# Final Report: Election Prediction

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## Introduction

The United States is getting closer to the 2020 presidential and Congressional elections on November 3, 2020. All 435 seats in the United States House of Representatives, 35 of the 100 seats in the United States Senate, and the office of President of the United States are up for election (Wikipedia, 2020). With the current polarizing political landscape, the election outcomes are significant to determine the next stage of this country. Polarization also makes election prediction both less and more difficult. It is less difficult because election results are less subject to election or candidate-specific factors, and it is more difficult as elections become increasingly close and fierce competitions, especially for presidential elections (Gelman, 2020). Therefore, we believe 2020 is a particularly challenging yet interesting year for statisticians to predict election outcomes and compare results with other predictions and the actual outcome to reflect on methodologies and unaccounted predictors. These election predictions not only inform the public about campaign trends and political sentiments but also help political strategists make decisions on allocating campaign resources for different candidates (Linzer et al.). American political pundits have been spending countless hours obtaining and analyzing relevant data to predict the election outcomes, and historical models and predictions and pre-election polls are two of the most important sources of information (Linzer et al.). In this report, similarly, we will also be using both literature review and polls for 2020 to build our prediction models.

We plan to build prediction models for the 2020 U.S. presidential election and the Senate election nationwide. Also, among all states, we decide to further predict the U.S. House election outcome for North Carolina, as it has been a swing state in presidential and Congressional elections for decades. Since 1996, the Republican statewide vote share in Congressional elections has varied "from a low of 45% in 2008 to a high of 55% in 2014" (Perrin et al.). To summarize, this report aims to use statistical models to predict (1) the outcome of the presidential election, (2) whether the US Senate remains in Republican control, (3) the electoral college vote, (4) the outcomes of all NC Congressional elections (the 13 federal Representatives to Congress), and (5) the outcome of the NC Senate election, including characterization of uncertainty in predictions.

## **Data Description**

In literature, election prediction relies on polling data as well as the fundamentals, which are economic indicators (The Economist, 2020) and voter turnout by demographic groups (Hansford, et al.). To forecast the outcomes of presidential election, senate election and house election (for North Carolina only), we obtained 2020 presidential polling data from *The Economist*, 2020 senate and house polling data as well as partisan lean data from *FiveThirtyEight*.

The fundamentals data were retrieved from various online sources, including Andrew Gelman's presidential election prediction model Github repository (for correlation across states and historical incumbent party's June approval ratings), Federal Reserve Economic Data (for second quarter real income growth), and NC Board of Elections website (for 2020 NC registered voter demographics). Please refer to Appendix B for a detailed description of all data sets used.

# Data Processing and Missing Data

For both the President and Senate models, we had to choose which states we considered to be "battlegrounds" to include in the models. We chose states for the models separately, since some states have a competitive race for President but not for Senate or vice versa.

For the presidential election data, we choose to use polling data from 30 days before the election (as opposed to over 30 days), as this aligns with Andrew Gelman's observation that polling data becomes more predictive as the day of poll becomes closer to election day (The Economist). Note that state-wide polls 30 days or less are unavailable for Oregon, Idaho, Wyoming, Nebraska, North Dakota, Illinois, Tennessee, Arkansas, Mississippi, and many Northeastern states. But these states are not swing states in recent elections, so we did not include those in our modeling process. For modeling, we will filter out those states with obvious party preferences and focus on those states showing percentages swinging right above or below 50%. For the presidential model, the states chosen are Arizona, Florida, Georgia, Iowa, Michigan, Minnesota, Nevada, New Hampshire, North Carolina, Ohio, Pennsylvania, Texas, and Wisconsin. These thirteen states are swing states in the plot, and are rated as either "Toss Up", "Lean Republican", or "Lean Democrat" races (the three most competitive categories) by the Cook Political Report (CITE), an nonpartisan elections newsletter, as of October 28. These states are also projected to be competitive in the Presidential race by both the FiveThirtyEight and Economist models. We select poll responses from likely voters only, since it is known that using all responses may overestimate support for the Democratic party, according to FiveThirtyEight (Silver, 2014).

For the Senate model, the states chosen are Alabama, Alaska, Arizona, Colorado, Georgia, Iowa, Kansas, Maine, Michigan, Montana, North Carolina, South Carolina, and Texas. Similarly, for states such as California with strong historical party preferences, state-wide polls within 30 days of election are missing, but the missing data does not hurt our modeling process as we are only focusing on the swing states. There is also a special election for the Senate in Georgia in addition to the regularly scheduled election. These fourteen races are rated as either "Toss Up", "Lean Republican", or "Lean Democrat" (the three most competitive categories) by the Cook Political Report (CITE) as of October 29. These states are also projected to have competitive Senate races by both the FiveThirtyEight and Economist models.

For the U.S. House election, due to the scarcity of poll responses for the NC House elections, we included all poll responses within 115 days of the election. We will supplement the polls with the results from our interim report to predict the House election for NC.

Appendix B stuff

#### Presidential Election Model:

- 2020 US presidential election polls all\_polls.csv: 2020 U.S. Presidential Election Polls compiled by *The Economist*, publicly available at https://projects.economist.com/us-2020-forecast/president/how-this-works.
- partisan\_leans\_538.csv: effect of partisan lean on the Democratic candidate's presidential election vote share in each state. Available at https://github.com/fivethirtyeight/data/tree/master/partisan-lean.
- abramowitz\_data.csv: downloaded from Andrew Gelman's Github repository on 2020 Presidential Election. This data set contains information on each 1948-2016 election year's 2nd quarter GDP performance, incumbent party's June approval rating and incumbent party's vote share. Available at https://github.com/TheEconomist/us-potus-model.
- states\_cov\_matrix\_full.csv: covariance matrix of states which take into account similarity between states based on their demographic and political profiles. Retrieved from Andrew Gelman's Github repository on 2020 Presidential Election.
- abramowitz\_additional.csv: Supplemented abramowitz\_data.csv with the corresponding year's 2nd quarter real income growth, 3rd quarter real income growth (data from FRED https://fred.stlouisfed.org/series/A067RO1Q156NBEA) and S&P stock performance 3 months prior to the election (data from https://www.multpl.com/s-p-500-historical-prices/table/by-month).

#### **Senate Election Model:**

- senate\_polls.csv: this is from course website https://projects.fivethirtyeight.com/polls-page/senate\_polls.csv
- partisan\_leans\_538.csv: same as the data set in presidential election model
- We also incroporated incumbency advantage in the model, which as *FiveThirtyEight* suggests, is on average 2.6 for senate incumbents (https://fivethirtyeight.com/features/how-much-was-incumbency-worth-in-2018/).

# House Election Model (for North Carolina):

- house\_polls.csv: this is from course website https://projects.fivethirtyeight.com/polls-page/house\_polls.csv
- ncvoter\_1027\_small.rds: NC registered voter demographics information provided by the NC State Board of Elections (https://dl.ncsbe.gov/list.html).

# **Exploratory Data Analysis**

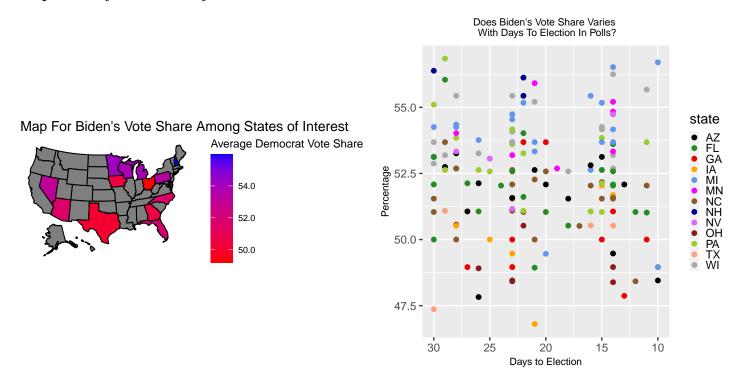


Figure 1: Presidential Election Data Visualization

After initial data cleanup for analysis, Figure 1 aims to explore polling data we have for the 2020 presidential election within 30 days of election, after filtering for the states of interest. The left plot shows that most states, as the polls indicate, have a vote share higher than 50% for Biden, averaging on all the polls available for each state respectively. While unsurprisingly Washington and California turn out to be blue, Louisiana, for example, still shows a deep red color. The right plot shows that within 30 days to election, variations exist for Biden support rate among polls within individual states. Combined with abundant literature that takes time into account for outcome prediction models, we will take days to election as a part of our model prediction as well (Gelman, 2020).

Similarly, Figure 2 visualizes the polling data we have for the 2020 U.S. Senate election, also within 30 days of election and after filtering for the states of interest. The left plot shows that most states, as the polls indicate, have a vote share higher than 50% for the Democratic Party, averaging on all the polls available for each state respectively. Nebraska is the only state with a bright red color in this data set. The right plot shows that within

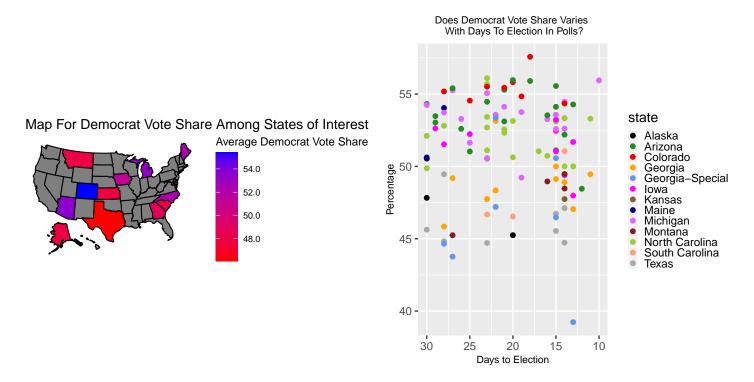


Figure 2: U.S. Senate Election Data Visualization

30 days to election, variations exist for the Democratic party vote share among polls within individual states, such as the trend seen for North Carolina as Democratic Party vote share decreases getting closer to the election. We will take days to election as a part of our model prediction as well.

Figure 3 shows the different Democratic Party vote shares predicted by our interim report for all congressional districts in North Carolina. After predicting for voter turnout in the interim report, we use the party registration for predicted voters to get the vote share for Democratic Party. First, we grouped predicted voters for congressional districts. There are three categories in party registration: Democratic, Republican, and other (indicating a third party or unaffiliated). Within each congressional district, we split the other population in half, and add it to both the Democratic Party vote count and the Republican Party vote count, as FiveThirtyEight used the same approach to get vote share for their House predictions, shown in[https://projects.fivethirtyeight.com/2020-election-forecast/house/]. Among 13 districts, 6 of them have a Democratic Party vote share higher than 50%.

#### Method

Similarly to prior work (Linzer 2013), we use a hierarchical model structure for our election models to overcome the limitation that not every state is polled on every day, allowing the model to borrow data across states (or Congressional districts). This also helps account for the fact that polls from each individual state are correlated data observations.

To specify priors for the mean of two-party vote share for Democrats in each state or district, we used a combination of state partisanship, economic fundamentals, candidate incumbency, and projected voter turnout based on demographics. First, we started with state or district partisan lean calculated by FiveThirtyEight (see "FiveThirtyEight's Partisan Lean" in references). Partisan lean is the average difference between how a state or district votes and how the country votes overall, based on results from the past two presidential elections as well as statewide elections in 2018. For example, North Carolina has a partisan lean of R+4, meaning that in a 50/50 political environment nationwide, a Republican would be expected to win North Carolina by 4 points. For each partisan lean, we turn the parsian lean into a prior mean of Democratic vote share by adding or subtracting half the partisan lean from 50%. North Carolina is a Republican-leaning state, so we subtract 2 from 50% to get a partisan lean prior of 48% (note that the Republican would then get 52% of the two-party vote, resulting in an

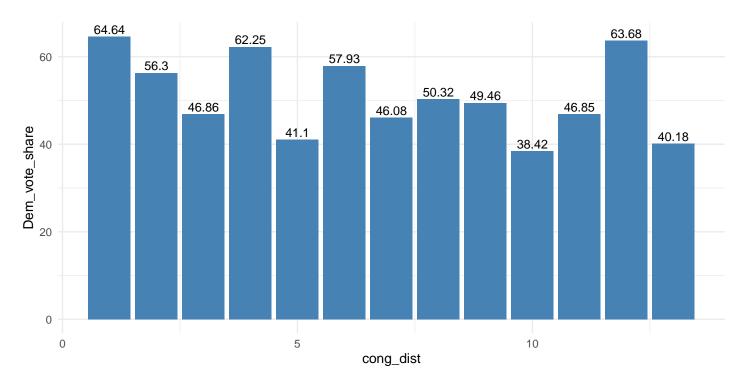


Figure 3: Democratic Vote Share Predicted By The Interim Report

R+4 margin of victory).

#### Presidential Election Model

For the presidential model, the states chosen are Arizona, Florida, Georgia, Iowa, Michigan, Minnesota, Nevada, New Hampshire, North Carolina, Ohio, Pennsylvania, Texas, and Wisconsin. These thirteen states are rated as either "Toss Up", "Lean Republican", or "Lean Democrat" races (the three most competitive categories) by the Cook Political Report (as of October 28), an nonpartisan elections newsletter. These states are also projected to be competitive in the Presidential race by both the FiveThirtyEight and Economist models. We select poll responses from likely voters only, since it is known that using all responses may overestimate support for the Democratic party, according to FiveThirtyEight (Silver, 2014). The response we will use is  $Y_k$ , Biden's share of the two-party vote using the following model where the poll k (of K=3361 [insert final number] polls) ended t days (of T=30 days) before the election and was conducted on state j (of J=13 states of interest). We choose to use polling data from 30 days before the election (as opposed to over 30 days), as this aligns with Andrew Gelman's observation that polling data becomes more predictive as the day of poll becomes closer to election day (The Economist).

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Gelman's observation that polling data becomes more predictive as the day of poll becomes closer to election day (The Economist).  Y_k \sim N(\theta_{jt}, \sigma_{yj}^2) \\ \theta_{\cdots t} \sim MVN(\theta_{\cdots t-1}, \Sigma) \\ \Sigma \sim Wishart(S, J+1) \text{ where } S \text{ is the state covariance matrix (obtained from Andrew Gelman's model) and } J \\ \text{is the number of states in the model.} \\ \text{Priors for } \sigma_{yj}^2 \colon \sigma_{yj}^2 \sim InvGamma(\nu_u, \nu_y \tau_y) \\ \nu_y \sim Uniform(0, 100) \text{ and } \tau_y \sim Uniform(0, 100). \\ \text{Priors for } \theta_{j1} \colon \theta_{j1} \sim N(\mu_j, \sigma^2) \\ \sigma^2 \sim InvGamma(0.5, 0.5) \\ \mu_j \sim N(h_j, 7.5^2) \\ h_j = 0.1 * \text{Presidental Fundamentals}_{2020} + 0.9 * \text{Vote Share from Partisan Lean}_j \\ \text{Presidental Fundamentals}_i = \gamma_0 + \gamma_1 \text{June Approval Ratings for Incumbent Party}_i + \gamma_2 \text{Three Month Stock Growth}_i + \gamma_3 \text{2nd Quarter Real Income Growth}_i + \epsilon_i \\ \epsilon_i \sim N(0, \phi^2) \\ \end{cases}
```

For our presidential model, we wanted to incorporate state-level correlations that differ between each pair of states. For example, Wisconsin is much more similar to its Great Lakes neighbor Michigan both geographically and demographically than it is to Arizona, which is in the Southwest and has a much larger Hispanic population. So, we would expect that Wisconsin and Michigan have a higher correlation in their election results than Wisconsin and Arizona. In order to incorporate this into our presidential model, we used a multivariate normal distribution to model two-party vote share in each state, which allowed us to specify a covariance matrix for the states. We used a covariance matrix which was downloaded from the Economist forecast model (Gelman, 2020). These similarities between states were calculated by comparing their demographic and political profiles, such as the state's share of white voters and how urban/rural the state is.

In essence, the presidential model used fundamentals and vote share from partisan lean as a starting point for the expected vote share for the Democratic party, and update the priors with presidential election polling data. We predicted Presidental Fundamentals<sub>i</sub> from a linear regression model that used historical election year's economic data and June approval ratings of the incumbent party. When computing the prior, 10% weight is allocated to the fundamentals based on economic data and 90% weight to partisan lean because the effect of economic indicators has shrunk over the years as electorates became increasingly polarized (The Economist, 2020). In addition, economic indicators are particularly volatile in 2020 due to the COVID-19 pandemic. We chose not to do this for the U.S. House and Senate models because these races are generally a bit more localized (Gillespie et al. 2020).

one sentence on hyperparameters

Presidential elections in the United States are decided by the Electoral College, so estimating percentage support in each state alone does not tell us who wins the election. For each set of MCMC samples of two-party vote share by state, we subsequently use the predicted winner in each state to add up the electoral votes of each candidate. For states not in the model, their electoral votes are allocated assuming they vote the same way as in 2016. The probability of President Trump winning re-election is then the probability that he receives 270 or more electoral votes across simulations. Note that although Maine and Nebraska allocate some electoral votes by Congressional District, only two electoral votes are competitive due to this wrinkle, so for simplicity we simply allocate all electoral votes to the statewide winner of each respective state.

### Senate Election Model

For the Senate model, the states chosen are Alaska, Arizona, Colorado, Georgia, Iowa, Kansas, Maine, Michigan, Montana, North Carolina, South Carolina, and Texas. There is also a special election for the Senate in Georgia in addition to the regularly scheduled election. These fourteen races are rated as either "Toss Up", "Lean Republican", or "Lean Democrat" (the three most competitive categories) by the Cook Political Report (as of October 29). These states are also projected to have competitive Senate races by both the FiveThirtyEight and Economist models. Note that the Georgia special election actually has multiple Republicans and Democrats running on the same ballot. If no candidate wins over 50% of the vote, which is considered likely, the top two finishers will advance to a one-on-one runoff election in January (Ballotpedia, 2020). For simplicity, our model simply sums up the support for Republican candidates and compares that to the sum of the support for Democratic candidates, then treats this election like the others. (This is not the ideal way to simulate this election, but the difficulty of predicting turnout and the political environment for the January runoff election made this decision seem like the best one to make.) Once again, we only included poll response from likely voters that responded within 30 days of the election.

The response we will use is  $Y_k$ , the Democrat candidate's share of the two-party vote using the following model where the poll k (of K=fill in polls) ended t days (of T = 60 days) before the election and was conducted on state j (of J=14 states of interest).

$$Y_k \sim N(\beta_{jt}, \sigma_{yj}^2)$$
  
$$\beta_{jt} \sim N(\beta_{jt-1}, \sigma_{\beta_j}^2)$$

```
Priors for \sigma_{yj}^2: \sigma_{yj}^2 \sim InvGamma(\nu_u, \nu_y \tau_y)

\nu_y \sim Uniform(0, 100) and \tau_y \sim Uniform(0, 100).

Priors for \sigma_{\beta j}^2 \sigma_{\beta j}^2 \sim InvGamma(\nu_\beta, \nu_\beta \tau_\beta))

\nu_\beta \sim Uniform(0, 100) and \tau_\beta \sim Uniform(0, 100).

Priors for \beta_{j1} \beta_{j1} \sim N(\mu_j, \sigma^2)

\sigma^2 \sim InvGamma(0.5, 0.5)

\mu_j \sim N(h_j, 7.5^2)

h_j = \text{Vote Share from Partisan Lean}_j + \text{Incumbency Advantage}_j
```

For the U.S. Senate model we also take into account incumbency advantage. Analysis by FiveThirtyEight (Rakich, 2018) found that incumbent senators get a 2.6-point boost. For each incumbent was running a Senate race, depending on whether they were a Democrat or Republican, we either added or subtracted this incumbency adjustment with the prior mean computed from partisan lean.

For the NC-specific prior, we supplemented partisan lean and incumbency adjustment with voter turnout predicted by the model in our Interim Report. When computing the prior for NC only, 10% weight is allocated to predicted Democratic vote share from turnout and demographics, and 90% weight is allocated to partisan lean and incumbency adjustment. The turnout is weighted much less because there is considerable uncertainty surrounding turnout because of the COVID-19 pandemic. See Appendix A.2 for more specifics on how the voter turnout model was used to compute predicted Democratic vote share.

For predicting control of the U.S. Senate, things are complicated slightly by the fact that a 50/50 split of Senate seats is a possible outcome of the elections. In this case, the Vice President breaks the tie, so the party that wins the Presidential election will only need 50 Senate seats for a Senate majority, while the party that loses will need 51. Since our President model gives Democrat Joe Biden a very high chance of winning (discussed more below), we assume in the Senate model that Democrats will control the Senate in the case of a 50/50 split.

# House Election Model

The response we will use is  $Y_k$ , the Democrat candidate's share of the two-party vote using the following model where the poll k (of K=fill in polls) ended t days (of T = 60 days) before the election and was conducted on district j (where j is in districts  $1, \dots, 11, 13$  of North Carolina). For district 12, the vote share is coded as 100 because there is only one candidate, and she is a Democrat. Note that, due to the scarcity of poll responses for the NC House elections, we included all poll responses within 115 days of the election.

