

# Spring-2023 (Decipher)

2

a) Here, positive pulse: 0  
negative pulse: 1

$$\text{Data rate} = 2f \text{ bps}$$

$$\text{Duration of each pulse} = 1/2f$$

$$S(t) = A \times (4/\pi) \times \sum_{k \text{ odd}, k=1}^{\infty} \sin(2\pi kt)/k$$

Case-1:

$$\text{Let, } f = 10^6 \text{ cycle/sec} = 1 \text{ MHz}$$

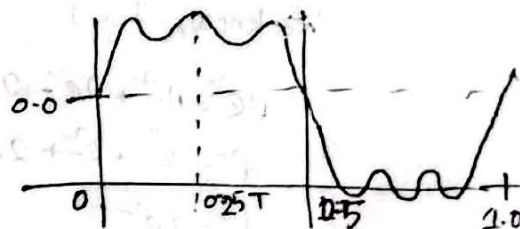
$$\text{Frequency components} = 1f, 3f, 5f$$

$$\text{Bandwidth} = 5f - 1f = 4f = 4 \times 1 \text{ MHz} = 4 \text{ MHz}$$

$$\text{Time period, } T = \frac{1}{10^6} = 10^{-6} = 1 \mu\text{s}$$

$$\text{Duration of each pulse} = \frac{1}{2 \times (10^6)} \quad [2 \text{ because 1 bit occurs at every } 0.5 \mu\text{s}]$$

$$\text{Data Rate} = 2 \times 1 = 2 \text{ mbps}$$



Case-2: (Frequency increased)

$$\text{Let, } f = 2 \times 10^6 \text{ cycle/sec} = 2 \text{ MHz}$$

$$\text{Frequency component} = 1f, 3f, 5f$$

$$\text{Bandwidth} = 5f - 1f = 4f = 4 \times 2 = 8 \text{ MHz}$$

$$\text{Time period, } T = \frac{1}{2 \times 10^6} = 0.5 \mu\text{s}$$

$$\text{Duration of each pulse} = \frac{1}{2 \times (2 \times 10^6)} \quad [4 \text{ because 1 bit occurs at every } 0.25 \mu\text{s}]$$

$$\text{Data Rate} = 2f = 2 \times 2 = 4 \text{ mbps}$$



Case-3: (Frequency component decreased)

$$\text{Let, } f = 2 \times 10^6 \text{ cycle/sec} = 2 \text{ MHz}$$

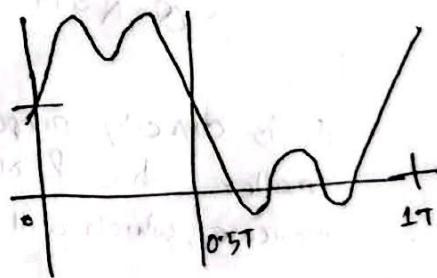
$$\text{Frequency component} = 1f, 3f$$

$$\text{Bandwidth} = 3f - 1f = 2f = 2 \times 2 = 4 \text{ MHz}$$

$$\text{Time period, } T = \frac{1}{f} = \frac{1}{2 \times 10^6} = 0.5 \mu\text{s}$$

$$\text{Duration of each pulse} = \frac{1}{2 \times (2 \times 10^6)}$$

$$\text{Data Rate} = 2f = 2 \times 2 \times 10^6 = 4 \text{ mbps}$$



From Case 1 and 2:

- Bandwidth increases
- data rate increases
- same signal quality

From 1 and 3:

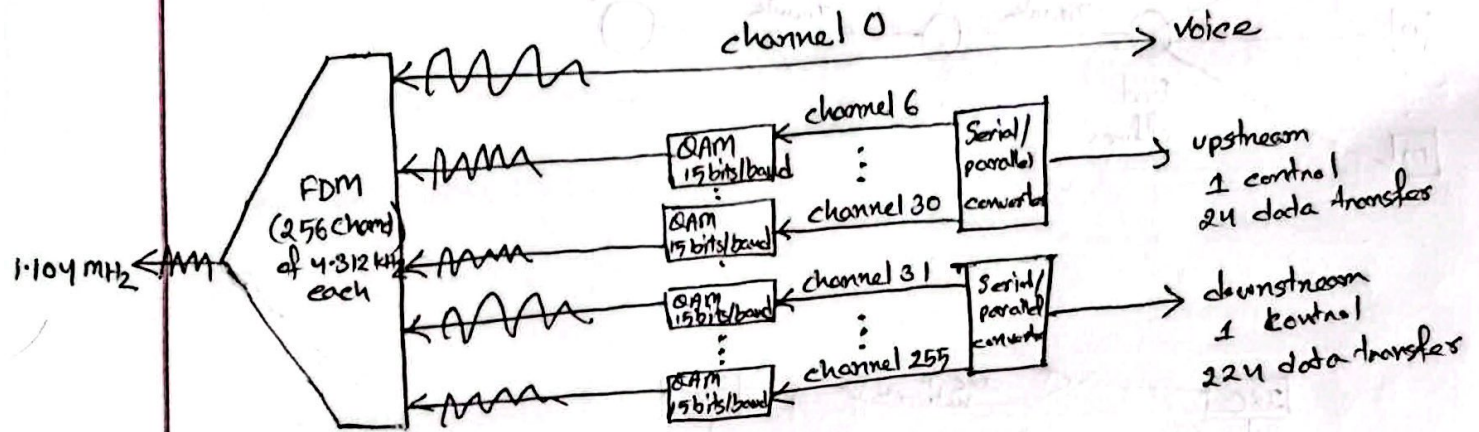
- Same bandwidth
- data rate decreases
- signal quality increases

