



# Deliver Time Optimization Project

By:

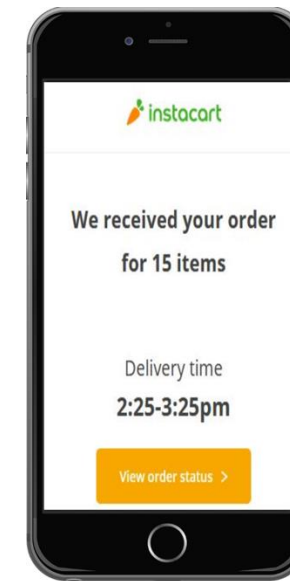
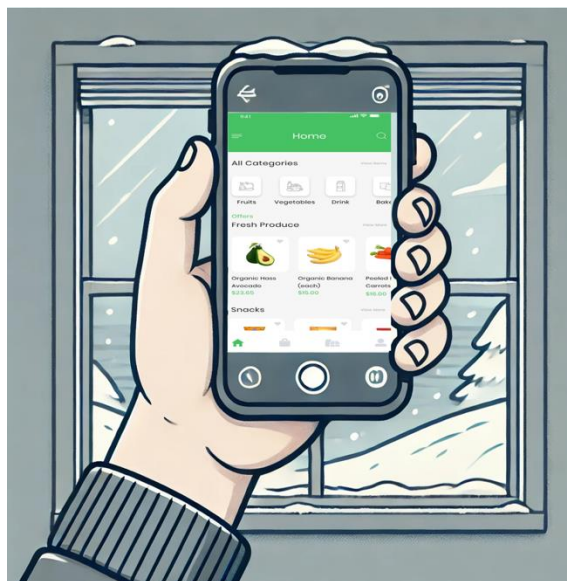
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What is  **instacart**?





# What is instacart?



## Instacart: Groceries & Food 12+

Shop Grocery Delivery Services

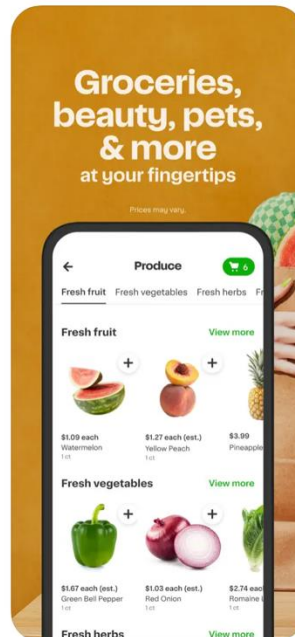
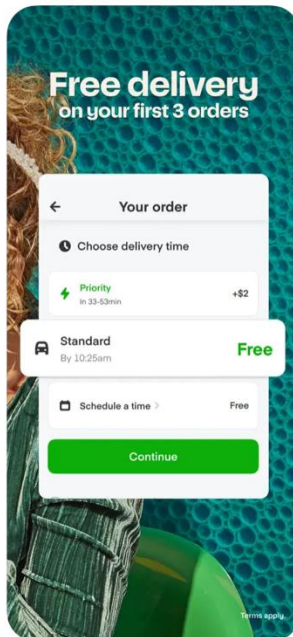
Maplebear Inc

#11 in Food & Drink

★★★★★ 4.8 • 3.8M Ratings

Free

Screenshots [iPhone](#) [iPad](#)



- A **four-sided marketplace** connecting customers, shoppers, drivers, and retail stores
- Fast-growing grocery delivery platform enabling **30-minute delivery**
- Complex coordination between **multiple stakeholders**

How Does



Work?



How Does



Work?



Shop Owner



Partnership  
Contract

Listing Groceries  
On Site / App

Sell

Advertise



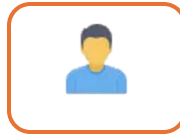
How Does



Work?



Customer



Sign Up

Browse Goods

Add to Cart

Fill out Details &  
Make Payment

Receive Goods

Shop Owner



Partnership  
Contract

Listing Groceries  
On Site / App

Sell

Advertise



How Does



Work?



Shopper/Driver



Register & Create a Profile

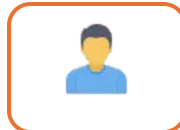
Receive Orders Via Notifications

Shop Goods

Deliver Goods

Get Paid

Customer



Sign Up

Browse Goods

Add to Cart

Fill out Details & Make Payment

Receive Goods

Shop Owner



Partnership Contract

Listing Groceries On Site / App

Sell

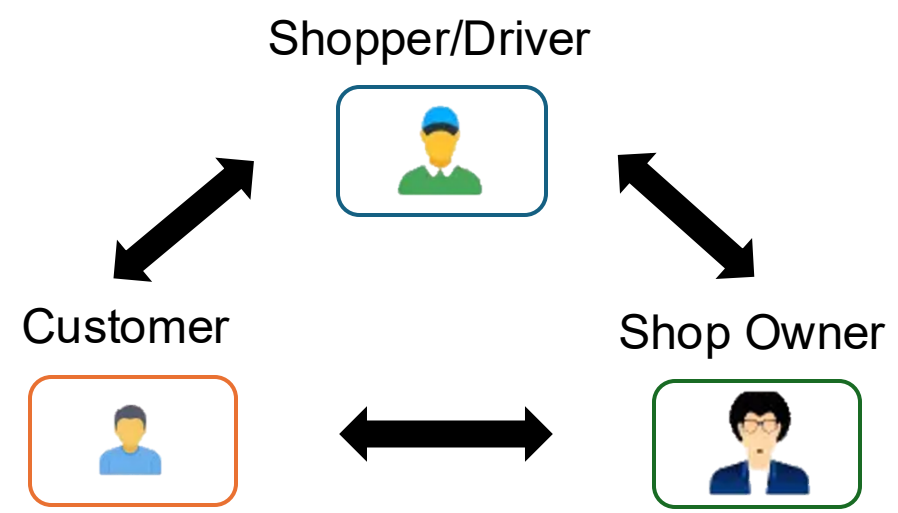
Advertise



How Does

 instacart

Work?