```
\begin{split} Y_k &\sim N(\beta_{jt}, \sigma_{yj}^2) \\ \beta_{jt} &\sim N(\beta_{jt-1}, \sigma_{\beta_j}^2) \\ \sigma_{yj}^2 &\sim InvGamma(\nu_u, \nu_y \tau_y) \\ \nu_y &\sim Uniform(0, 100) \text{ and } \tau_y \sim Uniform(0, 100). \\ \sigma_{\beta j}^2 &\sim InvGamma(\nu_\beta, \nu_\beta \tau_\beta)) \\ \nu_\beta &\sim Uniform(0, 100) \text{ and } \tau_\beta \sim Uniform(0, 100). \\ \beta_{j1} &\sim N(h_j, 7.5) \\ h_j &= 0.9 * \text{Vote Share from Partisan Lean}_j + 0.1 * \text{Expected Vote Share from Voter Turnout}_j \end{split}
```

According to FiveThirtyEight (Rakich, 2018),incumbent members of the House get a 2.7-point margin boost in their favor. For the U.S. House races, the incumbency adjustment was calculated by the same method as it was for the Senate races.

Expected Vote Share from Voter  $Turnout_j$  was calculated from the model in the Interim Report insert citation whatever that ends up being and also say something like our method for splitting undecided voters is in appendix A.3. Please see Appendix A.3 for more details.

## Results

#### Presidential Election Model

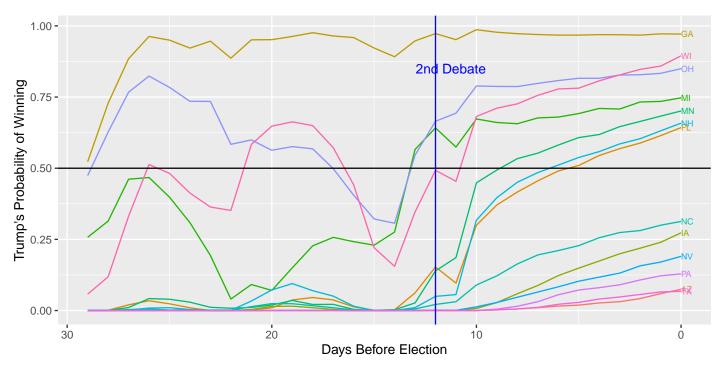


Figure 4: Probability of Re-election for President Trump over the 30 Days Before Election Day

4 shows how Trump's probability of winning the election changes over the 60 days before the election in each state of interest. It appears that his probability of winning increased after the last presidential debate. *check for final results* From 5 we see that swing states such as Florida and Ohio are predicted to vote Trump while other swing states such as Pennsylvania and North Carolina are predicted to vote Biden. *check for final results* 

Table 1: Predicted Probability of Winning and Electoral Vote Count

	Win Probability	Estimated EC Votes	2.5% Quantile EC Votes	97.5% Quantile EC Votes
Trump	0.08	219	154	325
Biden	0.92	319	213	384

The probability that Trump wins re-election is 0.08. The predicted electoral colleges votes for Trump is 219 with a 95% confidence interval of (154, 325).

## Senate Election Model

From 6 we see that for the Senate race, states such as Texas are predicted to lean heavily towards the Republican candidate and Democrats have a great than 50% chance of winning states such as Arizona and Michigan. From the histogram in 7 we see the distribution of the predicted number of Democrat seats point to a Democrat majority in the Senate, which is in agreement with the low probability that Republicans retain control of the Senate (0.1).

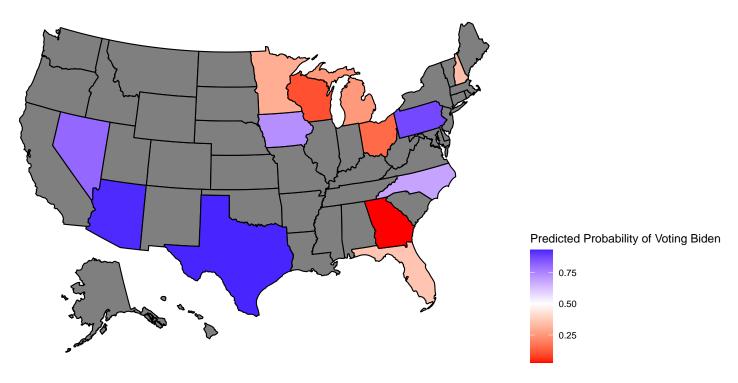


Figure 5: Plot of Predicted Presidential Result for States of Interest on Election Day

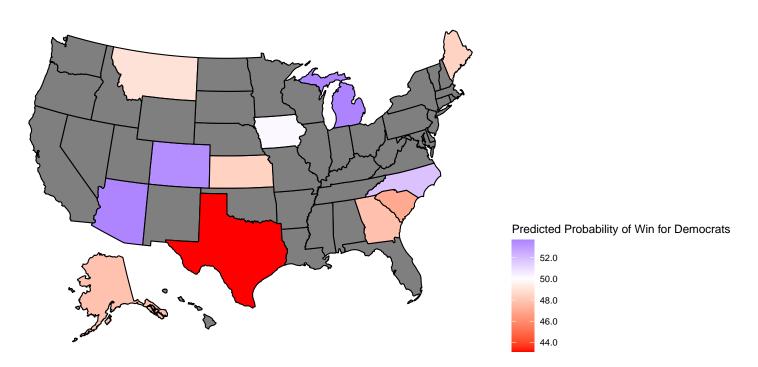


Figure 6: Plot of Predicted Senate Results for States of Interest on Election Day

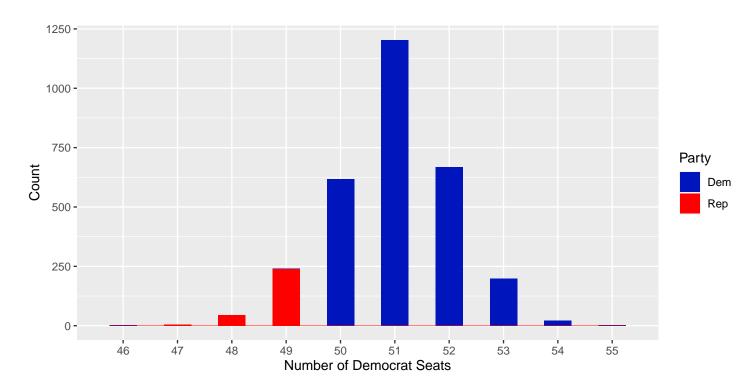


Figure 7: Plot of Predicted Senate Results for States of Interest on Election Day

Table 2: Predicted Vote Share for Tillis-Cunningham Race

	Estimate	2.5% Quantile	97.5% Quantile
Tillis	48.22	45.01	51.80
Cunningham	51.78	48.20	54.99

For the NC Senate race (Tillis vs. Cunningham), the predicted vote share for Cunningham is 51.78% with a 95% confidence interval of (48.2, 54.99).

# House Election Model

Table 3: Predicted Republican Vote Share in NC's 13 Districts

	Estimate	2.5% Quantile	97.5% Quantile
District 1	41.69	36.32	47.02
District 2	40.75	35.29	46.17
District 3	63.61	58.32	68.56
District 4	33.29	27.84	38.48
District 5	69.54	64.20	74.93
District 6	41.19	35.87	46.64
District 7	61.81	56.40	67.43
District 8	55.74	50.67	61.01
District 9	56.79	51.40	61.90
District 10	70.68	65.16	75.96
District 11	56.12	51.86	60.59
District 12	0.00	0.00	0.00
District 13	69.60	64.12	75.01

<sup>##</sup> OGR data source with driver: ESRI Shapefile

 $<sup>\</sup>texttt{\#\# Source: "/Users/cathylee/Documents/Course $f$ @ lders/Fall 2020/STA 440/Case 3/sta440 casestudy 3/C-Goods and the state of the$ 

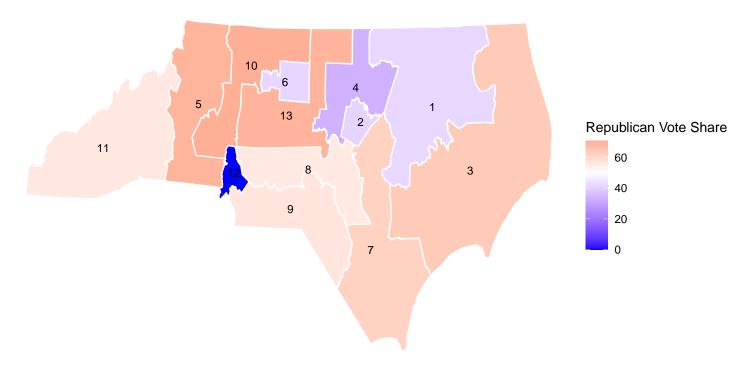


Figure 8: Plot of Predicted Senate Results for States of Interest on Election Day

50% partisan lean multiple times and the predictions for Trump's re-election probability was generally higher (approximately 0.25) than that from our main model, which makes sense since economic fundamental model contains stock growth and is slightly favored toward Trump. However, the sensitivity analysis models still point to an unlikely re-election.

 $\sigma_{yj}$ 

President model: unif(0,1) – I think this makes it more uninformative for gamma (does this hold for inv gamma?)  $Pr(Trump\ wins) = 0.128,\ 0.1176667,\ 0.2456667\ TLDR:\ comparable?$  Senate model:  $mu0 \sim N(priors,\ 1)$  (less variance)  $Pr(Rep\ control) = 0.1656667\ unif(0,1)\ Pr(Rep\ control) = 0.1436667\ sigma2\_0\_inv \sim gamma(3,0.5)$  (stronger prior?)  $Pr(Rep\ control) = 0.07466667\ TLDR:\ Tillis\ vote\ share\ +\ confidence\ intervals\ have\ been comparable, probability\ of\ republican\ control\ more\ sensitive$ 

To account for shock events,

## **Diagnostics**

## Discussion and Limitations

As polls are an important part of our data sources, we acknowledge that with the COVID-19 pandemic, polling has moved from in-person interviews to phone calls, live surveys and internet questions, which could lead to unknown biases with its lower response rates (Gelman, 2020). A recent election prediction study shows that state polls have much higher margins of error than expected (Shirani-Mehr et al., 2018).

# Appendix A

### A.1 Presidential Election Model

#### Presidential Model Purpose and Structure

The purpose of this model is to predict the probability that president Trump will win the election, as well as to predict the electoral college vote. The states chosen are Arizona, Florida, Georgia, Iowa, Michigan, Minnesota,

Nevada, New Hampshire, North Carolina, Ohio, Pennsylvania, Texas, and Wisconsin. These thirteen states are deemed to be competitive in the 2020 presidential race by political analysts.

The response we will use is  $Y_k$ , Biden's share of the two-party vote using the following model where the poll k (of K=3361 [insert final number] polls) ended t days (of T=30 days) before the election and was conducted on state j (of J=13 states of interest). We choose to use polling data from 30 days before the election (as opposed to over 30 days), as this aligns with Andrew Gelman's observation that polling data becomes more predictive as the day of poll becomes closer to election day (The Economist).

```
\begin{array}{l} Y_k \sim N(\theta_{jt},\sigma_{yj}^2) \\ \theta_{\cdots t} \sim MVN(\theta_{\cdots t-1},\Sigma) \\ \Sigma \sim Wishart(S,J+1) \text{ where } S \text{ is the state covariance matrix (obtained from Andrew Gelman's model) and } J \\ \text{is the number of states in the model.} \\ \text{Priors for } \sigma_{yj}^2 \colon \sigma_{yj}^2 \sim InvGamma(\nu_u,\nu_y\tau_y) \\ \nu_y \sim Uniform(0,100) \text{ and } \tau_y \sim Uniform(0,100). \\ \text{Priors for } \theta_{j1} \colon \theta_{j1} \sim N(\mu_j,\sigma^2) \\ \sigma^2 \sim InvGamma(0.5,0.5) \\ \mu_j \sim N(h_j,7.5^2) \\ h_j = 0.1 * \text{Presidental Fundamentals}_{2020} + 0.9 * \text{Vote Share from Partisan Lean}_j \\ \text{Presidental Fundamentals}_i = \gamma_0 + \gamma_1 \text{June Approval Ratings for Incumbent Party}_i + \gamma_2 \text{Three Month Stock Growth}_i + \gamma_3 \text{2nd Quarter Real Income Growth}_i + \epsilon_i \\ \epsilon_i \sim N(0,\phi^2) \end{array}
```

A hierarchical model was used, where Biden's share of the two-party vote for poll k on any given day t for state j is modelled as a normal distribution with mean  $\theta_{jt}$  and variance  $\sigma_{yj}^2$ . A random walk was used to calculate  $\theta_{jt}$  for each day t before the election (up until 30 days before the election) from  $\theta_{jt-1}$  and  $\Sigma$ , a JxJ state covariance matrix. The mean  $h_j$  of the normal prior on  $\mu_j$  (which is the mean of the normal prior on  $\theta_{j1}$ ) was calculated by multiplying the economic fundamentals Presidental Fundamentals, for i=2020 by 0.1 and state partisan lean by 0.9, then summing those two values. We predicted Presidental Fundamentals, from a linear regression model that had historical election year's June approval rating of the incumbent party, three month stock growth, and 2nd quarter real income growth as predictors. keep?

# Raw Model Output

```
##
                                    sd
                                                          97.5%
                       mean
## Sigma[1,1]
                 0.55224844 0.4284299
                                       0.130028220
                                                      1.5515671
## Sigma[2,1]
                 0.39637683 0.3364139 -0.019537113
                                                      1.2245520
## Sigma[3,1]
                 0.22913153 0.3511835 -0.265142162
                                                      1.0442528
## Sigma[4,1]
                 0.31696354 0.3089421 -0.067440477
                                                      1.0940727
## Sigma[5,1]
                 0.30968416 0.2903351 -0.069050958
                                                      1.0111283
## Sigma[6,1]
                 0.30335536 0.3385876 -0.080220985
                                                      1.0921662
## Sigma[7,1]
                 0.26147949 0.2780797 -0.087132782
                                                      0.9246032
## Sigma[8,1]
                 0.26106192 0.3117592 -0.163278377
                                                      0.9799422
## Sigma[9,1]
                 0.44209205 0.3869324
                                       0.032090007
                                                      1.3633532
## Sigma[10,1]
                 0.31890794 0.3208049 -0.074412137
                                                      1.0995922
## Sigma[11,1]
                 0.30358737 0.2990858 -0.102874853
                                                      0.9904030
## Sigma[12,1]
                 0.40706673 0.4323321 -0.040544427
                                                      1.4668525
## Sigma[13,1]
                 0.23396808 0.2470595 -0.114951396
                                                     0.8455124
## Sigma[1,2]
                 0.39637683 0.3364139 -0.019537113
                                                      1.2245520
## Sigma[2,2]
                 0.59659674 0.4122285 0.135627761
                                                      1.7001270
## Sigma[3,2]
                 0.18084427 0.3384868 -0.405991874
                                                      0.9405197
## Sigma[4,2]
                 0.36461373 0.3154110 -0.018485705
                                                      1.1814129
## Sigma[5,2]
                 0.41234840 0.3158972 0.054731831
                                                      1.2013768
```

```
Sigma[6,2]
                 0.32155732 0.3186707 -0.070342803
                                                      1.0886544
   Sigma[7,2]
##
                 0.31376253 0.2904751 -0.046181364
                                                      1.0501727
  Sigma[8,2]
                                                      1.1775075
##
                 0.34428953 0.3171198 -0.067948711
   Sigma[9,2]
                 0.42044418 0.3796895 -0.015035160
                                                      1.4208399
##
##
   Sigma[10,2]
                 0.39006382 0.3344196
                                        0.016022570
                                                      1.2337526
   Sigma[11,2]
                 0.42827510 0.3230276
                                        0.060542784
                                                      1.2659536
  Sigma[12,2]
                 0.30504366 0.3748234 -0.200395206
                                                      1.2918375
  Sigma[13,2]
                 0.30815403 0.2625373 -0.025453063
                                                      0.9718564
  Sigma[1,3]
                 0.22913153 0.3511835 -0.265142162
                                                      1.0442528
  Sigma[2,3]
                 0.18084427 0.3384868 -0.405991874
                                                      0.9405197
##
##
  Sigma[3,3]
                 0.57048283 0.5111974
                                        0.117884572
                                                      1.8950953
  Sigma[4,3]
                 0.19311008 0.3176773 -0.322389359
                                                      0.9506952
  Sigma[5,3]
                 0.19573876 0.2952243 -0.271924787
                                                      0.8984003
  Sigma[6,3]
                 0.18020273 0.3212975 -0.319502761
                                                      0.9537401
  Sigma[7,3]
                 0.31915142 0.3315678 -0.060611472
                                                      1.2177244
  Sigma[8,3]
##
                 0.08543833 0.3109987 -0.547602900
                                                      0.7460938
  Sigma[9,3]
                 0.15866933 0.3773115 -0.528904912
                                                      0.9656317
##
   Sigma[10,3]
                 0.24120108 0.3247990 -0.227809678
                                                      1.0656533
  Sigma[11,3]
                 0.15471430 0.3185689 -0.430793289
                                                      0.8753156
  Sigma[12,3]
                 0.24737169 0.4168516 -0.385605944
                                                      1.2949161
  Sigma[13,3]
                 0.12095536 0.2588323 -0.398800277
                                                      0.7181715
  Sigma[1,4]
                 0.31696354 0.3089421 -0.067440477
                                                      1.0940727
  Sigma[2,4]
                 0.36461373 0.3154110 -0.018485705
                                                      1.1814129
  Sigma[3,4]
##
                 0.19311008 0.3176773 -0.322389359
                                                      0.9506952
  Sigma[4,4]
                 0.49448467 0.3584712
                                        0.130288445
                                                      1.4643645
##
  Sigma[5,4]
                 0.40346074 0.3058430
                                        0.080006163
                                                      1.1501417
  Sigma[6,4]
                 0.38224234 0.3167077
##
                                        0.047934823
                                                      1.1785877
                 0.32526127 0.2714697
##
  Sigma[7,4]
                                        0.010473638
                                                      1.0178458
  Sigma[8,4]
                 0.34557766 0.3027402 -0.012735324
                                                      1.0522166
  Sigma[9,4]
                 0.28350474 0.3301138 -0.143475470
                                                      1.1583900
  Sigma[10,4]
                 0.40140218 0.3279991
                                         0.051659627
                                                      1.2225763
##
  Sigma[11,4]
                 0.39842972 0.3016645
                                        0.058235579
                                                      1.1741192
  Sigma[12,4]
                 0.24892208 0.3532325
                                       -0.230395606
                                                      1.1552519
  Sigma[13,4]
##
                 0.33818848 0.2596132
                                        0.036754763
                                                      0.9783368
  Sigma[1,5]
                 0.30968416 0.2903351 -0.069050958
##
                                                      1.0111283
   Sigma[2,5]
                 0.41234840 0.3158972
                                         0.054731831
                                                      1.2013768
   Sigma[3,5]
                 0.19573876 0.2952243
                                       -0.271924787
                                                      0.8984003
  Sigma[4,5]
                 0.40346074 0.3058430
                                        0.080006163
                                                      1.1501417
##
  Sigma[5,5]
                 0.48115187 0.3462441
                                        0.131740465
                                                      1.3662320
  Sigma[6,5]
                 0.36842193 0.3013049
                                        0.044019140
                                                      1.0926948
##
  Sigma[7,5]
                 0.32168564 0.2588782
                                        0.008834885
                                                      0.9668150
  Sigma[8,5]
##
                 0.36340086 0.3111115
                                        0.018704388
                                                      1.1189954
  Sigma[9,5]
                 0.30419552 0.3130704 -0.093307097
                                                      1.1069631
  Sigma[10,5]
                 0.41118773 0.3236804
                                        0.077152459
                                                      1.2207955
## Sigma[11,5]
                 0.42590999 0.3151122
                                         0.088310597
                                                      1.2211571
  Sigma[12,5]
                 0.23350886 0.3318924 -0.222729824
                                                      1.0670429
##
  Sigma[13,5]
                 0.35692275 0.2678183
                                        0.060796980
                                                      1.0253861
   Sigma[1,6]
                 0.30335536 0.3385876 -0.080220985
##
                                                      1.0921662
##
  Sigma[2,6]
                 0.32155732 0.3186707 -0.070342803
                                                      1.0886544
  Sigma[3,6]
                 0.18020273 0.3212975
##
                                       -0.319502761
                                                      0.9537401
  Sigma[4,6]
                 0.38224234 0.3167077
                                        0.047934823
                                                      1.1785877
## Sigma[5,6]
                 0.36842193 0.3013049
                                        0.044019140
                                                      1.0926948
```

