the 6% gap was after adjustment such as worker’s industry, occupation, age and education. Prior to adjustment, the median pay difference between man and woman is 16.3%. Hence, the reason for the 6% gap was assumed due to factors such as firm type, position within the industry, work experience, caregiving responsibilities and discrimination.

Therefore, is there a gender pay gap in Singapore, considering both genders are full time employees, in similar industry, position and holds the same educational level?

As this would be a sensitive subject, all data collection will be done through official government websites and based on two different sets of data.

Hypothesis

Let μ_{male} be the mean income for male

Let μ_{female} be the mean income for female

$$H_0: \mu_{male} - \mu_{female} = 0$$

$$H_1: \mu_{male} - \mu_{female} > 0$$

Data Criteria:

- 1) Population: Working adults in Singapore at the age of 25 – 64 old working adults
- 2) Sample: Employed working adults in Singapore at the age of 25 – 64, split between both genders
- 3) Sampling Method: Simple random sampling
- 4) Sample Size: 100 different samples across each gender, different occupations and position
- 5) Data Types: Quantitative Data Sets
- 6) Hypothesis Test: Two sample independent T-Test
- 7) Possible Errors: Type II

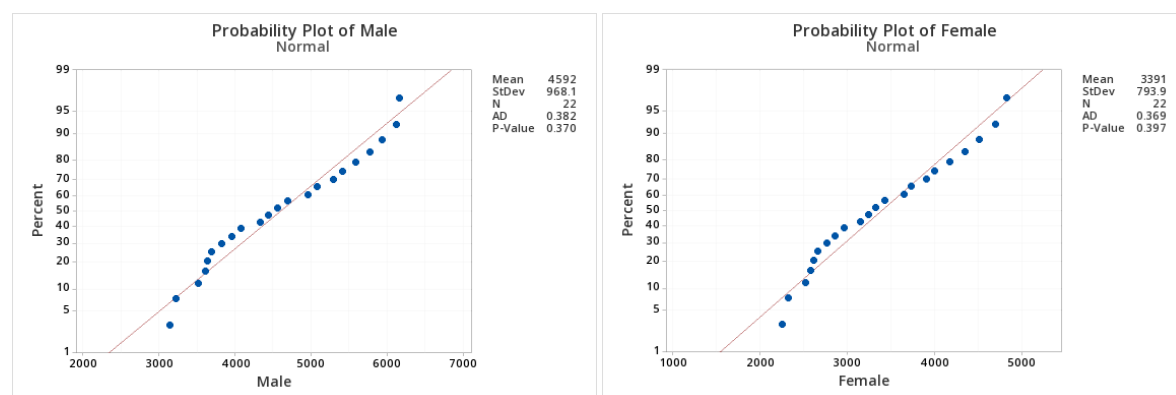
Data Sets:

- 1) Average Mean Salary by Gender year on year regardless of occupation
- 2) Median Salary Breakdown by Occupation and Gender regardless of timeline

Performing Normality Test on Average Mean Salary by Gender

H_0 : Data follow a normal distribution

H_1 : Data do not follow a normal distribution



Both samples have **P-values more than 0.05**, hence the Null Hypothesis is not rejected and the data follows a normal distribution.

Testing for Equal Variance on Average Mean Salary by Gender

Descriptive Statistics

Variable	N	StDev	Variance	95% CI for σ^2
Male	22	968.108	937233.041	(554749.646, 1914041.575)
Female	22	793.902	630281.076	(373064.317, 1287176.326)

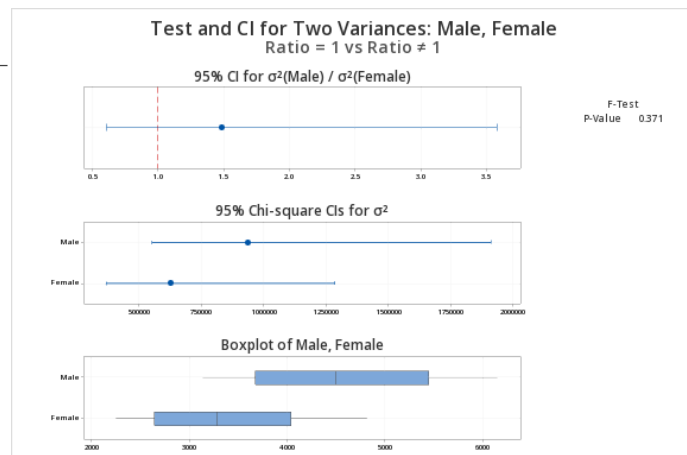
Ratio of Variances

Estimated Ratio	95% CI for Ratio using F
1.48701	(0.617, 3.582)

Test

Null hypothesis	$H_0: \sigma_1^2 / \sigma_2^2 = 1$
Alternative hypothesis	$H_a: \sigma_1^2 / \sigma_2^2 \neq 1$
Significance level	$\alpha = 0.05$

Test				
Method	Statistic	DF1	DF2	P-Value
F	1.49	21	21	0.371



P-value of F-test = $0.371 > \alpha = 5\%$

Also, the 95% confidence interval for the ratio of variances is $0.617 < \mu < 3.582$, which includes 1. Therefore, do not reject H_0 and the variances of control and treatment groups are equal.