# Why use 🥕 instacart?

- **Higher order values** than food delivery
- **Complex inventory management** (fresh/frozen items)
- Greater **batching potential**



# Why 🥕 instacart in Montreal?

- Complex road network (**one-way streets**)
- Frequent **construction zones**
- **Diverse** neighborhood densities
- **Extreme** seasonal weather
- **High reliance** on public transportation





Apoorva Mehta

Optimization???



Apoorva Mehta





Apoorva Mehta

Optimization???

- Shopper assignment to orders
- Minimizing in-store shopping time
- Batching multiple orders
- Determining the most efficient delivery routes

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Apoorva Mehta

Optimization???

- Shopper assignment to orders
- Determining the most efficient delivery routes



Optimization???

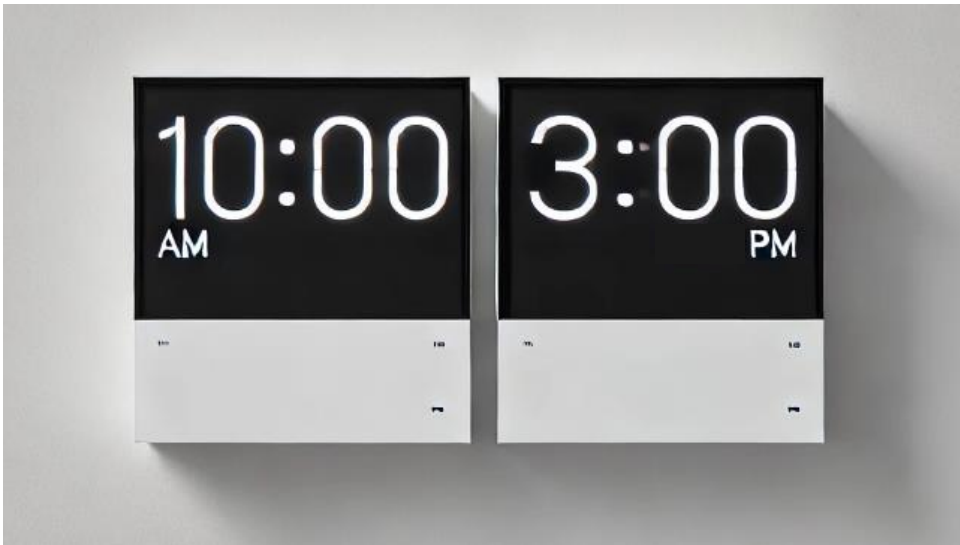
- Shopper assignment to orders
- Determining the most efficient delivery routes

Apoorva Mehta



## Why Dollarama?

- Well-distributed network across Montreal
- Represents residential, commercial, mix-used, and suburban areas.



## Focus on Peak Hours

- Focused on peak hours: 10:00 AM - 3:00 PM
- Simulates busiest period for realistic demand.
- Enables effective modeling of shopper assignments and delivery routes.



# Formulating the Optimization Problem

1

## Pickup Stage

Assign shoppers to pick up orders from Dollarama stores.

2

## Delivery Stage

Determine efficient routes for delivering orders to customers.





# Project Objective

Minimize Average Delivery Time

Develop an optimization model for peak hour deliveries.

# Key Assumptions



## Proximity

Dollarama branches serve nearby customer locations.



## Pre-packaged

Orders are ready for pickup at Dollarama stores.



## Delivery Capacity

Shoppers can deliver up to two orders per trip.





# Pickup Stage Optimization

## Pickup Assignment Rules

### Two Order Rule

2 orders  
within 10  
minutes



assign the  
nearest shopper

### One Order Rule

1 order and no  
additional order  
arrives within 10  
minutes



assign the nearest  
shopper



# Delivery Stage Optimization

## Four Areas in Montreal

- City is divided into residential, commercial, mixed-use, and suburban zones.
- Each zone accounts for different traffic and geographic challenges

## Real-World Traffic Constraints

- High-traffic zones
- Construction sites
- One-way streets

## Optimized Delivery Sequence

The sequence of deliveries is optimized by serving the nearest customer first while considering proximity and travel conditions.



# Mathematical Model: Variables and Parameters

Notation	Category	Description
$S$	Set	Set of supplier locations (possible pickup points).
$D$	Set	Set of demand locations (possible customer locations).
$I$	Set	Set of driver initial locations.
$\Delta_S$	Set	Set of pickup locations (only 1 element contained)
$\Delta_D$	Set	Set of delivery locations (up to 2 element contained)
$T_{ij}$	Parameter	Travel time between locations $i$ and $j$ , where $i, j \in S \cup D$ .
$x_{ij}$	Decision Variable	Binary variable: 1 if driver $k$ travels from $i$ to $j$ , 0 otherwise.