```
Sigma[6,6]
                 0.47216101 0.4038561
                                         0.110129226
                                                      1.5129629
   Sigma[7,6]
##
                 0.29139486 0.2832279
                                       -0.031382311
                                                      0.9595481
  Sigma[8,6]
                 0.34963068 0.3075001
##
                                         0.008258038
                                                      1.1369028
   Sigma[9,6]
                 0.25362418 0.3197088 -0.171556760
##
                                                      1.0064422
##
  Sigma[10,6]
                 0.38449907 0.3507409
                                        0.043578280
                                                      1.2330901
   Sigma[11,6]
                 0.37558078 0.3096065
                                        0.034708971
                                                      1.1503817
  Sigma[12,6]
                 0.23712627 0.4015493 -0.261133958
                                                      1.2065390
  Sigma[13,6]
                 0.32121459 0.2524105
                                         0.025577235
                                                      0.9917422
  Sigma[1,7]
                 0.26147949 0.2780797 -0.087132782
                                                      0.9246032
  Sigma[2,7]
                 0.31376253 0.2904751 -0.046181364
##
                                                      1.0501727
##
  Sigma[3,7]
                 0.31915142 0.3315678 -0.060611472
                                                      1.2177244
  Sigma[4,7]
                 0.32526127 0.2714697
                                        0.010473638
                                                      1.0178458
  Sigma[5,7]
                 0.32168564 0.2588782
                                        0.008834885
                                                      0.9668150
  Sigma[6,7]
                 0.29139486 0.2832279 -0.031382311
                                                      0.9595481
  Sigma[7,7]
                 0.42841992 0.3180437
                                        0.106675017
                                                      1.2796450
  Sigma[8,7]
##
                 0.23354090 0.2478805 -0.124560322
                                                      0.8645338
  Sigma[9,7]
                 0.22582433 0.2851076 -0.166077318
                                                      0.9142880
                 0.34556177 0.2911713
##
   Sigma[10,7]
                                        0.024104777
                                                      1.0391745
  Sigma[11,7]
                 0.30171247 0.2614041 -0.025596858
                                                      0.9686740
  Sigma[12,7]
                 0.23373481 0.3245889 -0.182196395
                                                      1.0460914
  Sigma[13,7]
                 0.25661497 0.2176755 -0.036485626
                                                      0.7820659
  Sigma[1,8]
                 0.26106192 0.3117592 -0.163278377
                                                      0.9799422
  Sigma[2,8]
                 0.34428953 0.3171198 -0.067948711
                                                      1.1775075
  Sigma[3,8]
##
                 0.08543833 0.3109987 -0.547602900
                                                      0.7460938
  Sigma[4,8]
                 0.34557766 0.3027402 -0.012735324
                                                      1.0522166
##
  Sigma[5,8]
                 0.36340086 0.3111115
                                        0.018704388
                                                      1.1189954
  Sigma[6,8]
##
                 0.34963068 0.3075001
                                        0.008258038
                                                      1.1369028
                 0.23354090 0.2478805 -0.124560322
##
  Sigma[7,8]
                                                      0.8645338
  Sigma[8,8]
                 0.49516759 0.3900034
                                        0.118183036
                                                      1.5470355
  Sigma[9,8]
                 0.22523025 0.3217966 -0.254900961
                                                      0.9871067
  Sigma[10,8]
                 0.32107630 0.3172237 -0.069846467
                                                      1.0641628
##
  Sigma[11,8]
                 0.37706769 0.3086602
                                        0.017083869
                                                      1.1352961
  Sigma[12,8]
                 0.18879742 0.3554798 -0.338498997
                                                      1.0770581
  Sigma[13,8]
##
                 0.33317965 0.2711368
                                        0.042592208
                                                      1.0290457
  Sigma[1,9]
##
                 0.44209205 0.3869324
                                        0.032090007
                                                      1.3633532
  Sigma[2,9]
                 0.42044418 0.3796895 -0.015035160
                                                      1.4208399
   Sigma[3,9]
                 0.15866933 0.3773115 -0.528904912
                                                      0.9656317
  Sigma[4,9]
                 0.28350474 0.3301138 -0.143475470
                                                      1.1583900
##
  Sigma[5,9]
                 0.30419552 0.3130704 -0.093307097
                                                      1.1069631
  Sigma[6,9]
                 0.25362418 0.3197088 -0.171556760
                                                      1.0064422
##
  Sigma[7,9]
                 0.22582433 0.2851076 -0.166077318
                                                      0.9142880
  Sigma[8,9]
                 0.22523025 0.3217966 -0.254900961
##
                                                      0.9871067
  Sigma[9,9]
                 0.62783722 0.6628192
                                        0.122593527
                                                      2.1797932
   Sigma[10,9]
                 0.30280755 0.3952960 -0.137340909
                                                      1.2219352
  Sigma[11,9]
                 0.31162711 0.3342808 -0.116120797
                                                      1.1485954
  Sigma[12,9]
                 0.41757345 0.4719417 -0.059015501
##
                                                      1.6119564
  Sigma[13,9]
                 0.21595068 0.2673372 -0.179592611
                                                      0.8663675
   Sigma[1,10]
                 0.31890794 0.3208049 -0.074412137
##
                                                      1.0995922
##
  Sigma[2,10]
                 0.39006382 0.3344196
                                                      1.2337526
                                        0.016022570
  Sigma[3,10]
                 0.24120108 0.3247990 -0.227809678
                                                      1.0656533
  Sigma[4,10]
                 0.40140218 0.3279991
                                        0.051659627
                                                      1.2225763
## Sigma[5,10]
                 0.41118773 0.3236804
                                        0.077152459
                                                      1.2207955
```

```
Sigma[6,10]
                 0.38449907 0.3507409
                                        0.043578280
                                                      1.2330901
   Sigma[7,10]
                 0.34556177 0.2911713
                                        0.024104777
                                                      1.0391745
  Sigma[8,10]
                 0.32107630 0.3172237 -0.069846467
                                                      1.0641628
   Sigma[9,10]
##
                 0.30280755 0.3952960
                                       -0.137340909
                                                      1.2219352
##
  Sigma[10,10]
                 0.50269435 0.4023515
                                        0.121665342
                                                      1.5504090
   Sigma[11,10]
                 0.40510713 0.3234143
                                        0.055958392
                                                      1.2417530
  Sigma[12,10]
                 0.24547993 0.3664216 -0.247336974
                                                      1.1846637
  Sigma[13,10]
                 0.33325393 0.2685002
                                         0.018929105
                                                      0.9862554
  Sigma[1,11]
                 0.30358737 0.2990858
                                       -0.102874853
                                                      0.9904030
  Sigma[2,11]
                 0.42827510 0.3230276
##
                                        0.060542784
                                                      1.2659536
##
  Sigma[3,11]
                 0.15471430 0.3185689 -0.430793289
                                                      0.8753156
  Sigma[4,11]
                 0.39842972 0.3016645
                                        0.058235579
                                                      1.1741192
  Sigma[5,11]
                 0.42590999 0.3151122
                                        0.088310597
                                                      1.2211571
  Sigma[6,11]
                 0.37558078 0.3096065
                                        0.034708971
                                                      1.1503817
## Sigma[7,11]
                 0.30171247 0.2614041
                                       -0.025596858
                                                      0.9686740
  Sigma[8,11]
                 0.37706769 0.3086602
##
                                        0.017083869
                                                      1.1352961
  Sigma[9,11]
                 0.31162711 0.3342808 -0.116120797
                                                      1.1485954
  Sigma[10,11]
                 0.40510713 0.3234143
                                        0.055958392
                                                      1.2417530
  Sigma[11,11]
                 0.49920785 0.3608231
                                        0.132356279
                                                      1.3793590
  Sigma[12,11]
                 0.23008003 0.3559078 -0.279849773
                                                      1.1227044
  Sigma[13,11]
                 0.35658729 0.2583648
                                        0.056404538
                                                      1.0062507
  Sigma[1,12]
                 0.40706673 0.4323321 -0.040544427
                                                      1.4668525
  Sigma[2,12]
                 0.30504366 0.3748234 -0.200395206
                                                      1.2918375
  Sigma[3,12]
##
                 0.24737169 0.4168516 -0.385605944
                                                      1.2949161
  Sigma[4,12]
                 0.24892208 0.3532325 -0.230395606
                                                      1.1552519
##
  Sigma[5,12]
                 0.23350886 0.3318924 -0.222729824
                                                      1.0670429
  Sigma[6,12]
##
                 0.23712627 0.4015493 -0.261133958
                                                      1.2065390
                 0.23373481 0.3245889 -0.182196395
  Sigma[7,12]
                                                      1.0460914
  Sigma[8,12]
                 0.18879742 0.3554798 -0.338498997
                                                      1.0770581
  Sigma[9,12]
                 0.41757345 0.4719417 -0.059015501
                                                      1.6119564
  Sigma[10,12]
                 0.24547993 0.3664216 -0.247336974
                                                      1.1846637
##
  Sigma[11,12]
                 0.23008003 0.3559078 -0.279849773
                                                      1.1227044
  Sigma[12,12]
                 0.64882469 0.6212399
                                        0.125415675
                                                      2.3163965
  Sigma[13,12]
##
                 0.15450660 0.2790072 -0.288551713
                                                      0.8356189
  Sigma[1,13]
##
                 0.23396808 0.2470595 -0.114951396
                                                      0.8455124
   Sigma[2,13]
                 0.30815403 0.2625373 -0.025453063
                                                      0.9718564
   Sigma[3,13]
                 0.12095536 0.2588323 -0.398800277
                                                      0.7181715
  Sigma[4,13]
                 0.33818848 0.2596132
                                        0.036754763
                                                      0.9783368
##
  Sigma[5,13]
                 0.35692275 0.2678183
                                        0.060796980
                                                      1.0253861
  Sigma[6,13]
                 0.32121459 0.2524105
                                        0.025577235
                                                      0.9917422
##
  Sigma[7,13]
                 0.25661497 0.2176755
                                       -0.036485626
                                                      0.7820659
  Sigma[8,13]
                 0.33317965 0.2711368
##
                                        0.042592208
                                                      1.0290457
  Sigma[9,13]
                 0.21595068 0.2673372 -0.179592611
                                                      0.8663675
  Sigma[10,13]
                 0.33325393 0.2685002
                                        0.018929105
                                                      0.9862554
## Sigma[11,13]
                 0.35658729 0.2583648
                                        0.056404538
                                                      1.0062507
  Sigma[12,13]
                 0.15450660 0.2790072
##
                                       -0.288551713
                                                      0.8356189
  Sigma[13,13]
                 0.39253282 0.2648491
                                        0.110801904
                                                      1.0774590
   sigma2_y[1]
##
                 2.07698410 0.4242994
                                         1.400318204
                                                      3.0530882
  sigma2_y[2]
                  1.95644998 0.3802834
                                                      2.8389453
##
                                         1.315545700
   sigma2_y[3]
##
                 2.10830086 0.4729073
                                         1.393772409
                                                      3.2163579
   sigma2_y[4]
                 2.08387738 0.4718844
                                         1.363591960
                                                      3.1305385
## sigma2_y[5]
                 2.25867366 0.4707497
                                         1.565265173
                                                      3.3067240
```

```
## sigma2_y[6]
                 1.98702060 0.4214625
                                       1.277127513
                                                     2.9318484
## sigma2_y[7]
                 1.87706605 0.3601562
                                       1.237199584
                                                     2.6817688
## sigma2_y[8]
                 1.98796623 0.4554713
                                       1.229529093
                                                     2.9714077
## sigma2_y[9]
                 2.00621551 0.4601906
                                      1.274673100
                                                     3.0483831
##
  sigma2_y[10]
                 1.93236318 0.4151012
                                       1.233017794
                                                     2.8055894
  sigma2_y[11]
                                       1.359558155
                 1.98677136 0.3753971
                                                     2.8113952
## sigma2_y[12]
                 1.97906343 0.4193522
                                       1.277671666
                                                     2.8987570
## sigma2_y[13]
                 1.98137490 0.3839901
                                       1.326860573
                                                    2.8177664
## theta[1,1]
                48.85228423 2.0615539 44.854628953 52.5960348
## theta[2,1]
                49.21002823 2.0745325 44.499960674 53.0740373
## theta[3,1]
                48.50192718 2.1982790 43.853799481 52.3648494
## theta[4,1]
                48.00486924 1.7899298 43.516113153 50.7916420
## theta[5,1]
                51.69888489 1.7986956 46.794510556 54.7411875
## theta[6,1]
                51.56064768 2.2024818 46.538841167 55.0416844
## theta[7,1]
                49.26728502 1.7188486 45.475730136 52.2158612
## theta[8,1]
                54.15544825 2.7017735 48.685336950 58.8889362
                50.62628875 2.4072132 44.944447180 54.6968791
## theta[9,1]
## theta[10,1]
                46.41150176 2.0686728 41.617483924 50.1049839
## theta[11,1]
                50.99180081 1.8660922 46.452521269 54.7367977
## theta[12,1]
                47.47861054 2.8094223 41.427044129 52.7151199
                52.36930400 1.7670892 48.056520073 55.5814482
## theta[13,1]
## theta[1,2]
                48.98658928 2.0166669 44.950181534 52.6159146
## theta[2,2]
                49.31554269 2.0562421 44.836465936 53.1019569
## theta[3,2]
                48.61299919 2.1918352 43.877804246 52.4770072
## theta[4,2]
                48.15626096 1.7661588 44.314751299 51.0042402
## theta[5,2]
                51.83388580 1.7709182 47.694221518 54.9067575
## theta[6,2]
                51.70872066 2.1741503 46.752988688 55.2378182
## theta[7,2]
                49.38713054 1.7028742 45.654910445 52.3222317
## theta[8,2]
                54.25437983 2.6638529 49.122386148 59.0329781
## theta[9,2]
                50.74833265 2.3668706 45.181808949 54.7020289
## theta[10,2]
                46.55861235 2.0207841 41.924013063 50.0730062
## theta[11,2]
                51.11634246 1.8440447 47.051586664 54.7939152
## theta[12,2]
                47.60937478 2.7567570 41.574362719 52.5895442
## theta[13,2]
                52.48668989 1.7278661 48.649662074 55.6415948
## theta[1,3]
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## theta[2,3]
                49.41633744 1.9843024 45.144275093 53.1164468
## theta[3,3]
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## theta[4,3]
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## theta[5,3]
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## theta[6,3]
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## theta[7,3]
                49.49425799 1.6648425 45.837584050 52.3534780
                54.33764549 2.5857312 49.339955995 59.1305070
## theta[8,3]
## theta[9,3]
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## theta[10,3]
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## theta[11,3]
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## theta[12,3]
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## theta[13,3]
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## theta[1,4]
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## theta[2,4]
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## theta[3,4]
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## theta[4,4]
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## theta[5,4]
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## theta[6,4]
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  theta[7,4]
##
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## theta[8,4]
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  theta[9,4]
                50.95766536 2.2176702 45.643570932 54.5860407
##
##
  theta[10,4]
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                51.34058338 1.7357414 47.707226210 54.6088425
  theta[11,4]
## theta[12,4]
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## theta[13,4]
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## theta[1,5]
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## theta[2,5]
                49.63155932 1.8478354 45.810946283 53.0678063
## theta[3,5]
                48.95047799 1.9838573 44.621533543 52.6682685
                48.58416849 1.6559409 45.210107137 51.5342607
## theta[4,5]
## theta[5,5]
                52.19270007 1.6369381 48.659066880 55.2267746
                52.12606574 2.0065433 47.637827061 55.6074154
## theta[6,5]
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## theta[7,5]
## theta[8,5]
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                51.05854584 2.1791292 46.010931380 54.7071479
## theta[9,5]
## theta[10,5]
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                51.46426518 1.6812446 47.968379923 54.5865910
## theta[11,5]
  theta[12,5]
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##
                52.76182504 1.5900140 49.666139306 55.7274165
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  theta[1,6]
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## theta[2,6]
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## theta[3,6]
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                48.72514575 1.5799572 45.460468763 51.5557327
## theta[4,6]
## theta[5,6]
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## theta[6,6]
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## theta[7,6]
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## theta[8,6]
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## theta[9,6]
                51.18640240 2.0213552 46.413971577 54.4408511
## theta[10,6]
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                51.57885896 1.5740651 48.338707897 54.5169180
## theta[11,6]
## theta[12,6]
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## theta[13,6]
                52.85840073 1.5085002 49.923875122 55.7011712
                49.56157686 1.6358514 45.998933615 52.4261388
## theta[1,7]
## theta[2,7]
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## theta[3,7]
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## theta[4,7]
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## theta[5,7]
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## theta[7,7]
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                54.70319323 2.2637984 50.407691334 58.9498595
## theta[8,7]
## theta[9,7]
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## theta[10,7]
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## theta[11,7]
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## theta[12,7]
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## theta[13,7]
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## theta[2,8]
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## theta[3,8]
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                49.01709631 1.4196515 46.075975823 51.6331778
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## theta[5,8]
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## theta[6,8]
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## theta[8,8]
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##
  theta[9,8]
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  theta[12,8]
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## theta[13,8]
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## theta[1,9]
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## theta[2,9]
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## theta[3,9]
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                49.16219270 1.3264517 46.471946636 51.5616772
## theta[4,9]
## theta[5,9]
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## theta[6,9]
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## theta[7,9]
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## theta[8,9]
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## theta[9,9]
## theta[10,9]
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##
                51.95873842 1.2441081 49.430846400 54.3413047
  theta[11,9]
  theta[12,9]
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## theta[2,10]
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## theta[3,10]
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                49.31733916 1.2126084 46.787879877 51.5050547
## theta[4,10]
## theta[5,10]
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                52.90206963 1.4257426 49.897150258 55.4368748
## theta[6,10]
## theta[7,10]
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## theta[8,10]
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## theta[10,10] 47.70531881 1.2623331 44.965146811 49.9474390
## theta[11,10] 52.10000484 1.0737714 49.929329893 54.2257666
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## theta[13,10] 53.25158812 1.0813613 51.101692369 55.2985864
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## theta[1,11]
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## theta[3,11]
                49.45318581 1.2188754 46.898470655 51.7096490
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## theta[6,11]
## theta[7,11]
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                55.19285293 1.7519518 52.093319590 58.6581098
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## theta[11,11] 52.22913550 0.8523918 50.567246921 53.9535852
## theta[12,11] 48.76529781 1.5744507 45.413620566 51.6300558
## theta[13,11] 53.34301013 0.9130715 51.516032082 55.0755134
## theta[1,12]
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## theta[2,12]
                51.12295061 0.6919367 49.706864780 52.4637255
## theta[3,12]
                49.79047452 0.9244765 47.934543936 51.5353107
                50.08528856 0.9706081 48.148653493 51.8959814
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## theta[6,12]
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## theta[1,13]
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## theta[2,13]
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## theta[3,13]
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## theta[4,13]
## theta[5,13]
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## theta[6,13]
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## theta[7,13]
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## theta[8,13]
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## theta[9,13]
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## theta[12,13] 49.45819044 1.2055082 46.833074880 51.7295150
## theta[13,13] 53.71233056 0.7699306 52.171507774 55.2063806
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## theta[2,14]
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## theta[3,14]
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                50.35126390 0.9208277 48.475724503 52.1064476
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## theta[5,14]
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                53.87350229 0.8639367 52.106617098 55.5082931
## theta[6,14]
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## theta[7,14]
## theta[8,14]
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                53.00803156 0.9882198 51.000487410 54.9859583
## theta[9,14]
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## theta[13,14] 53.91069390 0.6945690 52.535637527 55.2985174
## theta[1,15]
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##
  theta[2,15]
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                50.43932643 0.7328710 48.997753525 51.8564429
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## theta[4,15]
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## theta[6,15]
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## theta[7,15]
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## theta[8,15]
## theta[9,15]
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## theta[13,15] 54.16634188 0.4750141 53.251545090 55.0886693
## theta[1,16]
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## theta[2,16]
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## theta[3,16]
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                50.55269112 0.7257070 49.099808521 51.9570988
## theta[4,16]
## theta[5,16]
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## theta[6,16]
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## theta[8,16]
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##
  theta[9,16]
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  theta[10,16] 49.02949595 0.6808884 47.644238105 50.3742531
  theta[11,16]
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## theta[1,17]
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## theta[2,17]
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## theta[3,17]
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## theta[5,17]
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## theta[6,17]
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## theta[7,17]
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## theta[8,17]
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## theta[9,17]
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## theta[11,17] 52.68892761 0.6109176 51.383277025 53.8511236
## theta[12,17] 50.19191854 0.8051052 48.672761348 51.8508098
## theta[13,17] 53.39965875 0.5840649 52.211252766 54.5076390
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## theta[2,18]
                51.31123378 0.8028288 49.638942900 52.8052255
## theta[3,18]
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                49.82352425 0.8866311 48.008038016 51.5099324
## theta[4,18]
## theta[5,18]
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                53.44711560 0.8661712 51.690147198 55.0272516
## theta[6,18]
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## theta[7,18]
## theta[8,18]
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## theta[9,18]
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## theta[11,18] 52.44892369 0.7774099 50.750517461 53.8661870
## theta[12,18] 49.97630722 1.0515925 47.790245498 52.0639593
## theta[13,18] 53.22265434 0.6874641 51.808741097 54.4809073
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  theta[2,19]
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                50.71868869 1.0156778 48.769931900 52.8571373
  theta[3,19]
## theta[4,19]
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## theta[5,19]
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## theta[6,19]
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## theta[7,19]
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                55.14472633 1.3339375 52.699200490 57.6785532
## theta[8,19]
## theta[9,19]
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## theta[10,19]
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## theta[11,19] 52.28670091 0.8169994 50.494897348 53.7252940
## theta[12,19] 49.82489171 1.1483054 47.504237482 52.1062835
## theta[13,19] 53.11055558 0.6879769 51.732834707 54.4423767
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## theta[2,20]
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## theta[3,20]
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                49.59606074 0.9316887 47.648247902 51.3509774
## theta[4,20]
## theta[5,20]
                53.10178204 0.7662401 51.452066553 54.5459012
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## theta[6,20]
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## theta[8,20]
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## theta[9,20]
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## theta[13,20] 53.13405748 0.7596988 51.616652293 54.5526629
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## theta[2,21]
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## theta[3,21]
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               49.66427945 0.8897184 47.879684459 51.3889902
## theta[4,21]
## theta[5,21]
                53.17449681 0.6827048 51.784784741 54.4147377
## theta[6,21]
                53.50513329 0.8292140 51.805754036 55.0691959
## theta[7,21]
                51.45489587 0.6197845 50.222292907 52.6994365
## theta[8,21]
                55.19059834 1.2755557 52.729162372 57.6399418
                52.51456659 1.2028942 50.017031307 54.6926666
## theta[9,21]
## theta[10,21] 48.52382126 0.9306190 46.574897692 50.3229696
## theta[11,21] 52.36989639 0.8414357 50.432966554 53.8071915
## theta[12,21] 49.81734408 1.2853890 47.210123168 52.4234421
## theta[13,21] 53.26757637 0.7519813 51.705964642 54.6409560
## theta[1,22]
               51.60442899 0.6985955 50.254844467 52.9670834
## theta[2,22]
               51.29362925 0.6436591 49.895623849 52.4878940
## theta[3,22]
               51.03897907 0.8135771 49.522562247 52.7651558
## theta[4,22]
               49.82833718 0.7581856 48.277523840 51.2774017
                53.45253249 0.5498345 52.315939210 54.5149288
## theta[5,22]
               53.76182747 0.7310025 52.285053553 55.1325121
## theta[6,22]
## theta[7,22]
                51.48913468 0.5469793 50.408007359 52.5690509
## theta[8,22]
                55.46330106 1.1444546 53.340734786 57.6122859
## theta[9,22]
                52.55050296 1.0569618 50.380502030 54.5401252
## theta[10,22] 48.73440964 0.7698936 47.256176326 50.2873685
## theta[11,22] 52.64087838 0.6878629 51.179723510 53.8731305
## theta[12,22] 49.71794853 1.1758403 47.389483668 52.1140846
## theta[13,22] 53.54746585 0.6139231 52.328641258 54.7422087
## theta[1,23] 51.82525894 0.7351812 50.371002646 53.2993551
## theta[2,23]
                51.87460061 0.5281152 50.837930850 52.9342701
                51.15481628 0.6733604 49.893005708 52.4748938
## theta[3,23]
## theta[4,23]
                50.27822249 0.7317203 48.809640467 51.6981230
## theta[5,23]
                53.95367922 0.5327745 52.909746152 55.0637368
                54.07226518 0.7374206 52.502359040 55.4788840
## theta[6,23]
## theta[7,23]
                51.84756459 0.5604814 50.800957533 53.0221947
                55.83545478 0.9557865 54.049030797 57.6379897
## theta[8,23]
## theta[9,23]
                52.81882237 0.9275395 50.878418342 54.6478594
## theta[10,23] 49.19246096 0.6742578 47.950144851 50.6810987
## theta[11,23] 53.12136591 0.5429298 51.980605676 54.1415959
## theta[12,23] 49.81579900 1.0364114 47.682819029 51.8501554
## theta[13,23] 53.91059851 0.5786552 52.832482449 55.0569655
## theta[1,24]
                51.55494415 0.6422085 50.262773275 52.7919837
## theta[2,24]
                51.87680232 0.5313704 50.865638252 52.9351388
## theta[3,24]
                50.54848337 0.6382382 49.258105668 51.8178396
                50.23896291 0.6493978 48.987254596 51.5183206
## theta[4,24]
## theta[5,24]
                53.92370441 0.4739819 53.000547561 54.8610517
```

