

隨堂作業

長期成本

已知信力公司的生產函數為 $Q = 10L^{0.5}K^{0.5}$ ，且 $w = r = 10$

(A) 等成本線方程式

$$\begin{aligned} \bar{C} &= wL + rK \\ &= 10L + 10K \end{aligned}$$

(B) 邊際技術替代率

$$\begin{aligned} |MRTS| &= \frac{MP_L}{MP_K} \\ &= \frac{5L^{-0.5}K^{0.5}}{5L^{0.5}K^{-0.5}} = \frac{K}{L} \\ MP_K &= 5L^{0.5}K^{-0.5} \\ MP_L &= 5L^{-0.5}K^{0.5} \end{aligned}$$

(C) 等產量線會凸向原點嗎?

$$\begin{aligned} |MRTS| &= \frac{K}{L} \\ L \uparrow, K \downarrow, |MRTS| \downarrow \\ \frac{d|MRTS|}{dL} &= -KL^{-2} < 0 \end{aligned}$$

所以等產量線凸向原點。

(D) 條件要素需求函數

$$\begin{cases} \bar{Q} = f(K, L) & \text{--- ①} \\ \frac{MP_L}{w} = \frac{MP_K}{r} & \text{--- ②} \end{cases}$$

$$\begin{cases} Q = 10L^{0.5}K^{0.5} \\ \frac{MP_L}{w} = \frac{MP_K}{r} \end{cases}$$

$$\begin{cases} Q = 10L^{0.5}K^{0.5} \\ \frac{5L^{-0.5}K^{0.5}}{10} = \frac{5L^{0.5}K^{-0.5}}{10} \end{cases}$$

$$\frac{L^{0.5}}{K^{0.5}} = \frac{K^{0.5}}{L^{0.5}}$$

$$L^{0.5} \times L^{0.5} = K^{0.5} \times K^{0.5}$$

$$L^* = K^*$$

$$Q = 10L^{*0.5}L^{*0.5}$$

$$Q = 10L^*$$

$$L^* = 0.1Q$$

$$L^* = K^* = 0.1Q$$

(E) 總成本、平均成本、邊際成本函數

$$L^* = K^* = 0.1Q$$

$$\begin{aligned} TC &= 10 \times 0.1Q + 10 \times 0.1Q \\ &= 2Q \end{aligned}$$

$$AC = \frac{TC}{Q} = \frac{2Q}{Q} = 2$$

$$MC = \frac{dTC}{dQ} = 2$$

(F) 生產 10 單位時的最低成本為?

$$TC = 2 \times 10 = 20$$