# Pickup Stage: Objective Function and Constraints

$$\min_{\{x_{ij}\}} \sum_j \sum_i T_{ij} \cdot x_{ij}$$

s.t.

$$\sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} \geq 0 \quad \forall i \in I$$

$$\sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} \leq 1 \quad \forall i \in I$$

$$\sum_{i \in I} \left( \sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} \right) = 1$$

To make sure there's exactly one source node  
(one driver take the order)

$$\sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} = 0 \quad \forall i \in N \setminus \{I \cup \Delta_s\}$$

Intermediate Node

$$\sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} = -1 \quad i = m \in \Delta_s$$

Terminal Node

# Delivery Stage: Objective Function and Constraints

$$\min_{\{x_{ij}\}} \sum_j \sum_i T_{ij} \cdot x_{ij}$$

s.t.

$$\sum_{j \in N} x_{ij} - \sum_{j \in N} x_{ji} = \begin{cases} 1 & i = m \\ -1 & i = n \\ 0 & \text{o. w.} \end{cases}$$

Source Node  
Terminal Node  
Intermediate Node

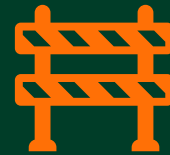
For any route starting from  $m$  and ending at  $n$ , the shortest path is found by solving the above optimization problem. We represent this shortest path as  $u(m, n)$ . Assuming  $\Delta_S = \{a\}$ ,  $\Delta_D = \{b, c\}$ , in order to find the shortest path starting from  $a \in \Delta_S$ , dropping by one of the element of  $\Delta_D$ , and ending at the other, we need to compare  $u(a, b) + u(b, c)$  and  $u(a, c) + u(c, b)$ .