```
## theta[6,24]
                53.97208250 0.6981698 52.514122593 55.2771597
## theta[7,24]
                51.62565523 0.4495364 50.751522025 52.5165934
## theta[8,24]
                55.92605079 1.0908137 53.952123650 57.9919769
## theta[9,24]
                52.63361834 0.7677086 50.998801768 54.0894613
##
  theta[10,24] 49.05623405 0.5758548 47.964933387 50.2519773
  theta[11,24]
                53.18511443 0.4530040 52.305326523 54.0966851
## theta[12,24] 49.45892687 0.8559553 47.730986848 51.0749667
## theta[13,24] 53.92186940 0.4693100 53.010769013 54.8535111
## theta[1,25]
                51.45852022 0.7556648 49.932836983 52.9178498
## theta[2,25]
                51.82361860 0.6500892 50.541084861 53.0773968
## theta[3,25]
                50.38905200 0.8457005 48.647619549 52.0570930
                50.15825613 0.7666013 48.680764567 51.6349386
## theta[4,25]
## theta[5,25]
                53.81727044 0.6448151 52.587640368 55.1072701
                53.86867049 0.8446513 52.056032307 55.4362229
## theta[6,25]
## theta[7,25]
                51.50322975 0.6390479 50.206024074 52.7225227
## theta[8,25]
                55.85982728 1.1928256 53.679647518 58.1422849
                52.61924779 0.8574941 50.839980535 54.2472737
## theta[9,25]
## theta[10,25] 48.96992284 0.7493116 47.540783172 50.4880510
## theta[11,25] 53.08040281 0.6379974 51.800499972 54.3612962
## theta[12,25] 49.35995790 0.9962118 47.280706699 51.2104130
## theta[13,25] 53.81279839 0.6397024 52.549150874 55.0571361
  theta[1,26]
                51.30334615 0.7274597 49.783469255 52.6908757
## theta[2,26]
                51.68768837 0.6736291 50.319683513 52.9572432
## theta[3,26]
                50.18663880 0.9241264 48.220496878 51.9190495
                50.03165013 0.7154291 48.613211915 51.4404754
## theta[4,26]
## theta[5,26]
                53.65878561 0.6049121 52.451019327 54.8593777
               53.72229836 0.8659392 51.943319823 55.3027178
## theta[6,26]
                51.34486780 0.6646231 50.024499176 52.5951370
## theta[7,26]
## theta[8,26]
                55.74968598 1.1954532 53.472653880 58.0590768
                52.54259610 0.8000491 50.933185634 54.0862307
## theta[9,26]
## theta[10,26] 48.83145827 0.7439872 47.330261482 50.2689737
## theta[11,26] 52.94372350 0.6120789 51.724976883 54.1578159
## theta[12,26] 49.21451543 0.9985077 47.057903214 51.0582549
## theta[13,26] 53.67579246 0.6440269 52.383728618 54.9229273
## theta[1,27]
                51.15096686 0.6433392 49.869845835 52.3762317
## theta[2,27]
                51.59984763 0.6439745 50.313298213 52.8705117
                50.04519305 0.9589500 48.027698289 51.8698604
## theta[3,27]
## theta[4,27]
                49.98410126 0.7541695 48.546488680 51.4752329
## theta[5,27]
                53.60411870 0.6071403 52.391123471 54.7773593
                53.66436013 0.8781932 51.808116686 55.3280123
## theta[6,27]
## theta[7,27]
                51.25125812 0.6669697 49.935268304 52.5358359
                55.72066974 1.2300119 53.421287316 58.1121106
## theta[8,27]
                52.41509151 0.8811340 50.644009094 54.1199781
## theta[9,27]
## theta[10,27]
               48.77458837 0.6943184 47.425473712 50.1437613
               52.89745291 0.5896079 51.739154820 54.0279843
## theta[11,27]
## theta[12,27] 49.06111407 1.0258611 46.910637195 50.9315907
## theta[13,27] 53.61524142 0.6030163 52.420837107 54.7719620
## theta[1,28]
                51.58592893 0.6613052 50.256230310 52.8564184
## theta[2,28]
                52.04585132 0.6545400 50.729281018 53.3222539
## theta[3,28]
                50.08628226 0.9057033 48.202342057 51.8237698
                50.34553953 0.7922143 48.803749139 51.8649411
## theta[4,28]
## theta[5,28]
                53.94851511 0.6798402 52.610667707 55.2891873
```

```
## theta[6,28]
                53.96263550 0.9014140 52.124732724 55.6723647
## theta[7,28]
                51.45924120 0.6601458 50.077734945 52.7163394
## theta[8,28]
                56.03603983 1.2378751 53.711179855 58.4349618
## theta[9,28]
                52.80861199 0.9041043 51.007370201 54.6007682
## theta[10,28] 49.11545913 0.7573832 47.701069469 50.6470641
## theta[11,28] 53.27226758 0.6602086 51.941326511 54.5594181
## theta[12,28] 49.32046017 0.9387904 47.334997763 51.0306719
## theta[13,28] 53.88951071 0.6526881 52.560691867 55.1770280
## theta[1,29]
                52.22322249 0.6264435 50.981210414 53.4773714
## theta[2,29]
                52.65890907 0.5897252 51.547089357 53.8058728
## theta[3,29]
                50.42768623 0.9858849 48.333302752 52.3156312
## theta[4,29]
                50.84540803 0.7094199 49.472491130 52.2478043
## theta[5,29]
                54.44686290 0.5735584 53.319970061 55.5486545
## theta[6,29]
                54.39292631 0.7911120 52.727180410 55.9441025
## theta[7,29]
                51.86990440 0.5513575 50.780676472 52.9373930
## theta[8,29]
                56.44943094 1.1461029 54.376286451 58.6935179
                53.35544999 0.8252050 51.739670077 54.9061574
## theta[9,29]
## theta[10,29] 49.62735419 0.6885071 48.360237812 51.0597694
## theta[11,29] 53.78118469 0.5363878 52.698416189 54.8529506
## theta[12,29] 49.76024047 0.7683924 48.242832730 51.2726836
## theta[13,29] 54.27705639 0.5740015 53.195699275 55.4116700
## theta[1,30]
               52.64727177 0.7433386 51.199295826 54.1153575
## theta[2,30]
               53.15383955 0.6935834 51.891610096 54.5828750
## theta[3,30]
               50.70503461 1.1458564 48.353503146 52.9105192
                51.25345437 0.7880477 49.757027164 52.7854885
## theta[4,30]
## theta[5,30]
               54.84097756 0.6874067 53.546652515 56.2559251
## theta[6,30]
               54.72280050 0.8847973 52.869955533 56.3847105
                52.24042805 0.6373213 51.032060824 53.5541708
## theta[7,30]
## theta[8,30]
                56.75505494 1.1384601 54.634126436 59.0393985
## theta[9,30]
                53.74218640 1.0122812 51.763172102 55.7503530
## theta[10,30] 50.02243642 0.8135265 48.566018967 51.7846160
## theta[11,30] 54.19375571 0.5803321 53.113257565 55.3878168
## theta[12,30] 50.04030989 0.7981271 48.476853630 51.6101979
## theta[13,30] 54.50995485 0.6189449 53.308792755 55.7760587
## theta[1,31]
                52.03092844 0.7490287 50.551568255 53.5087478
## theta[2,31]
                52.33964401 0.5816285 51.191909288 53.4689035
## theta[3,31]
                50.31963513 1.1423758 48.000153569 52.5478586
## theta[4,31]
               50.62246742 0.8112316 49.062857969 52.2056301
## theta[5,31]
               54.18332502 0.6704906 52.892606419 55.5100804
               54.16046051 0.9160760 52.236857953 55.8708614
## theta[6,31]
## theta[7,31]
               51.64485145 0.6125461 50.449871348 52.8270283
                56.20049100 1.0754211 54.184845971 58.3233780
## theta[8,31]
                53.08504250 1.0219402 51.103632436 55.0978450
## theta[9,31]
## theta[10,31] 49.37983692 0.8046828 47.864969941 51.1170317
## theta[11,31] 53.52348174 0.5725324 52.418334920 54.6531141
## theta[12,31] 49.35222563 0.8616713 47.613761410 50.9788644
## theta[13,31] 53.97266133 0.5799285 52.846888653 55.1131743
## mean Rhat: 1.074029
## mean effective sample size: 460.9934
```

Since the outcome of the election is decided by Electoral College vote, for each set of MCMC samples of the

two-party vote share by state, we use the predicted winner in each state j on the day of the election  $(\beta_{j1})$  and sum the electoral votes from those states for each candidate. For states not in the model, votes were given to the candidates based on how the states voted in 2016. The probability of President Trump winning re-election is the probability that he receives 270 or more electoral votes across simulations. (Note: Maine and Nebraska do not have a "winner-take-all" framework for allocating votes, but for simplicity, we assume that they have the same vote-allocating procedures as the other states).

#### A.2 Senate Election Model

The purpose of the Senate model is to predict whether the U.S. Senate remains in Republican control (and to predict the outcome for the NC Senate race). The states included in the model are Alaska, Arizona, Colorado, Georgia, Iowa, Kansas, Maine, Michigan, Montana, North Carolina, South Carolina, and Texas. These states were chosen because they are deemed by political analysts as being competitive states for the Senate race in 2020. There is also a special election for the Senate in Georgia in addition to the regularly scheduled election. For the Georgia special election, our model sums up the support for Republican candidates and compares that to the sum of the support for Democratic candidates, and treats this election in the same way as the other states.

The response we will use is  $Y_k$ , the Democrat candidate's share of the two-party vote using the following model where the poll k (of K=fill in polls) ended t days (of T = 60 days) before the election and was conducted on state j (of J=14 states of interest).

```
Y_k \sim N(\beta_{jt}, \sigma_{yj}^2)
\beta_{jt} \sim N(\beta_{jt-1}, \sigma_{\beta_j}^2)
Priors for \sigma_{yj}^2: \sigma_{yj}^2 \sim InvGamma(\nu_u, \nu_y \tau_y)
\nu_y \sim Uniform(0, 100) \text{ and } \tau_y \sim Uniform(0, 100).
Priors for \sigma_{\beta_j}^2 \sigma_{\beta_j}^2 \sim InvGamma(\nu_\beta, \nu_\beta \tau_\beta))
\nu_\beta \sim Uniform(0, 100) \text{ and } \tau_\beta \sim Uniform(0, 100).
Priors for \beta_{j1} \beta_{j1} \sim N(\mu_j, \sigma^2)
\sigma^2 \sim InvGamma(0.5, 0.5)
\mu_j \sim N(h_j, 7.5^2)
h_j = \text{Vote Share from Partisan Lean}_j + \text{Incumbency Advantage}_j
```

A hierarchical model was used, where the Democratic candidate's share of the two-party vote for poll k on any given day t for state j is modeled as a normal distribution with mean  $\beta_{jt}$  and variance  $\sigma_{yj}^2$ . A random walk was used to calculate  $\beta_{jt}$  for each day t before the election (up until 30 days before the election) from  $\beta_{jt-1}$  and  $\sigma_{\beta j}$ . The mean  $h_j$  of the normal prior on  $mu_j$  (which is the mean of the normal prior on  $\beta_{j1}$ ), was calculated by the sum of the Vote Share from Partisan Lean<sub>j</sub> and Incumbency Advantage<sub>j</sub>. keep?

#### Raw Model Output

```
##
                                                2.5%
                                                          97.5%
                                      sd
## beta[1,1]
                   46.4507584 2.2433708 41.59965446 50.6435166
## beta[2,1]
                   52.3060134 2.1867985 46.72905116 55.6747117
## beta[3,1]
                   54.3407636 1.7697115 50.52703121 57.6127336
## beta[4,1]
                   48.6580340 1.6538193 45.60341428 51.9550692
## beta[5,1]
                   45.5772068 1.9532845 41.67556604 49.6975127
## beta[6,1]
                   50.7226677 1.6592584 47.18653081 53.7717883
## beta[7,1]
                   46.2249577 2.6063537 40.90148615 51.1973216
## beta[8,1]
                   52.0308945 2.2519892 47.08007333 55.9982111
## beta[9,1]
                   53.9554866 1.7664757 50.67107557 57.9060076
## beta[10,1]
                   47.5874120 2.0102568 43.45416459 51.5177091
## beta[11,1]
                   51.7831808 1.6530492 48.20280605 54.9907635
## beta[12,1]
                   48.8159096 1.9127126 45.15421200 52.8553178
```

```
## beta[13,1]
                   45.7833702 1.8480167 42.38430159 49.9298690
## beta[1,2]
                   46.4896459 2.2087097 41.73140473 50.7067420
## beta[2,2]
                   52.3289635 2.1332011 46.76305635 55.6280756
## beta[3,2]
                   54.3711092 1.7153990 50.70312546 57.5107585
## beta[4,2]
                   48.6820835 1.5900333 45.55906919 51.7720312
## beta[5,2]
                   45.5860786 1.8948276 41.78424188 49.4964545
## beta[6,2]
                   50.7492053 1.6070817 47.32136332 53.6024884
## beta[7,2]
                   46.2482261 2.5790858 40.95415039 51.1620338
## beta[8,2]
                   52.0342957 2.2127825 47.17982380 55.9353012
                   53.9700156 1.7005589 50.93251803 57.7808375
## beta[9,2]
## beta[10,2]
                   47.6105677 1.9664164 43.60635351 51.4052042
                   51.8087928 1.5742675 48.42741143 54.8897353
## beta[11,2]
## beta[12,2]
                   48.8315938 1.8713619 45.27158091 52.8845275
                   45.8203025 1.8035136 42.50382068 49.8369427
## beta[13,2]
                   46.4972722 2.1748183 41.79078922 50.6082250
## beta[1,3]
## beta[2,3]
                   52.3504019 2.0757404 46.89180959 55.5676551
## beta[3,3]
                   54.4025269 1.6743724 50.83741377 57.4734257
## beta[4,3]
                   48.7026871 1.5316694 45.66027082 51.6917491
## beta[5,3]
                   45.5939497 1.8587148 41.96836855 49.4744802
## beta[6,3]
                   50.7842206 1.5345155 47.56099990 53.5312636
## beta[7,3]
                   46.2874322 2.5704155 41.03692954 51.1878884
## beta[8,3]
                   52.0451801 2.1927681 47.31900495 56.0179210
## beta[9,3]
                   53.9616679 1.6422515 51.02280354 57.7440600
## beta[10,3]
                   47.6457081 1.9178816 43.67544160 51.3512848
                   51.8224261 1.5060512 48.57959501 54.7184358
## beta[11,3]
## beta[12,3]
                   48.8449458 1.8210090 45.44757736 52.9417926
## beta[13,3]
                   45.8366463 1.7529638 42.65491212 49.7247423
## beta[1,4]
                   46.5096325 2.1446964 41.93718701 50.5971583
## beta[2,4]
                   52.3811437 2.0084432 47.18445415 55.4559586
## beta[3,4]
                   54.4305865 1.6369488 51.02141715 57.4256656
## beta[4,4]
                   48.7264314 1.4754701 45.70538022 51.5413339
## beta[5,4]
                   45.5914780 1.8051970 42.05007872 49.3659552
## beta[6,4]
                   50.8000562 1.4696533 47.72206160 53.3727090
## beta[7,4]
                   46.3211874 2.5536161 41.19514273 51.1742377
                   52.0428598 2.1662293 47.43433726 55.9819806
## beta[8,4]
## beta[9,4]
                   53.9696348 1.5858942 51.09637291 57.6014267
## beta[10,4]
                   47.6724513 1.8668032 43.89282346 51.2309429
## beta[11,4]
                   51.8493091 1.4369846 48.83034407 54.6103632
## beta[12,4]
                   48.8576964 1.7708459 45.71742528 52.7111169
                   45.8545564 1.6860656 42.79886556 49.5855540
## beta[13,4]
## beta[1,5]
                   46.5270050 2.1184366 42.04091230 50.5605798
                   52.3960022 1.9357695 47.40427586 55.3663511
## beta[2,5]
## beta[3,5]
                   54.4590620 1.6011863 51.10509080 57.3259556
## beta[4,5]
                   48.7412904 1.4171168 45.81660090 51.4376954
## beta[5,5]
                   45.5938862 1.7675097 42.11294752 49.1187604
## beta[6,5]
                   50.8211279 1.4119876 47.90429088 53.3159518
## beta[7,5]
                   46.3494214 2.5448663 41.13449596 51.2228690
## beta[8,5]
                   52.0688027 2.1458932 47.40572776 55.9524187
## beta[9,5]
                   53.9749684 1.5443841 51.16636715 57.5088164
## beta[10,5]
                   47.7098359 1.8038902 43.97822741 51.1170287
## beta[11,5]
                   51.8806487 1.3733100 48.98335827 54.5870886
## beta[12,5]
                   48.8678520 1.7168686 45.75473610 52.6724863
```