Two Sample T-Test on Average Mean Salary by Gender

Descriptive Statistics

Sample	N	Mean	StDev	SE Mean
Male	22	4592	968	206
Female	22	3391	794	169

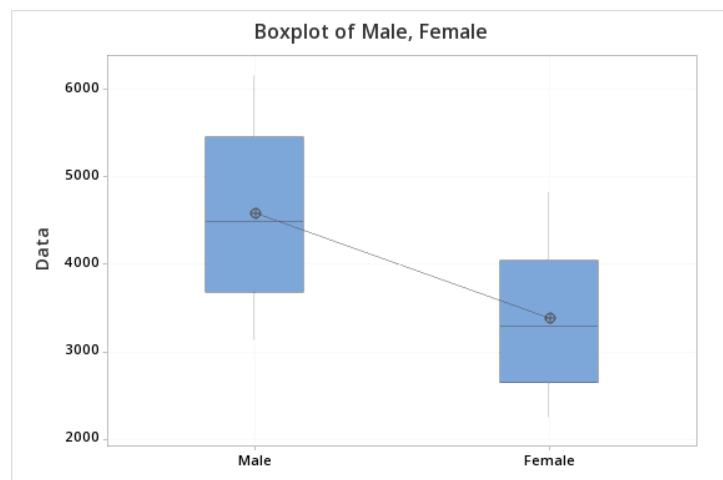
Estimation for Difference

Difference	Pooled StDev	95% Lower Bound for Difference
1201	885	752

Test

Null hypothesis	$H_0: \mu_1 - \mu_2 = 0$
Alternative hypothesis	$H_a: \mu_1 - \mu_2 > 0$

T-Value	DF	P-Value
4.50	42	0.000



$$\bar{x}_1 = 4592 \quad \bar{x}_2 = 3391 \quad \bar{x}_1 - \bar{x}_2 = 1201 \quad \text{d.f.} \approx 42 \quad \text{Test statistic} = 4.50 \quad \text{P-value} = 0.000$$

The 95% confidence bound for $\mu_1 - \mu_2$ is: > 752

Conclusion

Since $\text{P-value} = 0.000 < \alpha = 5\%$, it is rare to get a difference of sample mean Salary as extreme as 1201, if the population mean difference is 0.

We are 95% confident that the population mean difference falls above 752, which does not include the claimed difference of 0.

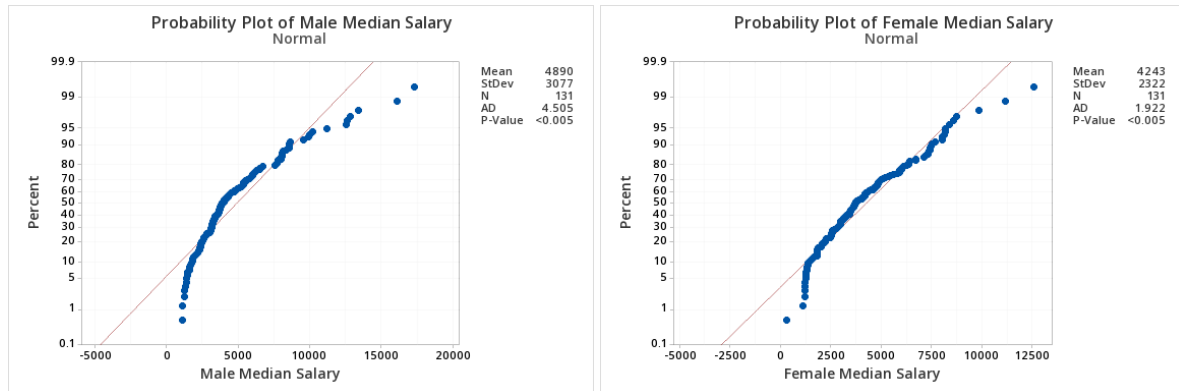
Therefore, we reject H_0 at $\alpha = 5\%$.

Hence, we can conclude that there is a difference in the average salary between male and female.

Performing Normality Test on Median Salary Breakdown by Occupation and Gender

H0: Data follow a normal distribution

H1: Data do not follow a normal distribution



Both samples have **P-values more than 0.05**, hence the Null Hypothesis is rejected and the data follows a non normal distribution. However, due to the **sample size more than 30**, Central Limit Theorem applies, therefore we are able to proceed with the T-Test.