# Data Simulation

## Location

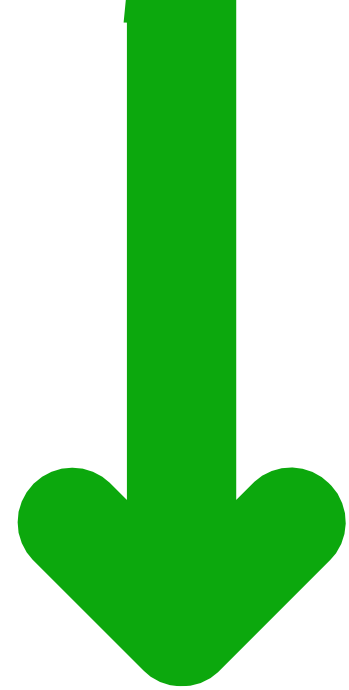


## Time



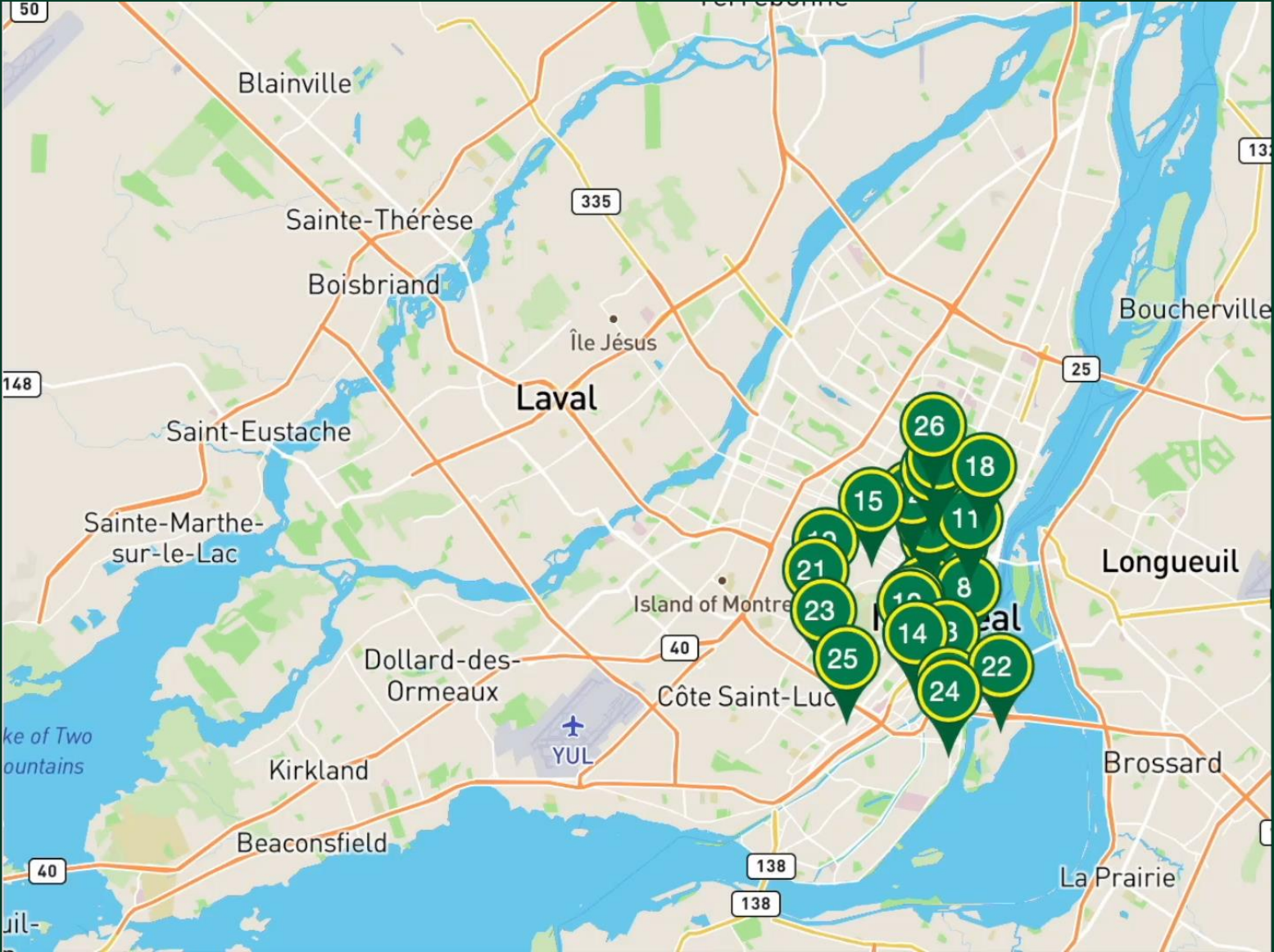


# Location Setup

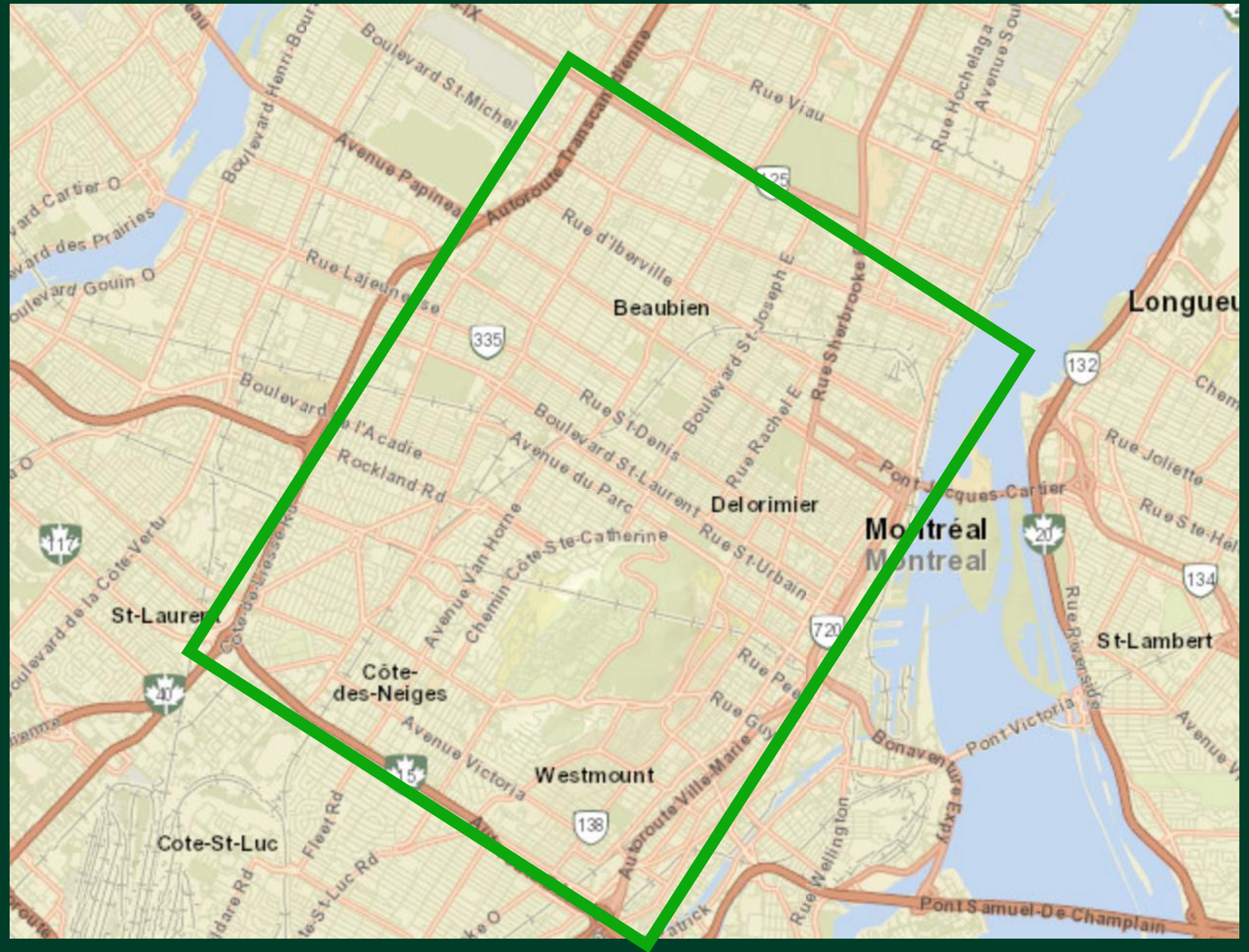