```
## beta[13,5]
                   45.8739376 1.6433555 42.91525381 49.5902015
## beta[1,6]
                   46.5369181 2.0918170 42.30038580 50.5286182
## beta[2,6]
                   52.4209609 1.8622084 47.65261644 55.3620168
## beta[3,6]
                   54.4934255 1.5479439 51.22021999 57.3540242
## beta[4,6]
                   48.7565441 1.3599191 45.99376876 51.3513729
## beta[5,6]
                   45.5914292 1.7333413 42.14084013 49.1108980
## beta[6,6]
                   50.8723847 1.3477733 48.15517471 53.2286846
## beta[7,6]
                   46.3865869 2.5345902 41.11783543 51.2642474
## beta[8,6]
                   52.0944968 2.1202371 47.53904839 56.0144854
## beta[9,6]
                   53.9684720 1.4624460 51.34241802 57.3044058
## beta[10,6]
                   47.7515750 1.7459987 44.24095880 51.1506414
                   51.9025948 1.3072086 49.13922418 54.5755418
## beta[11,6]
## beta[12,6]
                   48.8775857 1.6746169 45.86563107 52.5292894
                   45.9026161 1.5877677 42.99714600 49.4096485
## beta[13,6]
## beta[1,7]
                   46.5517737 2.0788082 42.20078284 50.5648052
## beta[2,7]
                   52.4423884 1.8214850 47.83797315 55.2662000
## beta[3,7]
                   54.5344213 1.5061993 51.42066337 57.3478975
## beta[4,7]
                   48.7721559 1.3043131 46.11785442 51.2292675
## beta[5,7]
                   45.5929511 1.6707891 42.26243636 48.9654654
## beta[6,7]
                   50.9084257 1.2986088 48.29994155 53.1661204
## beta[7,7]
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## beta[8,7]
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## beta[9,7]
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## beta[12,7]
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## beta[2,8]
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## beta[3,8]
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## beta[5,8]
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## beta[6,8]
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## beta[7,8]
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## beta[9,8]
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## beta[10,8]
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## beta[13,8]
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## beta[2,9]
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## beta[3,9]
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## beta[9,9]
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## beta[10,9]
## beta[11,9]
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## beta[12,9]
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## beta[9,10]
## beta[10,10]
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## beta[12,10]
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## beta[2,11]
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## beta[6,11]
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## beta[3,12]
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## beta[9,12]
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## beta[12,12]
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## beta[10,13]
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## beta[11,13]
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## beta[12,13]
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## beta[2,14]
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## beta[3,14]
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## beta[7,14]
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## beta[9,14]
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## beta[10,14]
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## beta[12,14]
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## beta[3,15]
## beta[4,15]
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## beta[8,15]
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## beta[11,15]
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## beta[12,15]
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## beta[4,16]
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## beta[10,17]
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## beta[11,17]
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## beta[12,17]
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## beta[12,18]
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## beta[2,19]
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## beta[7,19]
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## beta[12,19]
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## beta[3,20]
## beta[4,20]
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## beta[10,21]
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## beta[12,21]
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## beta[6,22]
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## beta[12,22]
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## beta[8,26]
                   52.3537983 1.5436570 48.99796781 55.1439165
## beta[9,26]
                   53.2971362 0.6964640 51.88290091 54.6503765
## beta[10,26]
                   47.0431523 1.3533366 44.26502066 49.4627238
                   52.4467005 0.7354556 51.04320166 53.9862058
## beta[11,26]
## beta[12,26]
                   47.9046602 1.4283001 44.93686676 50.5560030
                   46.0984842 0.9448671 44.28554119 48.0987626
## beta[13,26]
## beta[1,27]
                   47.4618450 1.4700258 44.09461319 50.3972924
## beta[2,27]
                   53.6111881 0.7078093 52.24430199 54.9594438
                   55.2679870 0.9362267 53.37511242 57.1152185
## beta[3,27]
## beta[4,27]
                   48.6024534 0.9173805 46.74524389 50.3933464
## beta[5,27]
                   46.2016904 1.1621773 43.91817702 48.3829458
## beta[6,27]
                   51.8327335 0.9539375 49.97904837 53.7463876
                   46.7452836 2.7133898 41.29619052 52.0879452
## beta[7,27]
## beta[8,27]
                   52.3640944 1.4948538 49.20271106 55.1464839
## beta[9,27]
                   53.4495606 0.7081610 52.07726318 54.8664754
## beta[10,27]
                   46.9520061 1.3574939 44.08995442 49.4453710
## beta[11,27]
                   52.3771826 0.7578924 50.91932501 53.8852459
## beta[12,27]
                   47.9196206 1.5196270 44.77370048 50.7517371
                   46.1524774 0.9366134 44.33378084 48.0825628
## beta[13,27]
## beta[1,28]
                   47.5722609 1.4605450 44.23145966 50.4744615
## beta[2,28]
                   53.6942170 0.7224197 52.29598129 55.1091818
                   55.2672804 0.9914321 53.25603453 57.2040805
## beta[3,28]
## beta[4,28]
                   48.5022231 0.9164981 46.66678874 50.2971843
## beta[5,28]
                   46.0848688 1.1801998 43.82973407 48.3405981
## beta[6,28]
                   51.8413230 0.9615027 49.95065859 53.7982913
## beta[7,28]
                   46.7603785 2.7476268 41.24162876 52.2203267
## beta[8,28]
                   52.3590314 1.4207960 49.40816857 55.0015970
## beta[9,28]
                   53.6043712 0.7257379 52.16331887 55.0172231
## beta[10,28]
                   46.8523748 1.3631335 44.02617140 49.3986889
                   52.3068993 0.7784794 50.74224627 53.8319352
## beta[11,28]
## beta[12,28]
                   47.9131191 1.6167875 44.54409007 51.0062493
## beta[13,28]
                   46.1935809 0.9022764 44.56786932 48.1391365
## beta[1,29]
                   47.6848497 1.4344787 44.45177709 50.5091427
                   53.6673304 0.7679560 52.13265892 55.1472795
## beta[2,29]
## beta[3,29]
                   55.2585334 1.0287523 53.13190571 57.2435084
## beta[4,29]
                   48.3580718 0.9985588 46.30876496 50.2707486
## beta[5,29]
                   46.0312334 1.2366088 43.54426637 48.3755283
## beta[6,29]
                   51.8677925 0.9387419 50.03582876 53.7358149
## beta[7,29]
                   46.7554409 2.7807474 41.15111317 52.2648013
## beta[8,29]
                   52.3619139 1.3557810 49.48227192 54.8444986
## beta[9,29]
                   53.6382803 0.7852292 52.09806866 55.1898938
## beta[10,29]
                   46.8636525 1.4377624 43.83159561 49.6131254
## beta[11,29]
                   52.2322878 0.7727406 50.59331291 53.7419728
## beta[12,29]
                   47.9130771 1.7037495 44.21988677 50.9993214
```

```
## beta[13,29]
                   46.2489814 0.8655470 44.69269510 48.0894850
##
  beta[1,30]
                   47.7991288 1.4156141 44.69305877 50.5769502
## beta[2,30]
                   53.6506213 0.7774959 52.13880114 55.1265817
## beta[3,30]
                   55.2627770 1.1256573 53.01983584 57.3903348
##
  beta[4,30]
                   48.3550312 1.1031878 46.08211241 50.4331675
  beta[5,30]
                   46.0259933 1.3216892 43.37429385 48.5746496
## beta[6,30]
                   51.9194306 0.9743408 50.02526565 53.8536274
##
  beta[7,30]
                   46.7472582 2.8285276 41.14622590 52.2613860
##
  beta[8,30]
                   52.2579323 1.3622229 49.49011940 54.8201552
## beta[9,30]
                   53.6713997 0.8551522 52.03762314 55.4141234
##
  beta[10,30]
                   46.8650164 1.5038064 43.80688647 49.6510935
  beta[11,30]
                   52.1206822 0.8143506 50.38648947 53.6985330
##
##
  beta[12,30]
                   47.9236093 1.7686198 44.21213856 51.1759230
                   46.2149077 0.9222641 44.50317426 48.1660882
## beta[13,30]
## beta[1,31]
                   47.8996625 1.3788202 44.76095190 50.4355935
                   53.6912338 0.8528018 52.00973344 55.3179302
## beta[2,31]
## beta[3,31]
                   55.2785179 1.2092872 52.90852160 57.6307819
## beta[4,31]
                   48.3585808 1.2016861 45.86013835 50.6686478
## beta[5,31]
                   46.0219710 1.3913000 43.19006592 48.7444100
  beta[6,31]
                   51.9119956 1.0926269 49.75673560 54.1812027
##
## beta[7,31]
                   46.7432851 2.8569825 41.01971904 52.3066243
  beta[8,31]
                   52.1675439 1.3656409 49.40700955 54.7009520
  beta[9,31]
                   53.6930802 0.9112265 51.84999218 55.5205501
##
## beta[10,31]
                   46.8551461 1.5830819 43.61816394 49.7614292
## beta[11,31]
                   52.0090255 0.8341724 50.25811229 53.5760578
##
  beta[12,31]
                   47.9192727 1.8396770 43.94391158 51.3031586
  beta[13,31]
                   46.1789356 0.9681142 44.33602796 48.1880520
##
## sigma2_beta[1]
                    0.2174465 0.1709002
                                          0.03591539
                                                       0.6455778
  sigma2_beta[2]
                    0.2195665 0.1769982
                                          0.03763168
                                                       0.6657771
## sigma2_beta[3]
                    0.2117813 0.1594372
                                          0.03599774
                                                       0.6146854
## sigma2_beta[4]
                    0.2150078 0.1639863
                                          0.03653461
                                                       0.6168701
  sigma2_beta[5]
                    0.2248891 0.1892429
                                          0.03824851
                                                       0.6904631
  sigma2_beta[6]
                    0.2127312 0.1623794
                                          0.03671041
                                                      0.6352535
##
  sigma2_beta[7]
                    0.2177799 0.1719668
                                          0.03634232
                                                       0.6345328
  sigma2_beta[8]
                    0.2146970 0.1668502
                                          0.03705036
                                                      0.6189533
##
  sigma2_beta[9]
                    0.2103161 0.1587663
                                          0.03750246
                                                       0.6029883
  sigma2_beta[10]
                    0.2202669 0.1761017
                                          0.03688560
                                                       0.6480835
## sigma2_beta[11]
                    0.2111939 0.1591431
                                          0.03804373
                                                       0.5951090
  sigma2_beta[12]
                    0.2172667 0.1701173
                                          0.03499755
                                                       0.6603020
  sigma2_beta[13]
                    0.2134587 0.1636727
                                          0.03839452
                                                       0.6263231
  sigma2_y[1]
                    4.3393222 2.2137569
                                          2.06291739
                                                      8.9778112
##
                                                       6.2710692
  sigma2_y[2]
                    3.8692044 1.0191342
                                          2.27841397
##
  sigma2_y[3]
                    3.4111862 1.1556115
                                          1.48423175
                                                       6.0022095
  sigma2_y[4]
                    3.9842974 1.2215696
                                          2.22593396
                                                       6.8663237
## sigma2_y[5]
                    7.4445583 4.5573201
                                          3.38615960 20.3325823
  sigma2_y[6]
                    3.7518461 1.1728339
##
                                          1.95333042
                                                       6.6424013
  sigma2_y[7]
                    4.3641806 3.0370416
                                          1.89056380 10.3323020
  sigma2_y[8]
                    4.2269202 2.2465433
##
                                          1.94931827
                                                       8.4792981
## sigma2_y[9]
                    3.5124807 0.9368648
                                          1.89915246
                                                       5.5939477
  sigma2_y[10]
                    3.9496067 1.6799443
                                          1.69059348
                                                       7.7787986
## sigma2_y[11]
                    3.6043268 0.9004233
                                                      5.7642380
                                          2.11599421
## sigma2_y[12]
                    4.2285806 1.8916422
                                          1.99432151
                                                      8.2372830
```

```
## sigma2_y[13] 3.7806794 1.1815197 1.90567452 6.6652333
## mean Rhat: 1.095761
```

For predicting control of the U.S. Senate, if a 50/50 split is predicted, then the VP breaks the tie. In this case, we predict Democrat majority since our presidential model gives Biden a high chance of winning (and a Democrat VP will break the tie).

## A.3 House Election Model

# House Model Purpose and Structure

## mean effective sample size: 215.8395

The purpose of the House model is to predict which candidate in each of NC's 13 congressional districts will win in their respective elections.

The response we will use is  $Y_k$ , the Democrat candidate's share of the two-party vote using the following model where the poll k (of K=fill in polls) ended t days (of T = 60 days) before the election and was conducted on district j (where j is in districts  $1, \dots, 11, 13$  of North Carolina). For district 12, the vote share is coded as 100 because there is only one candidate, and she is a Democrat. Note that, due to the scarcity of poll responses for the NC House elections, we included all poll responses within 115 days of the election.

```
\begin{split} Y_k &\sim N(\beta_{jt}, \sigma_{yj}^2) \\ \beta_{jt} &\sim N(\beta_{jt-1}, \sigma_{\beta_j}^2) \\ \sigma_{yj}^2 &\sim InvGamma(\nu_u, \nu_y \tau_y) \\ \nu_y &\sim Uniform(0, 100) \text{ and } \tau_y \sim Uniform(0, 100). \\ \sigma_{\beta j}^2 &\sim InvGamma(\nu_\beta, \nu_\beta \tau_\beta)) \\ \nu_\beta &\sim Uniform(0, 100) \text{ and } \tau_\beta \sim Uniform(0, 100). \\ \beta_{j1} &\sim N(h_j, 7.5) \\ h_j &= 0.9 * \text{Vote Share from Partisan Lean}_j + 0.1 * \text{Expected Vote Share from Voter Turnout}_j \end{split}
```

A hierarchical model was used, where the Democratic candidate's share of the two-party vote for poll k on any given day t for district j is modelled as a normal distribution with mean  $\beta_{jt}$  and variance  $\sigma_{yj}^2$ . A random walk was used to calculate  $\beta_{jt}$  for each day t before the election (up until 30 days before the election) from  $\beta_{jt-1}$  and  $\sigma_{\beta j}$ . The mean  $h_j$  of the normal prior on  $mu_j$  is computed by multiplying Vote Share from Partisan Lean<sub>j</sub> by 0.9 and Expected Vote Share from Voter Turnout<sub>j</sub> by 0.1, then summing those two values. keep?

#### Interim Report Model

