

Nested loops where each nested loop begins at the current value of the enclosing loop's loop index:

```

int x = 0;
for (int a = 0; a < n; a++)
{
    x += a;
    for (int b = a; b < n; b++)
    {
        x += b;
        for (int c = b; c < n; c++)
        {
            x += c;
            for (int d = c; d < n; d++)
            {
                x += d
            }
        }
    }
}

```

$O(1)$

int a = 0: $O(1)$
 $a < n$: $O(N + 1)$
 $a++$: $O(N)$
jump to loop start: $O(N)$

$O(N)$

int b = a: $O(N)$
 $b < n$: $O(N(N+1)/2 + N)$
 $b++$: $O(N(N+1)/2)$
jump to loop start: $O(N(N+1)/2)$

$O(N(N+1)/2)$

int c = b: $O(N(N+1)/2)$
 $c < n$: $O(N(N+1)(N+2)/6) + N(N+1)/2$
 $c++$: $O(N(N+1)(N+2)/6)$
jump to loop start: $O(N(N+1)(N+2)/6)$

$O(N(N+1)(N+2)/6)$

int d = c: $O(N(N+1)(N+2)/6)$
 $d < n$: $O(N(N+1)(N+2)(N+3)/24 + N(N+1)(N+2)/6)$
 $d++$: $O(N(N+1)(N+2)(N+3)/24)$
jump to loop start:
 $O(N(N+1)(N+2)(N+3)/24)$

$O(N(N+1)(N+2)(N+3)/24)$

An example of the above loops where each loop begins at 0 and iterates to $N - 1$ is shown on the next page.

Nested loops when each nested loop begins at 0 and iterates from 0 to N - 1:

```
int x = 0;                                O(1)
for (int a = 0; a < n; a++)                int a = 0:  O(1);
                                                a < n:    O(N + 1);
                                                a++:     O(N)
                                                jump to loop start:   O(N)
{
    x += a;
    for (int b = 0; b < n; b++)            O(N)
                                                int b = a:  O(N);
                                                b < n:    O(N2 + N);
                                                b++:     O(N2)
                                                jump to loop start:   O(N2)
{
    x += b;
    for (int c = 0; c < n; c++)            O(N2)
                                                int c = b:  O(N2);
                                                c < n:    O(N3 + N2);
                                                c++:     O(N3)
                                                jump to loop start:   O(N3)
{
    x += c;
    for (int d = 0; d < n; d++)            O(N3)
                                                int d = c:  O(N3)
                                                d < n:    O(N4) + O(N3)
                                                d++:     O(N4)
                                                jump to loop start:   O(N4)
{
    x += d
}
}
}
```