# Dollarama Stores







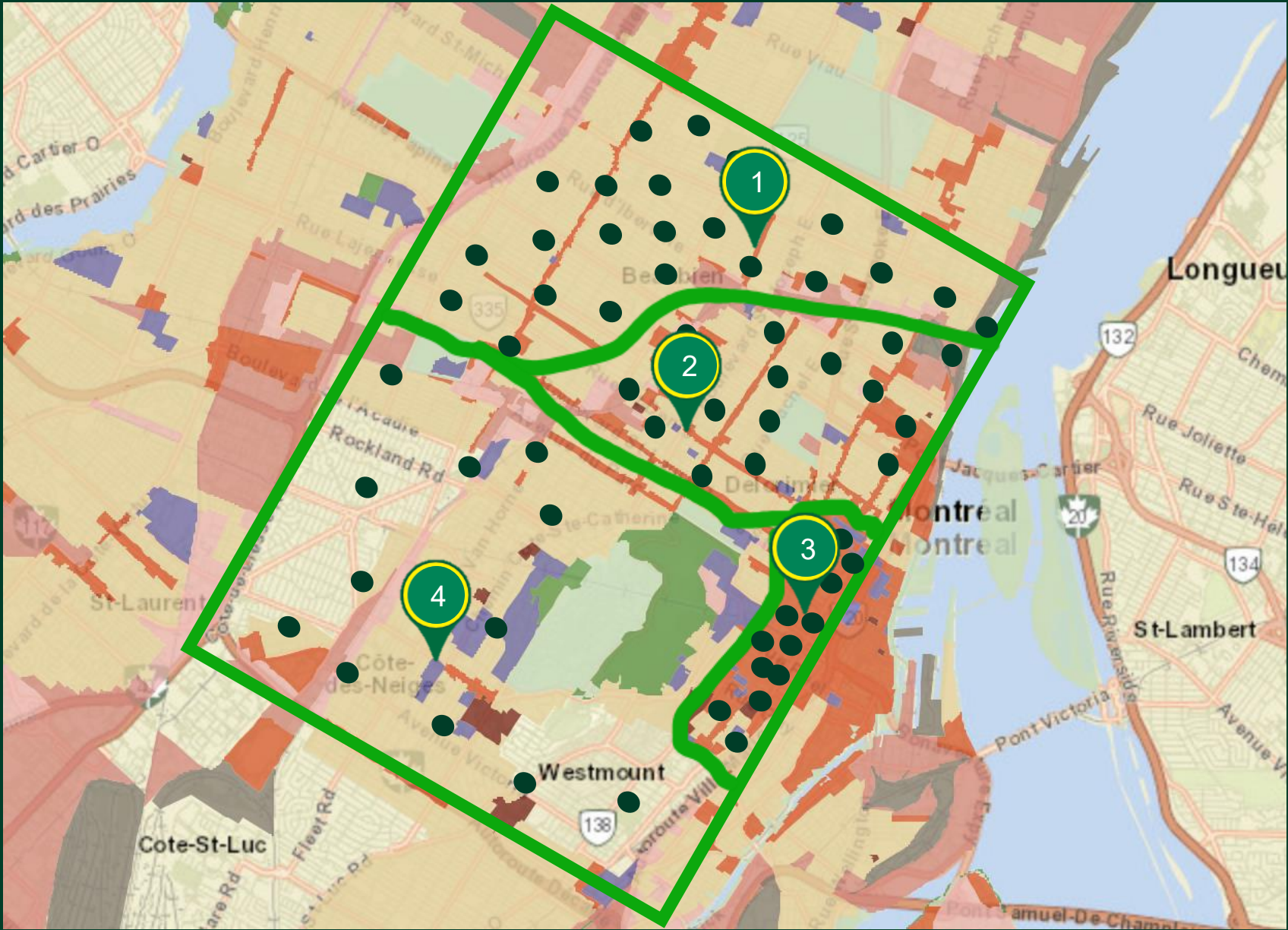


Residential

Mixed-use

Commercial

Suburbs



# Schema Summary

Land uses	Percentage of Demand Points	Demand Sites ( <i>D</i> )	Dollarama Stores ( <i>S</i> )