```
Vote_{i} \sim Binomial(n_{i}, \pi_{i}) logit(\pi_{i}) = \alpha_{0} + \Sigma_{j=1,2,3}\beta_{j} * I(Income_{i} = Income\ Category_{s}) + \Sigma_{j=5,6}\beta_{j} * I(Gender_{i} = Gender\ Category_{g}) +  \Sigma_{j=7,8}\beta_{j} * I(Race_{i} = Race\ Category_{r}) + \Sigma_{j=9,10,11}\beta_{j} * I(Age_{i} = Age\ Category_{a}) +  \Sigma_{j=12,13}\beta_{j} * I(Party_{i} = Party\ Category_{p}) +  \Sigma_{j=14,...,17}\beta_{j} * I(Gender_{i} = Gender\ Category_{g})I(Party_{i} = Party\ Category_{p}) +  \Sigma_{j=18,...,21}\beta_{j} * I(Race_{i} = Race\ Category_{r})I(Party_{i} = Party\ Category_{p}) +  \Sigma_{j=22,...,27}\beta_{j} * I(Gender_{i} = Gender\ Category_{g})I(Age_{i} = Age\ Category_{a}) +  \Sigma_{j=28,...,33}\beta_{j} * I(Party_{i} = Party\ Category_{p})I(Age_{i} = Age\ Category_{a})
```

where:

 $Income\ Category_s \in \{Median\ Income\ \$46864 - \$52798,\ Median\ Income\ \$52798 - \$64509,\ Median\ Income\ > \$6450$   $Gender\ Category_g \in \{Male, Unspecifie\ Race\ Category_r \in \{Black, Othe\ Age\ Category_a \in \{Age\ 30-44,\ Age\ 45-59,\ Age\ 60-Party\ Category_p \in \{Republican,\ Othe\ Age\ Category_p \in \{Republican,\ Othe\ Age\ Category_p \in \{Republican,\ Othe\ Cat$ 

Where  $\pi_i$  is the probability that subgroup i votes.  $Vote_i$  is the number of people in the ith subgroup that voted in the 2016 election. The baseline is Median Income < \$46864 for income, Female for gender, White for race, 18-29 for age, and Democrat for party affiliation.

We fit the voter turnout model from the Interim Report on the 2020 registered voter dataset. The predicted values were the number of people that will vote for each demographic subgroup in each congressional district. We made a reasonable assumption that if someone is registered as a Democrat, that they will indeed vote for the Democratic candidate (and made the same assumption for registered Republicans). If the demographic subgroup had third/unaffiliated party, then we split their predicted number of voters evenly between the Democrat and Republican parties. From this, we calculated Democratic party vote share for each district by taking the ratio of the predicted number of Democratic voters to total number of registered voters in that district.

# Raw Output for Appendix

##		mean	sd	2.5%	97.5%
##	beta[1,1]	58.306127	2.716740	52.977697539	63.675746
##	beta[2,1]	59.253823	2.777571	53.830873329	64.707466
##	beta[3,1]	36.385167	2.670935	31.436792575	41.684174
##	beta[4,1]	66.711295	2.729256	61.523445759	72.155486
##	beta[5,1]	30.463614	2.735714	25.070167216	35.796273
##	beta[6,1]	58.811408	2.742312	53.362761435	64.131692
##	beta[7,1]	38.194965	2.812420	32.566439603	43.595922
##	beta[8,1]	44.256514	2.564823	38.991609441	49.328885
##	beta[9,1]	43.211496	2.580971	38.101328337	48.597018
##	beta[10,1]	29.324002	2.730484	24.043756131	34.836887
##	beta[11,1]	43.880322	2.187492	39.408639848	48.139221
##	beta[12,1]	68.969534	2.744467	63.677429845	74.298244
##	beta[13,1]	30.396369	2.731562	24.989800885	35.883334
##	beta[1,2]	58.352260	3.040225	52.320255196	64.302066
##	beta[2,2]	59.267556	3.127547	53.209654701	65.536052
##	beta[3,2]	36.362939	3.021067	30.639348890	42.443572
##	beta[4,2]	66.670367	3.077007	60.774331456	72.879396
##	beta[5,2]	30.484026	3.009829	24.789901778	36.339399
##	beta[6,2]	58.837266	3.089096	52.785350981	64.904593
##	beta[7,2]	38.250039	3.142514	32.211870346	44.520885
##	beta[8,2]	44.391225	2.886468	38.351914439	50.094210
##	beta[9,2]	43.362126	2.858532	37.344276524	49.189518
##	beta[10,2]	29.309636	3.026344	23.355513128	35.415154
##	beta[11,2]	44.172316	2.432975	39.122144150	48.877901
##	beta[12,2]	68.944352	3.063979	62.817791974	75.036508
##	beta[13,2]	30.438862	3.056301	24.270146352	36.417821
##	beta[1,3]	58.368669		51.870150051	65.069312
##	beta[2,3]	59.276091	3.526879	52.585839537	66.302592
##	beta[3,3]	36.311190	3.348195	29.895473390	43.097538

##	beta[4,3]	66.643560	3.379636	59.891919751	73.405557
##	beta[5,3]	30.509747	3.382913	23.975655355	37.144857
##	beta[6,3]	58.835481	3.416625	52.333112910	65.587899
##	beta[7,3]	38.270992	3.489868	31.412035147	45.103616
##	beta[8,3]	44.527720	3.128332	37.845925520	50.696095
##	beta[9,3]	43.556225	3.070066	37.057456871	49.830085
##	beta[10,3]	29.268348	3.338790	22.691576703	36.030820
##	beta[11,3]	44.449054	2.628877	39.078423450	49.665543
##	beta[12,3]	68.965937	3.371608	62.124234052	75.664384
	beta[13,3]	30.413120	3.372929	23.691910985	37.108805
##	beta[1,4]	58.365505	3.632878	51.204359548	65.601744
##	beta[2,4]	59.247331	3.801727	51.932215509	66.917361
	beta[3,4]	36.324428		29.518788188	43.596500
	beta[4,4]	66.643179	3.638378	59.100184032	73.824224
##		30.524889		23.559421377	37.711960
	beta[6,4]	58.827705		51.710010972	65.968050
	beta[7,4]	38.288599		31.153627517	45.668316
##	beta[8,4]	44.679465		37.482810933	51.309609
	beta[9,4]	43.751912		36.798965705	50.308274
	beta[10,4]	29.255932		22.086106219	36.447439
	beta[11,4]	44.764004		39.063448015	50.837896
	beta[12,4]	68.929958		61.456805864	76.261149
	beta[13,4]	30.387894		23.327469316	37.687980
	beta[1,5]	58.338204		50.811769371	65.923478
##	beta[2,5]	59.304872		51.184248393	67.420540
##	beta[3,5]	36.328763		28.770960718	43.989578
	beta[4,5]	66.607566		58.584637237	74.066816
	beta[5,5]	30.536652		23.111815665	38.045611
	beta[6,5]	58.801986		51.305185383	66.367658
##		38.303831		30.444724652	46.468960
	beta[8,5]	44.773397		37.028889643	51.641192
	beta[9,5]	43.976716		36.669634874	51.004485
	beta[10,5]	29.244137		21.102460081	37.069445
	beta[11,5]	45.018522		38.894429749	51.740404
	beta[12,5]	68.949205		60.863494047	76.536290
	beta[13,5]	30.420340		22.998457762	38.371319
	beta[1,6]	58.304867		50.187979967	66.708488
##		59.298593		51.048209626	67.985691
	beta[3,6]	36.296599		28.526117351	44.655085
	beta[4,6]	66.611332		58.438574939	74.625763
	beta[5,6]	30.540835		22.771174840	38.650854
	beta[6,6]	58.798035		50.655577589	67.076381
	beta[7,6]	38.278691		29.909428996	46.882767
	beta[8,6]	44.859569		36.777941715	52.028967
	beta[9,6]	44.177958		36.320956602	51.437296
	beta[10,6]	29.234336		20.191063565	37.803459
	beta[11,6]	45.344910		39.247710483	52.329855
	beta[12,6]	68.955890		60.000992617	77.507457
	beta[12,6] beta[13,6]	30.437395		22.633896225	38.840688
	beta[1,7]	58.260632		49.709411964	66.726407
	beta[2,7]	59.296329		50.649496907	68.289360
	beta[2,7] beta[3,7]	36.290133		27.648299375	44.901723
пπ	2004[0,1]	55.255100	1.000120	21.010200010	11.001120

	beta[4,7]	66.587814		58.055145300	74.968408
	beta[5,7]	30.550488		21.970548559	39.483955
	beta[6,7]	58.785063		50.054345089	67.709637
	beta[7,7]	38.232816		29.557921255	47.813748
	beta[8,7]	45.012496		36.749567232	52.526230
	beta[9,7]	44.386974		35.800904827	51.635625
	beta[10,7]	29.210670		19.810118586	38.031075
	beta[11,7]	45.643531		39.595918578	52.994591
	beta[12,7]	68.881387		59.847795152	77.936175
##	beta[13,7]	30.427835		21.856797765	39.307411
##	beta[1,8]	58.268414		49.406168860	67.277460
	beta[2,8]	59.289803		49.959924066	69.108799
	beta[3,8]	36.292499		27.042237016	45.811325
##	beta[4,8]	66.587719		57.369607330	75.431523
##	- / -	30.536804		20.920941442	39.485781
	beta[6,8]	58.820231		49.813537225	68.160952
##	beta[7,8]	38.252243		29.162048851	48.192117
##	beta[8,8]	45.170439	3.882223	36.650085483	53.032581
	beta[9,8]	44.573776	3.851951	36.114132518	52.188508
##	beta[10,8]	29.236626	4.584843	19.645196332	38.439721
##	beta[11,8]	45.918617	3.534732	39.925660440	54.117024
##	beta[12,8]	68.925147	4.622607	59.228405231	78.340733
##	beta[13,8]	30.458401	4.556214	21.540221068	40.207513
##	beta[1,9]	58.227481	4.705658	48.827534270	67.469793
##	beta[2,9]	59.300895	4.902999	49.486445285	68.985516
##	beta[3,9]	36.300910	4.859348	26.559610569	46.483395
##	beta[4,9]	66.595457	4.741732	56.713108738	76.074615
##	beta[5,9]	30.514089	4.885376	20.698788360	40.394455
##	beta[6,9]	58.815551	4.893609	49.066195290	68.597732
##	beta[7,9]	38.219263	4.860930	29.018163419	48.782226
##	beta[8,9]	45.337447	4.021454	36.231640253	53.609536
##	beta[9,9]	44.811520	3.851604	36.438462750	52.170171
##	beta[10,9]	29.238296	4.809784	19.195282646	38.955400
##	beta[11,9]	46.232525	3.600083	40.118419854	54.684602
##	beta[12,9]	68.932522	4.855149	58.768413473	78.859970
##	beta[13,9]	30.448421	4.741623	21.260496585	40.199192
##	beta[1,10]	58.247449	4.972730	48.729943726	68.096116
##	beta[2,10]	59.271930	5.101482	49.054202063	69.489015
##	beta[3,10]	36.288553	5.062371	26.103773020	46.527697
##	beta[4,10]	66.613195	5.029024	55.863463490	77.038381
##	beta[5,10]	30.529794	5.336355	20.587857122	40.700657
##	beta[6,10]	58.820469	5.103717	48.872829775	69.218663
##	beta[7,10]	38.203178	5.053553	28.439100941	48.950892
##	beta[8,10]	45.505679	4.107839	36.658987968	54.134671
##	beta[9,10]	45.013589	3.916728	36.868484116	52.509908
##	beta[10,10]	29.230443	4.927455	18.593361748	38.984593
##	beta[11,10]	46.492548	3.656128	40.393340003	55.071663
##	beta[12,10]	68.973765	5.087724	58.200282340	79.389829
##	beta[13,10]	30.435523	4.949181	20.576660287	40.537013
##	beta[1,11]	58.266623	5.150298	47.914787416	68.444945
##	beta[2,11]	59.261359		48.660363549	70.413664
##	beta[3,11]	36.290370	5.306424	25.568221934	46.688181

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	beta[4,11]	66.608036		55.543123369	76.979618
	beta[5,11]	30.567121		20.332275024	40.832868
##	beta[6,11]	58.783717		48.383420142	69.777938
##	beta[7,11]	38.163950		27.768373582	49.661997
	beta[8,11]	45.631587	4.169952	36.246264533	54.293494
##	beta[9,11]	45.259294	3.992133	37.023478633	53.159288
##	beta[10,11]	29.197206	5.155472	18.512118346	39.628136
##	beta[11,11]	46.792953	3.766233	40.804479041	55.857930
##	beta[12,11]	68.962130	5.267353	57.936207098	80.052020
##	beta[13,11]	30.415973	5.158791	20.418780079	40.832706
##	beta[1,12]	58.302510	5.318072	47.413902113	68.966592
##	beta[2,12]	59.254457	5.585898	48.007494430	70.723173
##	beta[3,12]	36.339969	5.544313	25.012205351	47.060490
##	beta[4,12]	66.627207	5.403722	55.412321982	77.221734
##	beta[5,12]	30.557454	5.570089	19.567388996	41.269077
##	beta[6,12]	58.769380	5.549584	47.746141566	70.927868
##	beta[7,12]	38.166790	5.430003	27.333278172	49.773512
	beta[8,12]	45.783401	4.210739	36.437352864	54.277444
##	beta[9,12]	45.508003	4.035619	37.326282803	53.433867
##	beta[10,12]	29.166221	5.344817	18.173942715	39.838540
##	beta[11,12]	47.065534	3.793021	41.070979469	56.422165
	beta[12,12]	68.972807	5.379676	57.898251724	80.041023
	beta[13,12]	30.449992	5.372069	19.841436368	41.483756
	beta[1,13]	58.262313	5.470788	46.995975079	69.220810
	beta[2,13]	59.234750	5.773217	47.389997901	71.195490
##	beta[3,13]	36.337262	5.687907	24.650370831	47.574810
##	beta[4,13]	66.681401	5.595423	54.717485504	77.793053
##	beta[5,13]	30.571042	5.675612	18.524365707	41.905032
##	beta[6,13]	58.766203	5.708592	47.507514407	70.808711
	beta[7,13]	38.154545	5.642853	26.812866801	50.231639
##	beta[8,13]	45.946299	4.255413	36.752409829	54.615902
	beta[9,13]	45.740808	4.017914	37.658940787	53.461500
	beta[10,13]	29.180726		17.687237104	40.514079
	beta[11,13]	47.335563	3.862901	41.262953767	56.209493
	beta[12,13]	68.959719		57.312723831	80.479439
	beta[13,13]	30.421329	5.540451	19.387162344	41.702633
	beta[1,14]	58.301873		46.772466916	69.775547
	beta[2,14]	59.256256	5.875500	47.116404303	71.167237
##	beta[3,14]	36.321832		24.440119288	47.524982
	beta[4,14]	66.664215		54.466354809	78.439103
	beta[5,14]	30.584811		18.677108888	42.366872
	beta[6,14]	58.786263	5.882636	46.692209525	71.088970
	beta[7,14]	38.155730		26.623484389	50.353594
	beta[8,14]	46.065682		36.994539345	55.070331
	beta[9,14]	45.967892		38.607971485	53.715757
	beta[10,14]	29.178485		17.281554521	41.122449
##	beta[11,14]	47.624024		41.512498814	56.677932
	beta[12,14]	68.946208		56.821399985	80.522566
	beta[13,14]	30.397295		19.325979259	41.994068
	beta[1,15]	58.338386		46.809363654	70.520053
	beta[2,15]	59.267685		46.820573422	71.862300
	beta[3,15]	36.324546		24.029639291	48.310091
			2.300021		

	beta[4,15]	66.652767	5.893977	53.977288833	78.749912
##	beta[5,15]	30.562379	5.967742	17.874243540	42.629890
##	beta[6,15]	58.771929	5.988793	46.153458767	71.306672
##	beta[7,15]	38.148955	5.947232	26.109563892	50.253487
##	beta[8,15]	46.171479	4.323291	36.802827741	55.095160
##	beta[9,15]	46.157744	4.125107	38.508443584	54.359149
##	beta[10,15]	29.197460	5.843681	17.000430591	41.134019
##	beta[11,15]	47.927912	3.905768	41.786060481	56.732997
##	beta[12,15]	68.943342	5.970391	56.365425554	80.908491
	beta[13,15]	30.339386	5.851190	18.255294150	42.375917
##	beta[1,16]	58.336171	6.020326	45.998982492	71.063162
##	beta[2,16]	59.285772	6.080984	47.306352062	72.365226
	beta[3,16]	36.318764	6.268369	23.478254023	48.889813
	beta[4,16]	66.611462	6.068660	53.806954659	79.289792
	beta[5,16]	30.598517	6.381035	17.291937897	43.244396
	beta[6,16]	58.755407	6.164153	46.238480893	71.749485
	beta[7,16]	38.117870	6.125044	26.140244127	50.603916
	beta[8,16]	46.307109		37.058711739	55.486353
	beta[9,16]	46.349035		38.477622404	54.326619
	beta[10,16]	29.183833	6.025569	15.892613625	41.596688
	beta[11,16]	48.233554	3.989519	41.852107165	56.849217
	beta[12,16]	68.966861		56.060643175	81.237433
	beta[13,16]	30.342432		18.207775029	42.661679
	beta[1,17]	58.321885		45.735560302	71.086734
##	beta[2,17]	59.277326		46.436573437	72.419428
##	beta[3,17]	36.322355		22.724240017	49.132843
##	beta[4,17]	66.647102		53.352299422	78.970055
	beta[5,17]	30.614980	6.461924	16.467270534	43.295403
	beta[6,17]	58.753352	6.341515	45.959687652	72.076108
	beta[7,17]	38.128562	6.295447	25.498031197	50.544361
	beta[8,17]	46.443068	4.308399	37.910732732	55.805522
	beta[9,17]	46.528473	4.091345	38.567649964	54.672241
	beta[10,17]	29.150410	6.280176	15.540721166	42.205867
	beta[11,17]	48.514818	3.997312	42.317656921	56.910574
	beta[12,17]	68.975130	6.289467	55.886608126	81.612148
	beta[13,17]	30.305449	6.211051	17.864343045	43.255705
	beta[1,18]	58.306574	6.348285	45.470567881	70.878594
##		59.268614	6.502635	45.688482924	72.741568
##	beta[3,18]	36.322982	6.643092	22.464560254	49.742693
	beta[4,18]	66.630158		52.954368029	79.301547
	beta[5,18]	30.634613	6.599235	16.839208491	43.901412
	beta[6,18]	58.836614	6.502314	45.957680319	72.923843
	beta[7,18]	38.132090	6.409905	25.235019125	50.910532
	beta[8,18]	46.544646	4.300672	38.174085608	55.803514
	beta[9,18]	46.747231	4.170000	39.175698347	55.130454
	beta[10,18]	29.165170		15.358244357	42.315736
	beta[11,18]	48.669777		42.192984959	58.346601
	beta[12,18]	68.954676		55.553014150	81.849917
	beta[13,18]	30.287081		17.509148367	43.407955
	beta[1,19]	58.317593		45.184238176	71.461042
	beta[2,19]	59.261916		45.869593571	73.014204
	beta[3,19]	36.309328		22.138946429	49.995614
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	beta[4,19]	66.618513	6.610978	52.565389495	79.545391
##	beta[5,19]	30.637351	6.769377	16.736999562	43.598655
##	beta[6,19]	58.899817	6.710655	45.392925886	73.139528
##	beta[7,19]	38.147194	6.531765	25.102000748	50.886627
##	beta[8,19]	46.643279	4.303104	38.414612893	56.288110
##	beta[9,19]	46.945444	4.146384	39.448491536	55.268373
##	beta[10,19]	29.171655	6.624807	14.916578822	42.486671
##	beta[11,19]	48.807238	4.395896	42.300357935	59.218277
##	beta[12,19]	68.914446	6.623577	54.334482328	81.901753
##	beta[13,19]	30.258996	6.527071	17.231882583	43.309585
##	beta[1,20]	58.384975	6.629628	45.184399152	72.558088
##	beta[2,20]	59.262215	6.814608	45.546585146	73.152117
##	beta[3,20]	36.329758	6.939561	21.656203568	50.302140
##	beta[4,20]	66.599803	6.796110	52.160772009	80.203364
##	beta[5,20]	30.621707	6.867378	16.535627750	44.618199
##	beta[6,20]	58.843324	6.814834	45.077492033	73.329814
##	beta[7,20]	38.150904	6.613662	24.365897975	51.139155
##	beta[8,20]	46.801834	4.223229	38.828148397	55.990622
##	beta[9,20]	47.139525	4.155936	39.719027087	55.747196
##	beta[10,20]	29.165116	6.708796	14.798461824	42.528742
##	beta[11,20]	48.953740	4.567724	42.088507479	59.896537
##	beta[12,20]	68.932992	6.755592	54.376634353	82.577678
##	beta[13,20]	30.239741	6.746749	16.863660637	43.761707
##	beta[1,21]	58.333028	6.823553	44.745900753	73.257284
##	beta[2,21]	59.277259	6.900809	44.862863959	73.239429
##	beta[3,21]	36.338224	7.106053	21.382581325	50.741968
##	beta[4,21]	66.618064	6.913746	52.232482411	80.653652
##	beta[5,21]	30.622130	6.982153	16.631665016	44.548853
##	beta[6,21]	58.787358	7.062388	44.782995340	73.652071
##	beta[7,21]	38.123990	6.832153	24.532088954	51.516649
##	beta[8,21]	46.948894	4.219319	38.977576236	55.886760
##	beta[9,21]	47.362618	4.201026	39.939018308	56.273426
##	beta[10,21]	29.154332	6.881683	14.575735504	43.223389
##	beta[11,21]	49.027885	4.711607	41.857931032	60.606829
##	beta[12,21]	68.911713	6.893027	54.036193279	82.982557
##	beta[13,21]	30.173366	7.019513	16.517150409	44.207430
##	beta[1,22]	58.379061	6.911633	44.840159036	73.412273
##	beta[2,22]	59.301829	7.086533	44.849758762	74.169925
##	beta[3,22]	36.334380	7.252386	20.908706664	50.910205
##	beta[4,22]	66.658360	7.109628	52.255798392	81.190738
##	beta[5,22]	30.669940	6.985330	16.059923887	44.707825
##	beta[6,22]	58.778950	7.239992	44.404180745	74.098098
##	beta[7,22]	38.142335	7.000180	24.102572084	51.911347
##	beta[8,22]	47.111675	4.149624	39.196836491	55.741875
##	beta[9,22]	47.603159	4.265260	40.614446872	56.875426
	beta[10,22]	29.132797	7.100869	14.316880108	43.495748
	beta[11,22]	49.128431	4.882646	41.976107304	61.152214
	beta[12,22]	68.932881	7.068263	54.207193517	82.832962
	beta[13,22]	30.166614		15.671189128	44.467775
	beta[1,23]	58.351089		44.868240496	74.288377
	beta[2,23]	59.288893		44.676707287	74.032352
	beta[3,23]	36.310744		21.193100408	50.997657
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##	beta[4,23]	66.711161		51.889429279	81.337818
##	beta[5,23]	30.641085		15.413448042	44.719305
##	beta[6,23]	58.799939		44.031787435	74.778473
	beta[7,23]	38.098832		23.954320030	52.044849