From 2 and 3:

- Same data rate
- Bandwidth increases
- higher signal quality.

2(a)

Discrete Multitone Technique (DMT) is a modulation technique standard for ADSL which combines QAM and FDM.



Each channel bandwidth of  $= 4.312 \text{ kHz} \approx 4 \text{ kHz}$

QAM speed = 15 bits/byte

upstream: (6 to 30) = 24 channel

speed:  $24 \times 15 \times 4 = 1440 \text{ kbps} = 1.440 \text{ mbps}$

downstream: (31 to 255) = 224

speed:  $224 \times 15 \times 4 = 13440 \text{ kbps} = 13.440 \text{ mbps}$



b)

For same size of cells and same power transmitted from Base station

We know, fig-1

$$BC^2 = AB^2 + AC^2 - 2 \cdot AB \cdot AC \cdot \cos(120^\circ)$$

$$d^2 = R^2 + R^2 - 2 \cdot R \cdot R \cdot \left(-\frac{1}{2}\right)$$

$$d^2 = 3R^2$$

$$d = \sqrt{3} R$$

Now, fig-2

$$D = \sqrt{(i\sqrt{3}R)^2 + (j\sqrt{3}R)^2 - 2 \cdot (i\sqrt{3}R) \cdot (j\sqrt{3}R) \cdot \cos(120^\circ)}$$

$$= \sqrt{i^2 3R^2 + j^2 3R^2 - 2 \cdot i\sqrt{3}R \cdot j\sqrt{3}R \cdot \left(-\frac{1}{2}\right)}$$

$$= \sqrt{3R^2(i^2 + j + ij)}$$

$$= R \sqrt{3N}$$

$$\therefore D = R \sqrt{3N}$$

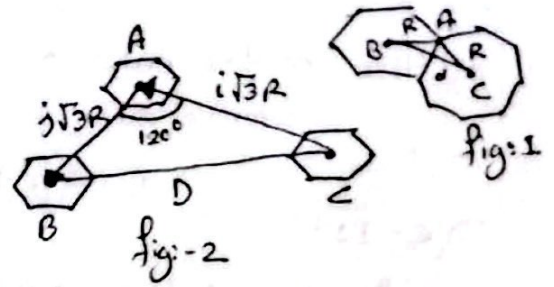
We know,

$$Q = \frac{D}{R} = \frac{R \sqrt{3N}}{R}$$

$$\therefore Q = \sqrt{3N}$$

$Q$  is directly proportional to  $\sqrt{N}$ . A smaller value of  $Q$  means a smaller value of  $N$ , means reuse will be more and the capacity will increase, which will also generate higher co-channel interference.

$$Q \downarrow \quad N \downarrow \quad \text{capacity} \uparrow \quad \text{CCI} \uparrow$$



$D$  = minimum distance between the centre of co-channel cells.

$R$  = Radius of the cell

$d$  = distance between centers of adjacent cells.

$N$  = number of cells, where  $N = i^2 + j + j^2$

$Q = \frac{D}{R}$  ; co-channel reuse ratio

2(b)

SNR	SIR
① Signal to Noise Ratio	① Signal to interference ratio
② Ratio of Signal power and background noise.	② Ratio of signal power and power of interfering signal.
③ Caused by thermal noise, environment or device noise	③ Caused by interference of nearby cells or overlapping frequencies.
④ Used in communication channel radio broadcasting.	④ in cellular network and wireless system.

SIR at center:

$$\begin{aligned}
 \text{SIR} &= \frac{\text{Signal Power}}{\text{Interference Power}} \\
 &= \frac{P_0 \left(\frac{R}{d_0}\right)^{-n}}{P_0 \left(\frac{D}{d_0}\right)^{-n}} \\
 &= \frac{R^n}{D^n} \left(\frac{d_0}{d_0}\right)^n \\
 &= \frac{(R/D)^{-n}}{6} ; 6 = i_0 \\
 &= \frac{(D/R)^n}{i_0} = \frac{(\sqrt{3}N)^n}{i_0}
 \end{aligned}$$

SIR at boundary:

$$\begin{aligned}
 \text{SIR} &= \frac{S}{I} = \frac{R^{-n}}{2(D-R)^{-n} + 2(D+R)^{-n} + 2(D)^{-n}} \\
 &= \frac{1}{2(Q-1)^{-n} + 2(Q+1)^{-n} + 2(Q)^{-n}}
 \end{aligned}$$