Residential	45%	D1~D16	S1
Commercial	25%	D17~D26	S2
<u>Mixed-used</u>	20%	D27~D33	S3
Suburbs	10%	D34~D36	S4



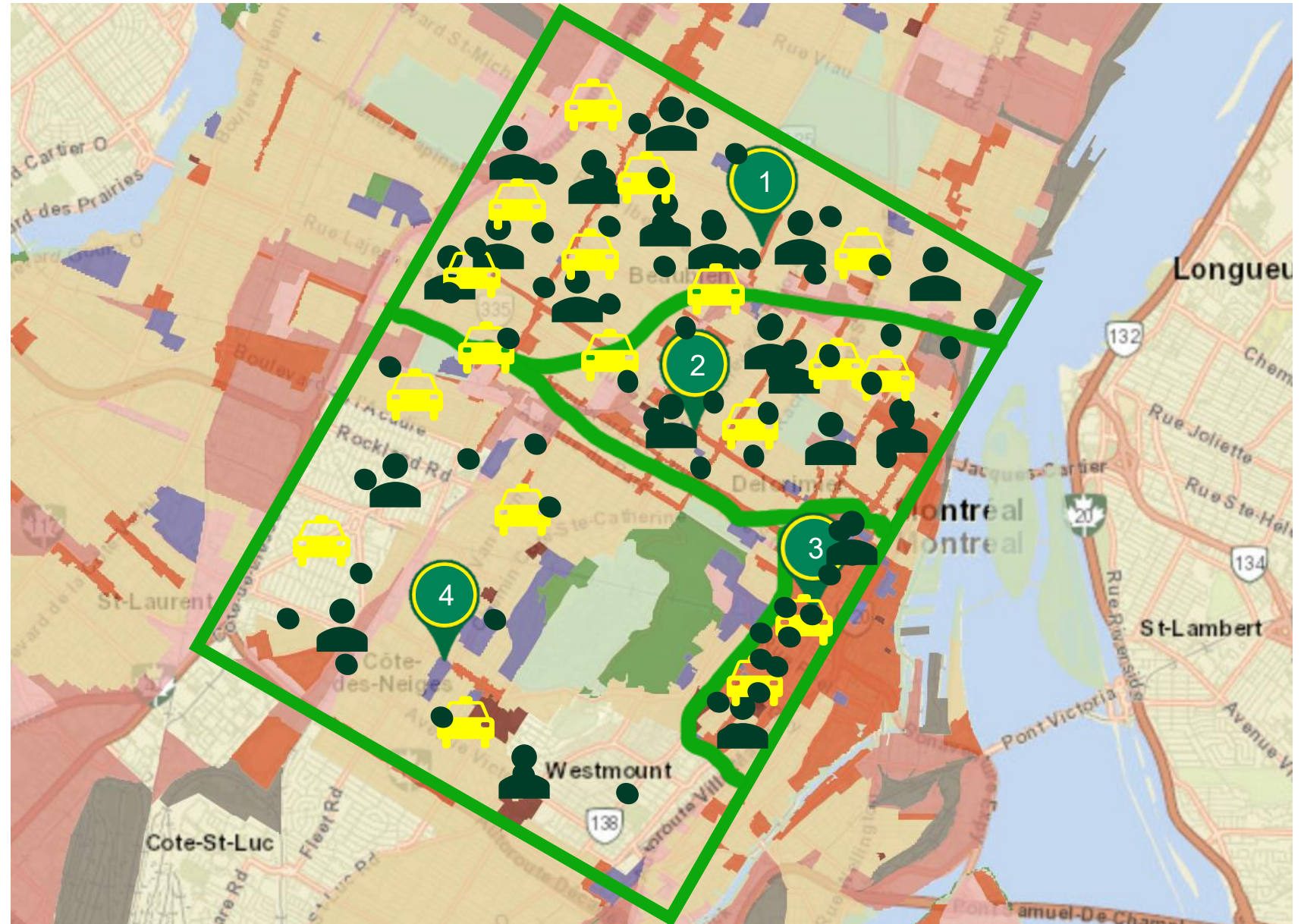
# Initial Points for Drivers and Source Locations for Orders