	beta[8,23]	47.307544		39.502083029	56.313161
	beta[9,23]	47.790716	4.298330	40.322991956	56.888825
	beta[10,23]	29.119000	7.159204	13.544456447	43.218340
	beta[11,23]	49.212014		41.892056284	61.738726
##	beta[12,23]	68.935403	7.174223	54.031189201	83.249761
##	beta[13,23]	30.115630	7.334874	14.515217728	44.475752
##	beta[1,24]	58.336031		43.923917841	73.272731
	beta[2,24]	59.270694	7.295185	44.419761293	74.227630
	beta[3,24]	36.314991	7.440503	20.997475824	51.450585
	beta[4,24]	66.708827	7.373735	51.476692114	81.649857
	beta[5,24]	30.685977	7.431120	15.430687298	45.368144
	beta[6,24]	58.812885		43.492548274	75.069349
##	beta[7,24]	38.055070		23.139100328	52.620093
##	beta[8,24]	47.527704	4.090125	39.811023449	56.178769
##	beta[9,24]	47.954563		40.438208619	57.221168
	beta[10,24]	29.142509	7.290425	13.803735115	43.611149
##	beta[11,24]	49.245636	5.132736	41.545158973	62.085743
##	beta[12,24]	68.990411	7.294981	54.268737105	83.550418
##	beta[13,24]	30.140435		14.293596367	44.936380
##	beta[1,25]	58.359116	7.329318	43.605945472	74.203684
##	beta[2,25]	59.271064	7.500391	44.006202915	74.728816
##	beta[3,25]	36.334136	7.633326	20.440892035	51.878908
	beta[4,25]	66.700430	7.444504	50.970011594	81.687284
##	beta[5,25]	30.689227	7.655568	15.219242366	46.221770
##	beta[6,25]	58.813084	7.574588	43.722227739	74.929812
##	beta[7,25]	38.080828	7.470243	22.681492650	52.842327
##	beta[8,25]	47.713083		40.433527135	56.775155
	beta[9,25]	48.079428	4.352540	40.457255275	57.418738
##	beta[10,25]	29.130557	7.429949	13.506115896	44.280967
	beta[11,25]	49.290853		41.667173561	62.025878
	beta[12,25]	68.966794	7.383241	53.811914763	84.126075
	beta[13,25]	30.160118	7.595330	14.092971878	45.275305
##	beta[1,26]	58.360611		43.205607838	74.028565
##	beta[2,26]	59.232147		43.765551891	74.685200
	beta[3,26]	36.314586	7.797782	20.101718783	52.162711
	beta[4,26]	66.685476	7.643953	50.722188456	82.136138
##	beta[5,26]	30.680942	7.977261	14.898505814	46.489211
	beta[6,26]	58.787844	7.684557	43.414280882	75.071718
	beta[7,26]	38.114291	7.589911	22.239582752	53.103183
	beta[8,26]	47.895263		40.882362570	56.815278
##	beta[9,26]	48.260340		40.732152402	57.445194
##	beta[10,26]	29.124755		12.881415916	44.244382
	beta[11,26]	49.408161	5.408229	41.771690631	62.720774
##	beta[12,26]	68.948972		53.463921133	84.132349
##	beta[13,26]	30.133584		13.776098867	45.385171
	beta[1,27]	58.352661		43.384365724	74.126017
	beta[2,27]	59.213533		43.320253250	75.383021
##	beta[3,27]	36.327205	7.919219	19.929613001	52.171283

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	beta[4,27]	66.702326		50.515620001	82.360221
	beta[5,27]	30.664580		13.989054365	46.819722
	beta[6,27]	58.781013		42.957864910	75.284220
##	beta[7,27]	38.154901		22.025412803	53.359401
	beta[8,27]	48.059529		41.404372109	56.688012
	beta[9,27]	48.381731		41.169647913	57.342771
##	beta[10,27]	29.120428	7.686989	12.719665265	44.763436
	beta[11,27]	49.461466		41.822762660	63.932493
##	beta[12,27]	68.968277	7.675911	53.083295671	84.497324
##	beta[13,27]	30.109131	7.836403	13.845008502	45.501562
##	beta[1,28]	58.388813	7.749344	43.126231736	74.114999
##	beta[2,28]	59.221344	7.886189	43.094458205	75.254985
##	beta[3,28]	36.325693	8.130292	19.330446330	52.314718
##	beta[4,28]	66.704719	7.907875	49.217919743	82.686228
##	beta[5,28]	30.647430	7.878266	13.348651640	46.757838
##	beta[6,28]	58.770549	7.953038	42.896862188	75.768467
##	beta[7,28]	38.176783	7.859607	22.124564158	53.623693
##	beta[8,28]	48.180134	3.536938	42.151152631	56.040795
##	beta[9,28]	48.543158	4.354064	41.426635951	57.451410
##	beta[10,28]	29.076100	7.784649	12.518390421	45.048406
##	beta[11,28]	49.538702	5.573821	41.729774462	64.569799
##	beta[12,28]	69.016248	7.725038	53.192741102	85.110034
##	beta[13,28]	30.112135	7.955354	13.758173225	45.728022
##	beta[1,29]	58.388375	7.895937	42.912426552	74.772536
##	beta[2,29]	59.209923	8.037368	42.330713311	75.337637
##	beta[3,29]	36.329592	8.136441	19.091861127	52.356614
##	beta[4,29]	66.693147	8.056034	49.686300795	82.997463
##	beta[5,29]	30.661621	8.051739	13.586113546	47.113767
##	beta[6,29]	58.786726	8.042698	42.789835667	75.772358
##	beta[7,29]	38.121583	8.011942	22.261782318	53.609690
##	beta[8,29]	48.374186	3.343004	42.666469128	55.689562
##	beta[9,29]	48.675968	4.291979	41.636738451	57.494187
##	beta[10,29]	29.076926	7.940232	12.168736672	45.255600
##	beta[11,29]	49.619604	5.729946	41.795605221	65.059051
##	beta[12,29]	69.006914	7.903579	53.233256734	85.516148
##	beta[13,29]	30.113794	8.038976	13.931821996	46.138378
##	beta[1,30]	58.405280	7.985358	42.409859745	75.375195
##	beta[2,30]	59.190132	8.121986	42.414946881	75.714370
##	beta[3,30]	36.324500	8.257989	18.505170231	52.519473
##	beta[4,30]	66.717932	8.279229	48.587751944	83.738281
##	beta[5,30]	30.665387	8.125884	13.108117849	47.456315
##	beta[6,30]	58.809266	8.241909	42.766113711	76.314390
##	beta[7,30]	38.136258	8.113950	21.605238611	53.838367
##	beta[8,30]	48.374920	3.469840	42.472431181	56.262291
##	beta[9,30]	48.858458	4.321865	41.742379798	57.650443
##	beta[10,30]	29.068039	8.061060	11.651731872	45.545969
##	beta[11,30]	49.676875	5.836066	41.725145417	65.500220
##	beta[12,30]	68.984087	8.023210	52.746320250	85.452682
##	beta[13,30]	30.099370	8.099412	13.371774534	45.976690
##	beta[1,31]	58.405322	8.141417	42.219517033	75.767319
##	beta[2,31]	59.202163	8.240867	41.428756071	76.259253
##	beta[3,31]	36.330624	8.318322	18.474305923	52.465169

##	beta[4,31]	66.767165	8.409721	48.561604539	84.166468
##	beta[5,31]	30.715365		12.896407598	48.113251
##	beta[6,31]	58.770578		42.180950777	75.876092
	beta[7,31]	38.141041	8.281447	20.753533164	54.228917
	beta[8,31]	48.352146	3.591761	42.522402831	56.547823
##	beta[9,31]	48.978578	4.344048	41.827528315	57.965734
##	beta[10,31]	29.087480	8.203606	11.815270435	45.626210
##	beta[11,31]	49.766943	5.867911	41.699531137	65.662993
##	beta[12,31]	69.001572	8.110464	52.811669334	85.757175
##	beta[13,31]	30.043771	8.164211	12.790561647	45.798382
##	beta[1,32]	58.397283	8.327742	41.754774571	75.982748
##	beta[2,32]	59.246670	8.354888	41.310874283	76.355037
##	beta[3,32]	36.379510	8.494378	18.216258228	53.359564
##	beta[4,32]	66.717809	8.491812	48.188657130	84.293506
##	beta[5,32]	30.691713	8.319938	12.536224390	47.799236
##	beta[6,32]	58.749662	8.442745	42.234912385	76.185943
##	beta[7,32]	38.171561	8.363757	21.210772986	54.146962
##	beta[8,32]	48.337925	3.652381	42.018881707	57.012004
##	beta[9,32]	49.197333	4.253861	42.081565198	57.846987
##	beta[10,32]	29.101255	8.323924	11.581156230	46.233340
##	beta[11,32]	49.760127	5.910531	41.478098841	66.011081
##	beta[12,32]	69.002466	8.346700	52.206337790	86.132964
##	beta[13,32]	30.057511	8.293582	12.521668364	46.299268
##	beta[1,33]	58.363050	8.515607	41.803872189	76.780161
##	beta[2,33]	59.259829	8.510742	40.988121226	77.221818
##	beta[3,33]	36.357808	8.639713	17.787882918	53.958855
##	beta[4,33]	66.702033	8.650870	48.669019007	84.441895
##	beta[5,33]	30.690800	8.508055	12.309171787	48.083626
##	beta[6,33]	58.738126	8.479283	42.122644404	75.922231
##	beta[7,33]	38.188739	8.564912	20.622662113	54.501034
##	beta[8,33]	48.336329	3.620403	42.115415592	56.800534
##	beta[9,33]	49.385765	4.251209	42.021157236	57.793415
##	beta[10,33]	29.129031	8.438221	10.715903408	46.283507
##	beta[11,33]	49.782489	5.897437	41.199014102	65.772357
##	beta[12,33]	69.015222	8.476621	51.883178649	86.552070
##	beta[13,33]	30.056081	8.435342	11.935030707	46.595457
##	beta[1,34]	58.337080	8.585368	41.250944281	76.227461
##	beta[2,34]	59.240301	8.626346	41.114094045	77.206329
##	beta[3,34]	36.337712	8.749139	17.777673824	54.126746
##	beta[4,34]	66.733223	8.718471	49.012065320	84.902938
##	beta[5,34]	30.696055	8.617647	11.972031662	48.263148
##	beta[6,34]	58.690203	8.601654	41.788576846	77.036900
##	beta[7,34]	38.152323	8.823461	20.538360018	54.864974
##	beta[8,34]	48.327681	3.661307	41.724390849	56.810018
##	beta[9,34]	49.386044	4.491684	41.855367443	58.049463
##	beta[10,34]	29.116853	8.587442	10.510940846	46.748104
##	beta[11,34]	49.753827		41.100226162	65.096384
	beta[12,34]	69.021027		51.688666137	87.282493
##	beta[13,34]	30.038949		11.542266387	46.922635
##	beta[1,35]	58.301167		41.391949657	76.495223
	beta[2,35]	59.239932		40.114102584	77.601488
##	beta[3,35]	36.375970		17.820692170	54.768484
	- · -				

##	beta[4,35]	66.707187	0 770527	49.030541861	85.027266
		30.738280		12.272459321	
	beta[5,35] beta[6,35]	58.691741		41.421417352	48.876473 77.411867
##					
##	beta[7,35]	38.179575		20.402896140	55.122419
	beta[8,35]	48.326164		42.098410192	56.683027
	beta[9,35]	49.385504		41.464022839	58.689330
	beta[10,35]	29.089098		10.685081980	46.845660
##	, , , , ,	49.734665		41.148496195	64.073444
	beta[12,35]	68.956366		50.967050708	87.263363
##	beta[13,35]	29.994411	8.704314	11.022609108	47.259752
##	beta[1,36]	58.322351	8.786967	40.933249212	76.883964
##	beta[2,36]	59.270942	9.032085	39.860439848	78.529761
##	beta[3,36]	36.362008	9.088661	17.601532312	55.174064
##	beta[4,36]	66.752500	8.920629	48.845998864	85.994887
##	beta[5,36]	30.764507	8.803632	12.629435694	49.131105
##	beta[6,36]	58.702858	8.836718	40.971385361	77.716841
##	beta[7,36]	38.163203	9.002164	20.205639274	55.511474
##	beta[8,36]	48.321837	3.524404	42.052537616	56.383302
##	beta[9,36]	49.399843	4.873875	41.347955702	59.500296
##	beta[10,36]	29.047275	8.894310	10.064662584	46.861783
##	beta[11,36]	49.756600	5.642103	41.228426815	64.068104
	beta[12,36]	68.951891		51.020552750	87.590803
	beta[13,36]	30.002838		11.200756574	47.942744
	beta[1,37]	58.341108		41.264843599	77.051938
	beta[2,37]	59.287404		40.322821289	78.633457
##	beta[3,37]	36.366248		17.627972176	55.296685
##	beta[3,37] beta[4,37]	66.757056		47.926249689	85.193607
	beta[4,37] beta[5,37]	30.773170		11.760803474	49.231633
	beta[6,37]	58.704776		41.133307694	78.306443
	beta[7,37]	38.149012		20.160715882	56.041741
		48.335032		42.530093976	56.179212
	beta[8,37]				
	beta[9,37]	49.415194		40.750152182	60.281467
	beta[10,37]	29.055831		10.065773373	47.103764
	beta[11,37]	49.736746		41.056461263	64.073448
	beta[12,37]	68.953397		51.127304349	87.830202
	beta[13,37]	30.016123		10.699783852	48.176534
	beta[1,38]	58.340468		40.180364778	77.327484
##	, , , , ,	59.286290		40.067979567	78.734585
##	beta[3,38]	36.368730		17.491857229	55.832696
	beta[4,38]	66.788116		47.588104682	85.396471
	beta[5,38]	30.767453	8.905424	11.422559599	49.843618
##	beta[6,38]	58.720409	9.082314	41.162307046	78.581337
##	beta[7,38]	38.172983	9.242998	19.182914386	56.549156
##	beta[8,38]	48.387789	3.498412	42.168388358	56.413607
##	beta[9,38]	49.444886	5.306420	40.800231582	60.749636
##	beta[10,38]	29.035435	9.142563	9.418918387	47.089320
##	beta[11,38]	49.715431	5.352785	41.035532568	63.293734
##	beta[12,38]	68.920898	9.070841	50.354393036	88.211045
##	beta[13,38]	30.038596	9.063264	10.567711050	48.120986
##	beta[1,39]	58.359120	9.055597	40.087699119	77.355351
##	beta[2,39]	59.284449	9.469253	39.502874714	78.399574
	beta[3,39]	36.408078	9.519165	16.818198437	56.536652

##	beta[4,39]	66.776303	0 306232	47.168488626	85.992522
	beta[5,39]	30.758422		11.085774912	49.653635
	beta[6,39]	58.710203		40.576298194	78.587820
	-	38.140829		18.894201298	56.998035
##	beta[7,39]				
	beta[8,39]	48.429538		41.858979011	56.709754
	beta[9,39]	49.473816		40.357940479	60.951173
	beta[10,39]	28.995772	9.302294	9.130487427	47.417964
	beta[11,39]	49.709755		41.182487243	62.277429
	beta[12,39]	68.942451		49.783307056	88.434486
##	beta[13,39]	30.003333		10.393625232	47.771017
##	beta[1,40]	58.353360	9.231575	39.431915295	77.871004
##	beta[2,40]	59.290483	9.635168	38.411617382	78.866058
##	beta[3,40]	36.399430	9.659436	16.597760585	56.977430
##	beta[4,40]	66.768518	9.424373	47.229364921	85.992447
##	beta[5,40]	30.727088	9.094256	11.412599951	49.889352
##	beta[6,40]	58.709054	9.289561	39.995344031	78.472721
##	beta[7,40]	38.146629	9.373491	19.164503954	57.627618
##	beta[8,40]	48.451595	3.813805	41.368817089	57.200151
##	beta[9,40]	49.448852	5.644211	39.983535608	61.891590
##	beta[10,40]	28.999952	9.442012	8.618916745	47.525784
##	beta[11,40]	49.685392	4.965266	41.061955231	61.435476
	beta[12,40]	68.931455	9.355081	49.594773334	88.582473
	beta[13,40]	30.051289	9.299604	9.718960143	48.051397
	beta[1,41]	58.336727		39.071837410	78.805922
	beta[2,41]	59.286191		38.720183462	79.558980
##	beta[2,41] beta[3,41]	36.418498	9.713833	16.493530288	57.493731
##	beta[3,41] beta[4,41]	66.831560		47.615645885	86.931792
	beta[5,41]	30.701429	9.188257		49.874717
##				39.671102795	78.852236
	beta[6,41]	58.741832			
	beta[7,41]	38.183375	9.411449	19.164451608	57.790796
##	beta[8,41]	48.495216	3.912999	41.193255320	57.663554
	beta[9,41]	49.441621		39.995993475	62.198043
	beta[10,41]	29.026590	9.435413	8.788286374	47.850572
	beta[11,41]	49.671192		41.188750018	60.665107
	beta[12,41]	68.911594		49.524821191	88.890187
	beta[13,41]	30.080213		10.507102014	48.092876
	beta[1,42]	58.327299		38.494441114	79.135529
##	beta[2,42]	59.315197		38.758678715	79.756946
##	beta[3,42]	36.431269	9.855190	16.702552703	57.422336
##	beta[4,42]	66.794619	9.618841	47.270909739	87.279727
##	beta[5,42]	30.724200	9.270947	11.697667477	49.581526
##	beta[6,42]	58.709875	9.539052	39.072112399	78.369050
##	beta[7,42]	38.200600	9.499330	19.127685432	58.811867
##	beta[8,42]	48.485498	4.018009	40.977861641	58.217997
##	beta[9,42]	49.489778	5.953679	39.464632502	62.525827
##	beta[10,42]	28.976214	9.587119	8.456011989	48.057925
##	beta[11,42]	49.606954	4.854200	40.985117783	61.233931
##	beta[12,42]	68.922454	9.483470	49.213112779	88.231759
	beta[13,42]	30.113020		10.527053415	48.956384
	beta[1,43]	58.394157		38.319952365	79.931830
	beta[2,43]	59.262977		38.906056136	78.935442
	beta[3,43]	36.390810		16.160352123	57.869348
11	2300[0, 10]	20.00010	J.JU1001		3, .000010

##	beta[4,43]	66.806487	9.716313	47.240231384	88.402134
##	beta[5,43]	30.755100	9.442915	11.307810825	50.556291
##	beta[6,43]	58.698953	9.636199	38.785208086	78.747404
##	beta[7,43]	38.189758	9.633878	19.518471948	58.635497
##	beta[8,43]	48.496378	4.160272	40.617589007	58.535339
	beta[9,43]	49.483359		39.055451967	63.309265
	beta[10,43]	28.983426	9.576681	8.159164170	47.874831
	beta[11,43]	49.552887		40.541488469	61.582569
	beta[11,43] beta[12,43]	68.939115		49.246824195	88.995207
			9.697521	9.535885444	49.358725
	beta[13,43]	30.138320			
##	beta[1,44]	58.405969		38.387239157	79.697591
	beta[2,44]	59.302714		38.498677602	79.710075
	beta[3,44]	36.412800		16.343707023	57.240067
	beta[4,44]	66.854301		46.902249065	88.266295
	beta[5,44]	30.755484		10.800641827	50.965044
	beta[6,44]	58.702254		39.029395870	78.735606
##	beta[7,44]	38.203245	9.651559	18.652743731	58.949260
##	beta[8,44]	48.529961	4.245846	40.282785902	59.027521
##	beta[9,44]	49.453420	6.148721	38.741434479	62.775051
##	beta[10,44]	29.014147	9.656701	8.626992705	48.055538
##	beta[11,44]	49.427021	5.099508	39.999163899	61.011901
##	beta[12,44]	68.923515	9.702870	48.915360632	89.206240
	beta[13,44]	30.141496	9.814635	10.204458277	50.130765
	beta[1,45]	58.430856	9.717739	38.972051096	79.758418
##	beta[2,45]	59.312852		38.256471921	80.287300
##	beta[3,45]	36.378715		15.659445261	57.202105
	beta[4,45]	66.802716		47.024185883	88.505745
	beta[5,45]	30.766169	9.586867	9.965656773	50.708335
	beta[6,45]	58.714490		38.570894024	79.643478
	beta[0,45]	38.219739		19.029486536	59.264245
	beta[8,45]	48.549159		39.720507688	58.072259
				38.560404723	
	beta[9,45]	49.478769			63.430349
	beta[10,45]	29.032992	9.689625	8.090693482	48.261811
	beta[11,45]	49.344680		39.642010590	61.275254
	beta[12,45]	68.878893		49.325852234	89.337864
	beta[13,45]	30.166113		10.166690817	50.701074
	beta[1,46]	58.499507		38.409384574	80.097271
##	beta[2,46]	59.330301		38.493708436	80.978253
	beta[3,46]	36.410325	10.179832	15.619467395	57.070546
	beta[4,46]	66.721869	10.040144	45.963368365	88.335803
##	beta[5,46]	30.790977	9.689562	9.849343843	50.858197
##	beta[6,46]	58.752577	9.997818	38.282581329	79.618938
##	beta[7,46]	38.224216	9.806980	18.222606321	58.963267
##	beta[8,46]	48.568829	4.392153	39.555711824	58.544346
##	beta[9,46]	49.478814	6.492325	38.766877622	63.394037
##	beta[10,46]	29.081176	9.858958	7.923523351	48.403863
	beta[11,46]	49.269274	5.350192	39.254654944	61.349672
	beta[12,46]	68.918785		48.085270324	89.964039
	beta[13,46]	30.181177	9.998305	9.735086322	50.057624
	beta[1,47]	58.423416		38.576325587	80.338348
	beta[2,47]	59.283561		38.303267450	81.235734
	beta[2,47] beta[3,47]	36.379006		15.081852478	57.482141
π#	0000[0,71]	30.313000	10.024000	10.001002410	01.402141

##	beta[4,47]	66.729498	10.071167	45.610250117	88.876759
##	beta[5,47]	30.815304	9.835193	9.599901756	51.673917
##	beta[6,47]	58.758131	10.071746	37.866078057	79.835772
##	beta[7,47]	38.212291	9.921624	17.729374945	59.259893
##	beta[8,47]	48.608688	4.478398	39.193238629	57.986176
##	beta[9,47]	49.442414	6.546517	38.139298413	64.214771
##	beta[10,47]	29.121687	9.988454	7.296830671	49.486167
##	beta[11,47]	49.197262	5.449391	38.616841354	60.913929
##	beta[12,47]	68.936028	10.148096	47.907419430	89.631177
##	beta[13,47]	30.190164	10.029180	10.412857376	50.130141
##	beta[1,48]	58.376473	9.966157	38.088012056	79.725484
##	beta[2,48]	59.316804	10.499138	38.339091728	81.578694
##	beta[3,48]	36.383144	10.409268	14.380657387	57.154426
##	beta[4,48]	66.735541	10.190436	45.536808312	88.417871
##	beta[5,48]	30.821549	9.952443	10.212783464	51.782073
##	beta[6,48]	58.763379	10.163826	37.563366017	79.826758
##	beta[7,48]	38.192056	10.039275	18.057363093	59.112538
##	beta[8,48]	48.643146	4.443255	39.692474090	57.852687
##	beta[9,48]	49.456994	6.703917	37.905764264	64.284976
##	beta[10,48]	29.111836	10.032908	6.897197424	49.585019
##	beta[11,48]	49.073080	5.475640	37.974862071	61.387713
##	beta[12,48]	68.953508	10.210129	48.101115995	90.397385
	beta[13,48]	30.215184	10.143215	10.135639255	50.678913