Testing for Equal Variance on Median Salary Breakdown by Occupation and Gender

Descriptive Statistics

Variable	N	StDev	Variance	95% CI for σ^2
Male Median Salary	131	3076.503	9464868.930	(6459279.351, 1.42935E+07)
Female Median Salary	131	2322.194	5392582.719	(4103140.490, 7304170.195)

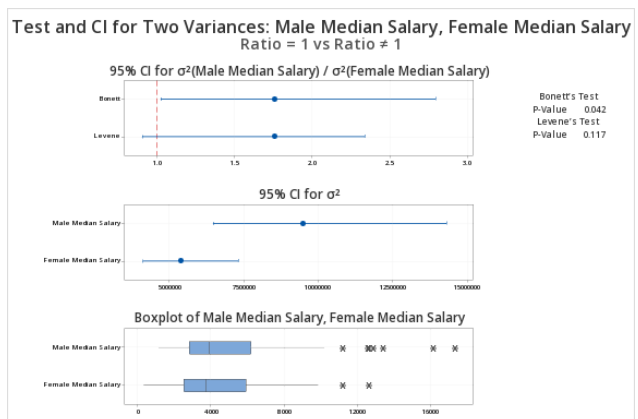
Ratio of Variances

Estimated Ratio	95% CI for Ratio using Bonett	95% CI for Ratio using Levene
1.75516	(1.022, 2.793)	(0.903, 2.336)

Test

Null hypothesis $H_0: \sigma_1^2 / \sigma_2^2 = 1$
Alternative hypothesis $H_1: \sigma_1^2 / \sigma_2^2 \neq 1$
Significance level $\alpha = 0.05$

Method	Test Statistic	DF1	DF2	P-Value
Bonett	4.12	1		0.042
Levene	2.48	1	260	0.117



P-value of Levene's F -test = **0.117** $>$ $\alpha = 5\%$

Also, the 95% confidence interval for the ratio of variances is **0.903** $<$ μ $<$ **2.336**, which includes 1. Therefore, do not reject H_0 and the variances of control and treatment groups are equal.

Two Sample T-Test on Median Salary Breakdown by Occupation and Gender

Descriptive Statistics

Sample	N	Mean	StDev	SE Mean
Male Median Salary	131	4890	3077	269
Female Median Salary	131	4243	2322	203

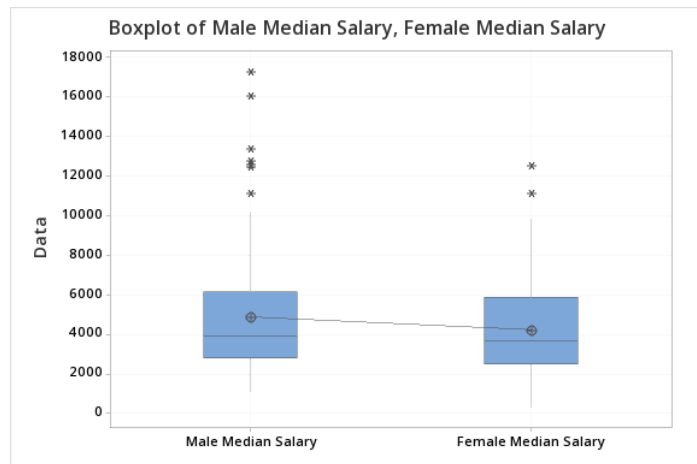
Estimation for Difference

Difference	Pooled StDev	95% Lower Bound for Difference
648	2726	92

Test

Null hypothesis $H_0: \mu_1 - \mu_2 = 0$
 Alternative hypothesis $H_1: \mu_1 - \mu_2 > 0$

T-Value	DF	P-Value
1.92	260	0.028



$$\bar{x}_1 = 4890 \quad \bar{x}_2 = 4243 \quad \bar{x}_1 - \bar{x}_2 = 648 \quad \text{d.f.} \approx 260 \quad \text{Test statistic} = 1.92 \quad \text{P-value} = 0.028$$

The 95% confidence bound for $\mu_1 - \mu_2$ is: > 92

Conclusion

Since $\text{P-value} = 0.028 < \alpha = 0.05$, it is rare to get a difference of sample median Salary as extreme as 648, if the population mean difference is 0.

We are 95% confident that the population mean difference falls above 92, which does not include the claimed difference of 0.

Therefore, we reject H_0 at $\alpha = 5\%$.

Hence, we can conclude that there is a difference in the average salary between male and female.

In summary, we conclude that there is a gender income gap between male and female working adults. Despite government initiative to work on closing the gap, there is still room for improvement.

Reference:

<https://www.channelnewsasia.com/news/singapore/women-singapore-earn-6-per-cent-less-than-men-wage-gap-12247034>

<https://stats.mom.gov.sg/genderpaygap/index.aspx>

<https://www.randstad.com.sg/career-advice/career-development/what-women-and-men-can-do-to-close-the-gender-pay-gap/>

<https://data.gov.sg/dataset/average-mean-monthly-nominal-earnings-per-employee-by-sex-annual>