Residential

Mixed-use

Commercial

Suburbs

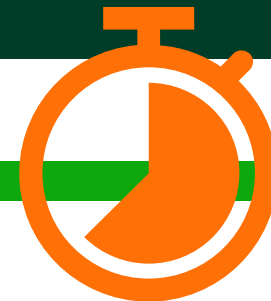




# Order Log

Order Number	Timestamp	S	D
1	10:03:11	S2	D20
2	10:05:42	S2	D25
3	10:07:59	S3	D30
4	10:11:33	S2	D17
5	10:18:42	S2	D19
6	10:24:19	S1	D6
7	10:27:03	S1	D6
8	10:34:28	S2	D19
9	10:37:39	S1	D4
10	10:41:09	S1	D8
11	10:45:00	S3	D31
12	10:46:59	S1	D14
13	10:49:42	S4	D36
14	10:51:27	S2	D18

# Time Cost Setup





# Driving Time Matrix (T\_ij base)

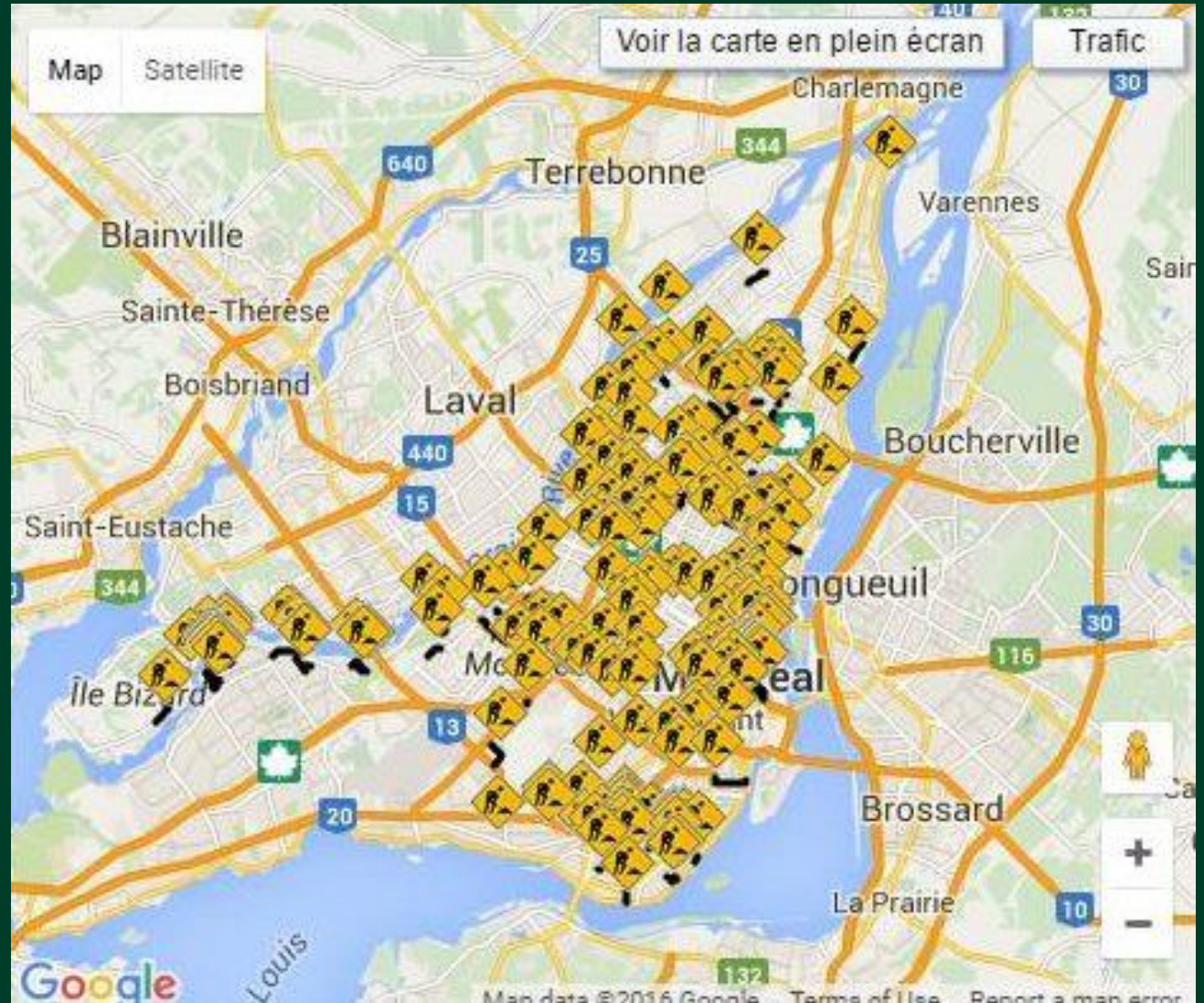
(Minutes)	S1	S2	S3	S4	D8	D14	D15	D19	D2
S1	0	18.9	13.25	23.0166667	26.0333333	3.61666667	7.03333333	21.0666667	
S2	18.9	0	7.71666667	15.8333333	19.0833333	18.5	22.9333333	9.55	
S3	13.25	7.71666667	0	20.7166667	23.7166667	15.3666667	19.6166667	9.51666667	
S4	23.0166667	15.8666667	20.7166667		4.6	22.8666667	25.3333333	12.1666667	
D1	6.16666667	16.5333333	12.25		27.8	7.9	12.0666667	18.4166667	
D2	8.43333333	11	8.61666667		1000023.6	8.21666667	12.3833333	16.65	
D3	11.0666667	10.2666667	5.95		24.1666667	11.1333333	15.1833333	15.3166667	
D4	22.1333333	16.1	19.8166667		5.75	22.7666667	1000025.23	12.0833333	
D5	26.0333333	19.0833333	23.7166667		0	26	28.4666667	15.7333333	
D6	3.61666667	18.5	15.3666667		26	0	6.15	20.3	
D7	7.03333333	22.9333333	19.6166667		4.6666667	6.15	0	23.1666667	
D8	21.0666667	9.55	9.51666667		7.3333333	20.3	23.1666667	0	
D9	21.9166667	11.0166667	9.86666667		4.3333333	21.5833333	24.4333333	4.76666667	
D10	20.95	16.8833333	15.3		20.05	20.1	22.0166667	10.6333333	
D11	19.4833333	24.2333333	23.5833333		6.3333333	19.0166667	16.6333333	21.5	
D12	21.8833333	26.6666667	26.0166667		10.0666667	1000021.43	10019.05	23.9166667	
D13	18.7833333	23.55	22.9		22.95	18.3333333	15.95	20.8166667	
D14	19.2333333	23.8833333	23.35		13.2833333	18.7833333	16.4	21.1333333	
D15	18.4166667	20.4166667	21.6666667		26.7166667	17.6666667	20.5	20.5	
D16	14.75	17.65	18.9		23.95	14.9166667	17.2833333	17.7333333	
D17	15.1	7.78333333	8.51666667		16.2666667	14.35	17.1833333	10.0333333	
D18	15.25	7.4	12.65		14.7333333	14.5	17.3166667	12.8833333	
D19	16	2.48333333	6.4		18.8666667	15.25	18.0833333	7.88333333	
D20	17.25	7.25	5.21666667		22.8666667	17.0333333	10.8666667	0.18333333	