### c) Without Sectoring

We know,

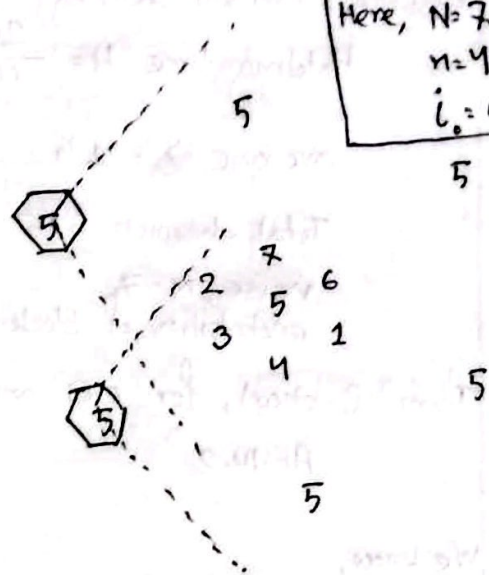
$$SIR = \frac{(\sqrt{3}N)^n}{i_0} = \frac{(\sqrt{3 \times 7})^4}{6}$$

$$= 73.5$$

$$= 10 \log(73.5)$$

$$= 18.66 \text{ dB}$$

Here,  $N=7$   
 $n=4$   
 $i_0=6$  (hexa)



### With sectoring

$$SIR = \frac{(\sqrt{3}N)^n}{2} = \frac{(\sqrt{3 \times 7})^4}{2}$$

$$= 220.5$$

$$= 10 \log(220.5)$$

$$= 23.41 \text{ dB}$$

For  $120^\circ$ ;

- 3 sectors.
- number of affected clusters  $= 2 = i_0$

$\therefore$  SIR increases with sectoring.

For  $120^\circ$  sectoring 3 antennas are used, as SIR is increased, other co-channel cannot affect their signal.

$\therefore$  CCI is low.

Our accepted SIR value is  $18.66 \text{ dB}$ , so, with sectoring we need to decrease the  $N$  to achieve the SIR value.

For  $N=4$  ( $i=2, j=0$ )

$$SIR = \frac{(\sqrt{3 \times 4})^4}{2} = 72 = 18.57 \text{ dB}$$

So,  $N \downarrow$

$\therefore$  capacity increases.

$\therefore$   $\Phi$  or reuse ratio decreases

Assume, (without sectoring)

$$\text{Holding time, } H = \frac{2 \text{ min}}{60} = \frac{1}{30} \text{ hour}$$

$$\text{average, } \lambda = 1 \text{ h}$$

$$\text{Total channel} = 395$$

$$\therefore \text{channel per cell} = \frac{395}{7} \approx 57$$

$$\text{reuse, } N = 7$$

$$\text{probability of blocking} = 0.01$$

From B-chart, for 0.01 and 57;

$$A = 44.2$$

We know,

$$A = U A_u$$

$$U = \frac{A}{A_u} = \frac{44.2}{0.03333}$$

$$= 1326$$

$$\text{Here, } A_u = \lambda H$$

$$= 1 \times \frac{1}{30}$$

$$= 0.03333$$

With sectoring

For  $120^\circ$  sector;

3 sectors.

$$\therefore \text{number of channel per sector} = \frac{57}{3} = 19$$

For B-chart for 0.01 and 19;

$$A = 11.2$$

$$\therefore U = \frac{11.2}{0.03333}$$

$$= 336$$

$$\therefore \text{for 3 sectors} = (336 \times 3) = 1008$$

$$\text{Efficiency} = \left( \frac{1326 - 1008}{1326} \right) \times 100 = 24\%$$

$\therefore$  sectoring decreases trunking efficiency.

$A_u$  = Traffic intensity per user  
 $U$  = Total no. of user supported per cell  
 $A$  = Traffic intensity per cell



## 2(c) Microcell zone concept:

- ① A cell is conceptually divided into microcells.
- ② Directional Antenna placed on cell edge, radiating power inward.



- ③ Central Base station connects to all zones, assigns channels as needed.
- ④ As Base station has all channels information, seamless zone transition with no handoff, simply switches channel to the next zone.

Benefits: ① Improve coverage, fewer call drops, higher capacity in dense areas.

Without microzone

$$SIR = \frac{(\sqrt{3N})^n}{i_0} \quad \begin{array}{l} n=4 \\ N=7 \\ i_0=6 \end{array}$$

$$= 18.66 \text{ dB}$$

With (3 zone)

$$SIR = \frac{(\sqrt{3N})^n}{i_0} = \frac{(\sqrt{3 \times 3})^4}{1} \quad \begin{array}{l} n=4 \\ N=3 \\ i_0=1 \end{array}$$

$$= 20 \text{ dB}$$

$i_0=1$ ; there will be at least one interferer.

So,  $N \downarrow$   $SIR \uparrow$   $CCI \uparrow$  capacity  $\uparrow$