Azure Maps

# Construction

Road Closure

Passable but slow





# One-Way street





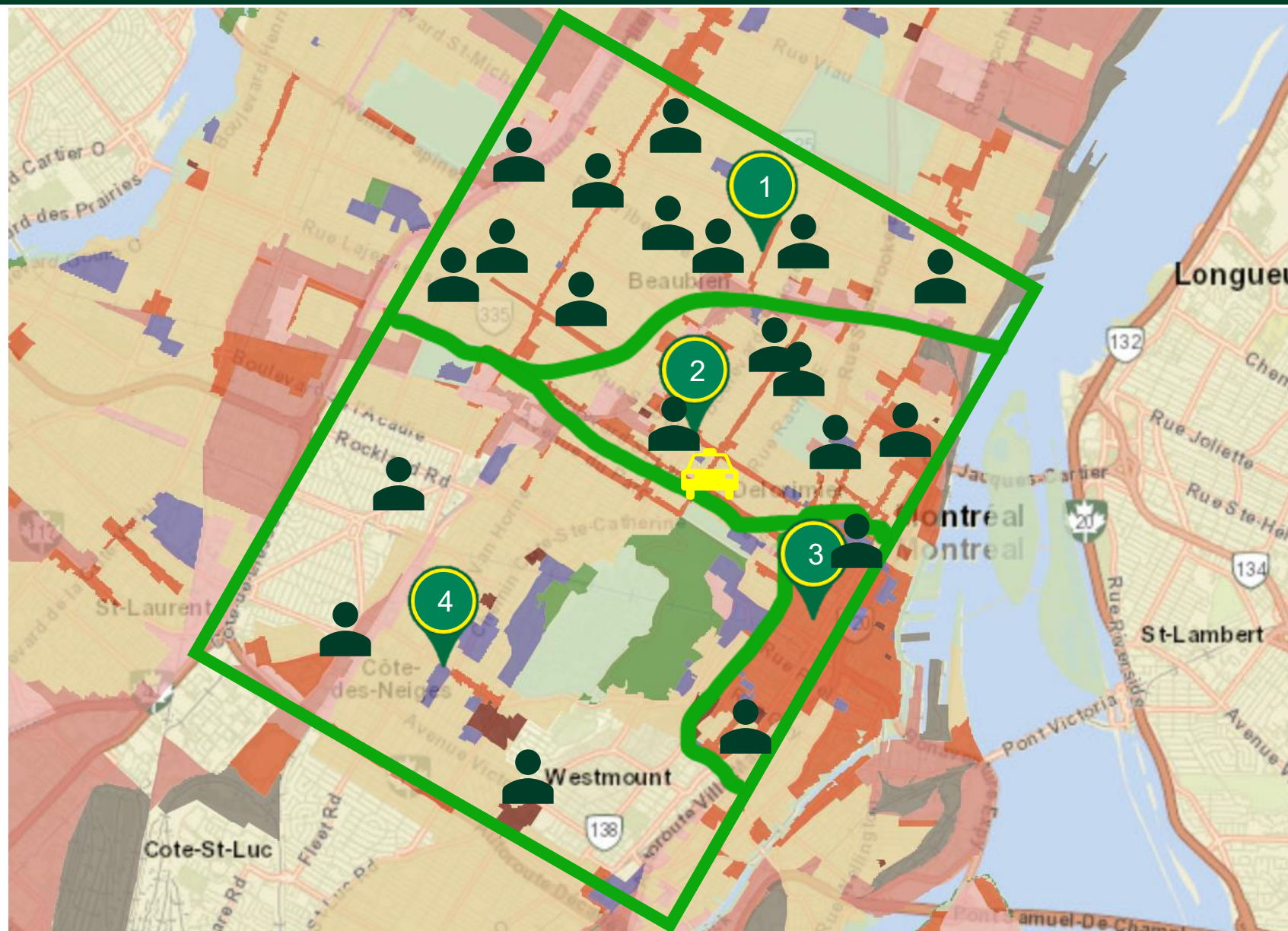
# Distance Weighting

Residential

Mixed-use

Commercial

Suburbs



# Weighting Schema

	Residential	Commercial	<u>Mixed-used</u>	Suburbs
Residential	Rand (0.05, 0.15)	0.15	0.1	0.05
Commercial	0.15	Rand (0.15, 0.25)	0.15	0.1
<u>Mixed-used</u>	0.1	0.15	Rand (0.1, 0.2)	0.05
Suburbs	0.05	0.1	0.05	0

# Time Penalties

**A=1 if Road closure**

$$T_{ij} = T_{ij}^{\text{base}} + MA_{ij}$$

**B=1 if Passable but slow**

$$T_{ij} = T_{ij}^{\text{base}} + MB_{ij}$$

**C=1 if One-Way street**

$$T_{ij} = T_{ij}^{\text{base}} + MC_{ij}$$

**Density Penalty**

$$T_{ij} = T_{ij}^{\text{base}} \times (1 + \beta_{ij} \text{ density penalty})$$

## Total Time Cost

$$T_{ij} = T_{ij}^{\text{base}} \times (1 + \beta_{ij} \text{ density penalty}) + MA_{ij} + MB_{ij} + MC_{ij}$$

# Preliminary Result

```
initial_points = ['D1', 'D2', 'D3']
delta_s = ['S19']
delta_d = ['D26', 'D88']
source_node = delta_s[0]

result_p = optimize_shortest_path(tij_matrix, initial_points, delta_s)
result_d = compare_routes(tij_matrix, source_node, delta_d)

# Results
print(f"Shortest Pickup Path: {result_p['path']}")
print(f"Pickup Travel Time: {result_p['total_time']} minutes")
print(f"\nShortest Delivery Path: {result_d['shortest_path']}")
print(f"Delivery Travel Time: {result_d['total_time']} minutes")
print(f"Delivery Route Description: {result_d['route_description']}")
total_travel_time = result_p['total_time'] + result_d['total_time']
print(f"\nTotal Travel Time: {total_travel_time} minutes")
```

✓ 0.5s

Shortest Pickup Path: [('D3', 'S19')]

Pickup Travel Time: 5.95 minutes

Shortest Delivery Path: ['S19', 'D75', 'D25', 'D26', 'D25', 'D88']

Delivery Travel Time: 49.116666699999996 minutes

Delivery Route Description: u(S19, D26) + u(D26, D88)

Total Travel Time: 55.0666667 minutes

Initial Point Chosen: D3

Pickup Path:

D3->S19

Pickup Time = 5.95 min

Delivery Path:

S19->D75->D25->D26->D25->D88

Delivery Time = 49.12 min

Total Time = 55.07 min



# Time Window Integration

## Why Time Windows?

- Instacart customers often specify preferred delivery intervals.
- Balances operational efficiency with customer-specific delivery preferences.

## The New Constraint

- In the Delivery Stage, a time window metric measures the gap between order placement and the desired delivery time.
- Delivery routes prioritize orders nearing time window limits.

## Key Benefits

- Improved customer satisfaction encourages loyalty and increases the likelihood of future orders.
- Better alignment with real-world operational settings.



# Multi-Supplier & Multi-Store Integration

## Why Multi-Supplier & Multi-Store?

- Real-world orders often span multiple suppliers (e.g., Provigo, IGA).
- Shared demand points between suppliers fulfill diverse customer needs.
- Enhances service flexibility and adapts to customer expectations.

## New Model Features

- Many to many relationships: Demand points linked with multiple suppliers and shoppers.
- Flexible Shopper Routes: Shoppers can visit multiple suppliers in a single trip, allowing high-priority deliveries to be completed without waiting for all pickups to be finished.

## Key Benefits

- Adapts to Montreal's diverse supplier landscape and customer requirements.



# Conclusion: Driving Sustainability Through Optimization

## For Customers

Faster and more reliable access to groceries, improving convenience and satisfaction.

## For Drivers

Increased earnings with more deliveries and reduced frustration from optimized routes.

## For Instacart

Enhanced efficiency, stronger customer loyalty, and sustainable business growth.

## For Environment

Reduced energy use and emissions, promoting eco-friendly delivery practices.