##	beta[1,49]	58.371748	10.076427	37.610775850	80.675610
##	beta[2,49]	59.262730	10.537179	38.194307498	81.923461
##	beta[3,49]	36.401477	10.576266	14.374298813	57.507530
##	beta[4,49]	66.791020	10.392486	44.781314836	89.294955
##	beta[5,49]	30.861386	10.016867	9.679411445	52.220877
##	beta[6,49]	58.727007	10.214012	37.561745616	79.754401
##	beta[7,49]	38.173544	10.068986	17.952996392	58.910903
##	beta[8,49]	48.665191	4.589358	39.611942349	58.550163
##	beta[9,49]	49.393515	6.896712	36.959567670	64.542820
##	beta[10,49]	29.149170	10.113054	6.766574563	49.558695
##	beta[11,49]	48.979910	5.479934	37.953116067	61.139598
##	beta[12,49]	68.975411	10.222189	47.854051187	90.485636
##	beta[13,49]	30.183653	10.215848	9.427334993	50.598959
##	beta[1,50]	58.359633	10.173904	37.726434046	80.278073
##	beta[2,50]	59.254114	10.660825	37.828848998	81.586989
##	beta[3,50]	36.373283	10.709186	14.387938771	57.587661
##	beta[4,50]	66.780769	10.471904	44.737988893	89.022409
##	beta[5,50]	30.846789	10.105321	9.152477380	52.042250
##	beta[6,50]	58.759141	10.279610	37.756613081	80.158068
##	beta[7,50]	38.121702	10.177687	17.780112791	59.767881
##	beta[8,50]	48.679945	4.567504	39.497142616	57.927683
##	beta[9,50]	49.385363	6.986503	36.891909846	64.707378
	beta[10,50]	29.142695	10.250042	6.658297429	49.806549
	beta[11,50]	48.894773		37.388418318	60.792996
	beta[12,50]	68.939555	10.367675	47.644376610	91.177732
	beta[13,50]	30.187666	10.255948	8.777585890	50.407425
	beta[1,51]	58.360508		37.391792101	80.466785
	beta[2,51]	59.214193		37.563021517	81.792932
	beta[3,51]	36.372563	10.788348	14.107608358	57.888447

##	beta[4,51]	66.832387	10.530477	44.684969452	89.726578
##	beta[5,51]	30.842377	10.285400	9.259517983	52.490213
	beta[6,51]	58.771224	10.342302	37.582263220	80.131550
##	beta[7,51]	38.124566	10.325040	17.343901195	59.462827
##	beta[8,51]	48.666946	4.547974	39.576742231	58.176938
##	beta[9,51]	49.403413	7.142299	36.147592232	65.078941
##	beta[10,51]	29.173840	10.417500	6.709338557	50.130286
##	beta[11,51]	48.796643	5.539586	37.460855979	60.910156
##	beta[12,51]	68.933561	10.493311	47.371023231	91.104252
##	beta[13,51]	30.177794	10.336718	8.327671177	50.996954
##	beta[1,52]	58.358538	10.238379	37.396494319	80.939294
##	beta[2,52]	59.234402	10.865255	37.556279355	82.498279
##	beta[3,52]	36.379327	10.957520	13.548887188	57.988779
##	beta[4,52]	66.896477	10.540694	45.137626078	89.427730
##	beta[5,52]	30.812262	10.383023	8.924519973	53.395845
##	beta[6,52]	58.737873	10.494347	36.513691614	80.817242
##	beta[7,52]	38.129867	10.375952	17.131317373	60.727658
##	beta[8,52]	48.648500	4.516445	39.721257965	57.914559
##	beta[9,52]	49.408848	7.220367	36.147935818	64.860569
##	beta[10,52]	29.167035	10.390763	6.073941805	50.503183
##	beta[11,52]	48.734515	5.636700	37.446339036	60.993169
##	beta[12,52]	68.880616	10.535383	47.012084178	90.937786
##	beta[13,52]	30.193530	10.389880	8.003942688	51.143873
##	beta[1,53]	58.341440	10.260756	36.870105757	80.802492
##	beta[2,53]	59.218473	10.946704	38.010436406	81.834745
##	beta[3,53]	36.386089	11.063236	13.740314043	59.118357
##	beta[4,53]	66.874743	10.623580	45.084557438	88.915980
##	beta[5,53]	30.807665	10.542474	9.332499709	53.797092
##	beta[6,53]	58.789201	10.545334	36.597044566	80.953247
##	beta[7,53]	38.128572	10.490000	16.936744619	60.634267
##	beta[8,53]	48.564014	4.514155	39.632684987	58.633418
##	beta[9,53]	49.402590	7.391540	35.937221252	65.269496
##	beta[10,53]	29.157230	10.403835	6.254603198	50.162928
##	beta[11,53]	48.644189	5.629157	36.752845703	61.395883
##	beta[12,53]	68.867769	10.657177	46.960059281	91.292683
##	beta[13,53]	30.235656	10.580251	7.845516186	51.964238
##	beta[1,54]	58.351241	10.423225	37.282258057	81.733496
##	beta[2,54]	59.222953	11.046093	37.419624873	82.533546
##	beta[3,54]	36.414459	11.100828	13.226809567	59.347321
##	beta[4,54]	66.900985	10.686572	45.026811314	89.628045
##	beta[5,54]	30.773649	10.644238	8.799265359	54.224195
	beta[6,54]	58.755876	10.612440	36.207909358	81.116149
##	beta[7,54]	38.121836	10.591404	16.351813840	60.820745
	beta[8,54]	48.564066	4.464247	39.684957586	58.439100
	beta[9,54]	49.432602	7.581063	35.819965337	66.004459
	beta[10,54]	29.159083		6.541942937	51.352615
	beta[11,54]	48.582843		36.756121162	61.381583
	beta[12,54]	68.880772		46.541235569	91.511470
	beta[13,54]	30.232632	10.707013	7.507528645	51.545120
	beta[1,55]	58.343371		36.562238189	81.479082
	beta[2,55]	59.229158		36.900865752	82.705022
	beta[3,55]	36.365920		12.864779686	59.466620
			1,0010		22.100020

##	beta[4,55]	66.917908	10.803984	45.010219945	89.941779
##	beta[5,55]	30.780107	10.864908	7.786811227	53.919234
	beta[6,55]	58.805079	10.744315	36.586321595	81.370895
	beta[7,55]	38.134680	10.726170	16.027044153	61.503235
##	beta[8,55]	48.510220		39.514798471	57.916517
##	beta[9,55]	49.460040		35.172964231	66.315828
##	beta[10,55]	29.164294	10.530930	6.561905336	50.806524
##	beta[11,55]	48.556084	5.763693	36.819071593	61.521158
##	beta[12,55]	68.863385	10.851512	46.136422023	91.602013
##	beta[13,55]	30.232908	10.832946	7.900152233	51.800465
##	beta[1,56]	58.371922	10.665882	36.116386784	81.913443
	beta[2,56]	59.267522	11.182612	37.492784085	83.161382
##	beta[3,56]	36.382676		12.963487104	60.321347
	beta[4,56]	66.910817	10.900907	44.729870439	90.445138
##	beta[5,56]	30.793502	10.982388	7.895552844	53.916957
##	beta[6,56]	58.835567	10.851720	36.431103803	81.554842
##	beta[7,56]	38.163235	10.752045	16.026432348	60.646408
##	beta[8,56]	48.513139	4.419162	39.451658984	57.990484
##	beta[9,56]	49.452286	7.901976	34.663283088	66.420171
##	beta[10,56]	29.169069	10.648283	6.478439505	51.585557
##	beta[11,56]	48.484691	5.854181	36.702473733	61.666074
##	beta[12,56]	68.844701	10.991723	46.272332667	91.873197
##	beta[13,56]	30.267814	10.897896	7.626706282	52.009110
##	beta[1,57]	58.356785	10.820326	36.309412844	82.617113
##	beta[2,57]	59.218785	11.207454	37.275134821	82.897199
##	beta[3,57]	36.366838	11.413242	13.057425364	60.329897
	beta[4,57]	66.934335	10.901233	44.588549850	90.700158
##	beta[5,57]	30.808424	11.120891	7.637684719	54.254930
##	beta[6,57]	58.846877	10.993248	36.490434651	81.787732
	beta[7,57]	38.143969	10.809271	16.376183478	61.043716
##	beta[8,57]	48.465420	4.422176	39.367811830	57.935443
##	beta[9,57]	49.453209	8.008460	33.884218092	66.651680
	beta[10,57]	29.194361	10.776201	6.490554527	51.299729
	beta[11,57]	48.381313		36.673099218	61.690526
	beta[12,57]	68.849023	11.130463	45.255149913	92.088191
	beta[13,57]	30.285477	10.956350	8.390324596	52.622708
	beta[1,58]	58.329161		35.470286955	82.345793
	beta[2,58]	59.206358		37.808780208	83.013399
	beta[3,58]	36.380671	11.531063	12.910055425	60.636513
	beta[4,58]	66.931938		43.796551416	90.622406
	beta[5,58]	30.786600	11.258816	7.020274303	54.419597
	beta[6,58]	58.828922		35.863443852	81.851471
	beta[7,58]	38.137641		15.960975008	61.244778
	beta[8,58]	48.393890	4.464992	39.102932054	58.065218
	beta[9,58]	49.421673	8.139247	34.164584881	66.743577
	beta[10,58]	29.142205		6.707854288	51.584996
##	beta[11,58]	48.268719		36.436398721	62.264508
##	beta[12,58]	68.841191		45.055445507	92.216677
	beta[13,58]	30.263699	11.063687		52.672884
	beta[1,59]	58.367483		35.187186501	83.697803
	beta[2,59]	59.208403		37.442798539	82.954968
##	beta[3,59]	36.398560	11.657224	13.115135881	60.861212

##	beta[4,59]	66.896607	11.024604	44.344113119	90.822548
##	beta[5,59]	30.822151	11.357791	7.259622816	54.458574
##	beta[6,59]	58.854387	11.030556	36.276026604	82.682631
##	beta[7,59]	38.137141	11.039464	15.874004305	61.027153
##	beta[8,59]	48.337983	4.427708	38.844276032	57.868409
##	beta[9,59]	49.423118	8.348622	33.655405610	66.933881
##	beta[10,59]	29.146749	10.966565	6.162773092	50.860331
##	beta[11,59]	48.200853	6.185793	36.399784986	62.582954
##	beta[12,59]	68.800269	11.283705	45.041936902	92.512809
	beta[13,59]	30.233704	11.034258	7.467569945	52.322719
##	beta[1,60]	58.399385	11.216877	35.299687117	83.912895
##	beta[2,60]	59.221091	11.384827	36.293106530	82.595534
	beta[3,60]	36.407102		13.333197127	61.079396
	beta[4,60]	66.928589		43.383818775	90.714565
	beta[5,60]	30.787482	11.349042	6.824251845	54.764170
	beta[6,60]	58.858079		36.868076389	82.592953
	beta[7,60]	38.165060		15.786224385	61.782034
	beta[8,60]	48.267115		38.898205129	57.504716
	beta[9,60]	49.413152		33.105198061	68.323963
	beta[3,60] beta[10,60]	29.199060	11.088639	5.441454211	51.715760
	beta[10,60] beta[11,60]	48.077798		36.350945112	62.273026
	beta[11,60] beta[12,60]	68.837330		45.059385147	92.416020
	beta[13,60]	30.190974	11.126890	7.239842949	53.175586
	beta[1,61]	58.371852		34.701425186	83.659054
##	beta[2,61]	59.219874		36.450351763	83.746174
##	beta[3,61]	36.437960		12.703765676	61.793046
	beta[4,61]	66.916942		43.104250789	91.228247
	beta[5,61]	30.781223	11.545389	6.576052289	54.329584
	beta[6,61]	58.853556		36.304430192	82.952119
	beta[7,61]	38.158854	11.218346	15.518861044	61.261440
	beta[8,61]	48.256132		39.239965241	57.361407
	beta[9,61]	49.420281		32.650724922	68.153958
	beta[9,61] beta[10,61]	29.148674	11.172535	5.309437026	52.322882
	beta[11,61]	47.976439		35.826713427	61.475557
	beta[11,61] beta[12,61]	68.837590		45.624958727	92.615233
	beta[13,61]	30.162911		6.334993787	53.166707
		58.391343		34.461657051	82.773453
##	beta[1,62] beta[2,62]	59.238652		36.204043700	83.918613
					61.602292
	beta[3,62]	36.429648		12.458547333 42.995189708	
	beta[4,62]	66.953771 30.777061	11.719088	6.643962964	91.811529 54.700657
	beta[5,62]				
	beta[6,62]	58.822960		36.133674386	82.527150
	beta[7,62]	38.192201		14.988273257	61.409143
	beta[8,62]	48.153490		39.115646432 32.894364583	56.658797
	beta[9,62]	49.431759			68.274806
	beta[10,62]	29.151681	11.306333	5.169229961	52.452953
	beta[11,62]	47.866026		34.834361162	61.797696
	beta[12,62]	68.848084		45.165849442	92.573702
	beta[13,62]	30.166750	11.290535	6.122693283	53.399221
	beta[1,63]	58.373729		34.079818559	84.043405
	beta[2,63]	59.202479		35.727945320	84.208520
##	beta[3,63]	36.417399	11.930145	11.885525227	61.881696

##	beta[4,63]	66.954686	11.349544	42.698047641	91.513979
	beta[5,63]	30.810003	11.822721	6.933093799	54.825385
	beta[6,63]	58.880541	11.368932	35.940211580	83.389061
	beta[7,63]	38.203453		13.864259274	62.037468
##	beta[8,63]	48.116468	4.324737	38.586997265	57.050284
##	beta[9,63]	49.420086	8.879292	32.314616284	68.501876
##	beta[10,63]	29.112195	11.457877	4.775617753	52.606172
##	beta[11,63]	47.772666	6.241172	34.831031978	61.623744
##	beta[12,63]	68.849640	11.618509	45.129750446	93.230882
##	beta[13,63]	30.149187	11.327947	5.711058387	53.599843
##	beta[1,64]	58.375628	11.520699	33.872698478	83.599130
##	beta[2,64]	59.177138	11.763269	35.605706196	84.651303
##	beta[3,64]	36.427187	11.994397	12.360076599	61.910626
##	beta[4,64]	66.942923	11.447698	42.963776574	91.565736
##	beta[5,64]	30.829439	11.696516	6.622654464	55.359942
##	beta[6,64]	58.895988	11.467617	35.351837032	84.106282
##	beta[7,64]	38.213059	11.631348	13.813603747	62.804926
##	beta[8,64]	47.992343	4.335173	38.520324624	56.755129
##	beta[9,64]	49.397296	9.073611	32.534713759	68.376852
##	beta[10,64]	29.107985	11.607488	4.081686529	52.564719
##	beta[11,64]	47.694091	6.249770	34.814495849	61.420876
##	beta[12,64]	68.870790	11.735939	44.863761849	93.904641
	beta[13,64]	30.178077	11.407891	5.821665232	53.480482
	beta[1,65]	58.360293	11.615244	33.923621724	83.323372
##	beta[2,65]	59.152876	11.851874	35.142731077	85.146911
##	beta[3,65]	36.462653	12.092097	11.707490776	61.670257
	beta[4,65]	66.967801	11.554573	42.683096204	91.463034
	beta[5,65]	30.896622	11.819904	6.511232906	55.885813
	beta[6,65]	58.843573	11.538920	34.853962209	84.591943
##	beta[7,65]	38.223277	11.735928	14.018747249	62.881761
##	beta[8,65]	47.938952	4.317256	38.274920125	57.092983
	beta[9,65]	49.416578	9.197400	32.083009851	68.838766
	beta[10,65]	29.087871	11.675726	4.266908684	52.742621
	beta[11,65]	47.639925	6.274316	34.509333380	60.919568
	beta[12,65]	68.871959	11.789986	45.340007609	94.105321
	beta[13,65]	30.194340	11.510016	5.337938975	54.040600
	beta[1,66]	58.319068	11.740632	33.433443007	83.614582
	beta[2,66]	59.153497	11.874212	34.720834645	84.958936
	beta[3,66]	36.467368		11.887423043	62.034647
	beta[4,66]	66.964838	11.623368	43.095558132	91.223000
	beta[5,66]	30.882659	11.820394	6.591294988	55.942858
	beta[6,66]	58.876684		35.000832680	84.249143
	beta[7,66]	38.213197		14.037734423	63.043339
	beta[8,66]	47.828085		38.277693346	56.159101
	beta[9,66]	49.433882		31.521365898	69.135348
	beta[10,66]	29.071038	11.765064	3.798024744	52.709295
	beta[10,66]	47.582478		34.431942064	61.430073
	beta[11,66] beta[12,66]	68.843516		44.454908881	94.459279
	beta[13,66]	30.166756	11.654989		54.338490
	beta[1,67]	58.335350		33.593979298	83.070067
	beta[1,67]	59.145296		35.110508035	85.251156
				11.822771719	
##	beta[3,67]	36.490503	12.214404	11.022//11/19	62.087071

##	beta[4,67]	66.955054	11.710533	43.636065803	91.682543
##	beta[5,67]	30.911322	12.170245	5.635220508	56.720341
##	beta[6,67]	58.880914	11.657765	34.889448986	84.544273
##	beta[7,67]	38.229864	11.899796	14.117395868	63.434659
##	beta[8,67]	47.704448	4.283660	38.268340695	55.915032
##	beta[9,67]	49.457194	9.423271	31.340991634	69.631722
##	beta[10,67]	29.083442	11.892838	3.614520539	52.397398
##	beta[11,67]	47.550898	6.239501	33.837221721	60.831068
##	beta[12,67]	68.824949	11.981327	43.763197087	95.013018
##	beta[13,67]	30.204274	11.704860	4.155919560	54.274206
##	beta[1,68]	58.338325	11.984597	32.761158696	83.665478
##	beta[2,68]	59.167650	11.970022	34.454614518	86.098268
##	beta[3,68]	36.483560	12.314699	11.850445126	62.589779
##	beta[4,68]	67.004598	11.854641	42.587606149	92.807817
##	beta[5,68]	30.951491	12.311378	5.820253640	57.063566
##	beta[6,68]	58.831470	11.750276	34.038952511	84.533575
##	beta[7,68]	38.266988	11.959153	13.903926425	63.739515
##	beta[8,68]	47.647819	4.303650	38.250003639	56.235636
##	beta[9,68]	49.423036	9.534090	31.534536076	69.782768
	beta[10,68]	29.139129	12.069566	2.914690032	53.526170
##	beta[11,68]	47.513857	6.232526	33.774650920	60.842811
	beta[12,68]	68.820723	12.079601	43.832960337	94.977532
	beta[13,68]	30.232503	11.772844	4.815861901	54.330568
	beta[1,69]	58.340948	12.141020	32.308162336	83.671443
##	beta[2,69]	59.180642	11.972796	34.794681196	84.628579
##	beta[3,69]	36.517004		11.180227182	63.024401
##	beta[4,69]	67.074346	11.904119	42.591502206	93.206374
	beta[5,69]	30.980940	12.468565	5.372143052	57.498884
	beta[6,69]	58.827283	11.835322	34.368102837	84.737354
	beta[7,69]	38.276345	11.954292	13.672977752	64.366874
	beta[8,69]	47.582802	4.374362	37.674961692	56.003573
	beta[9,69]	49.440078	9.673483	31.160361510	70.014294
	beta[10,69]	29.137937	12.065679	3.517033752	53.795796
	beta[11,69]	47.497258		34.060121599	60.997473
	beta[12,69]	68.835773	12.113050	43.921416916	94.873925
	beta[13,69]	30.271566	11.860393	5.118499679	54.615339
	beta[1,70]	58.376557	12.113884	32.307987744	84.039839
##	beta[2,70]	59.180403	11.994052	34.317278123	84.715138
##	beta[3,70]	36.532871	12.493138	10.847719694	63.308818
	beta[4,70]	67.045646	12.039169	42.391243970	93.138444
	beta[5,70]	30.971603	12.793942	4.982994407	57.275895
	beta[6,70]	58.825254	11.849343	34.594148388	84.647890
	beta[7,70]	38.257487		13.910830265	64.611359
	beta[8,70]	47.499951	4.363396	37.361483064	56.000985
	beta[9,70]	49.462794		30.726174630	70.453000
	beta[10,70]	29.141884	12.062563	3.109836522	53.955494
	beta[11,70]	47.512724		34.206399401	61.177899
	beta[12,70]	68.878035		44.242526446	95.134336
	beta[13,70]	30.295872	11.995297	4.955058760	55.732865
	beta[1,71]	58.389135		32.094280559	84.138663
	beta[2,71]	59.139176		34.170543889	84.868332
	beta[3,71]	36.512162		10.104695942	63.608130
		<b></b>			

##	beta[4,71]	67.073922	12.111629	42.616533721	93.493815
##	beta[5,71]	30.991149	13.092239	4.279579041	57.150367
##	beta[6,71]	58.821858	11.867665	34.551054006	84.285714
##	beta[7,71]	38.253813	12.207121	12.485185945	64.915939
##	beta[8,71]	47.469760	4.376404	37.278858315	55.803421
##	beta[9,71]	49.517369	9.920173	30.063638875	71.616799
##	beta[10,71]	29.124487	12.126597	3.328032843	54.763195
##	beta[11,71]	47.477054	6.149547	34.299553257	61.363167
##	beta[12,71]	68.899953	12.265686	43.669368042	94.927925
##	beta[13,71]	30.368542	12.080691	4.998923155	56.128048
##	beta[1,72]	58.414393	12.298819	31.666610346	84.186927
##	beta[2,72]	59.200237	12.180809	34.115466880	85.234820
##	beta[3,72]	36.507679	12.752761	9.715142074	64.297358
##	beta[4,72]	67.044334	12.133782	41.785651851	93.558911
##	beta[5,72]	30.949765	13.209077	4.594940175	56.814419
##	beta[6,72]	58.802256	12.001162	34.052073739	84.539552
##	beta[7,72]	38.278682	12.312897	13.036511822	64.869772
##	beta[8,72]	47.410875	4.399645	37.113256583	55.943761
##	beta[9,72]	49.516255	9.991996	30.322847470	72.141849
##	beta[10,72]	29.120122	12.193277	3.477082916	54.102608
##	beta[11,72]	47.462080	6.109807	34.517458640	61.028475
##	beta[12,72]	68.919687	12.334761	43.163687501	95.580325
##	beta[13,72]	30.358773	12.203530	4.401692206	55.667976
##	beta[1,73]	58.449060	12.372700	30.798546104	85.222698
##	beta[2,73]	59.238416	12.271963	34.275660387	85.614054
##	beta[3,73]	36.521323	12.887359	9.981926698	63.729871
##	beta[4,73]	67.040703	12.202768	41.548395113	93.486045
##	beta[5,73]	30.963490	13.312499	4.609267070	56.619057
##	beta[6,73]	58.758012	12.023991	32.920769845	84.581795
##	beta[7,73]	38.261928	12.384401	12.577460540	64.197204
##	beta[8,73]	47.356301	4.342371	37.152438616	55.215584
##	beta[9,73]	49.543790	9.998745	30.851432615	71.710668
##	beta[10,73]	29.151020	12.195170	3.476246834	54.522922
##	beta[11,73]	47.465257	6.057054	34.323694181	60.893485
##	beta[12,73]	68.916134	12.465056	42.488397083	95.467160
##	beta[13,73]	30.330845	12.258066	4.500789090	55.023851
##	beta[1,74]	58.463040	12.501422	30.294223787	84.434830
##	beta[2,74]	59.259105	12.357756	34.266725650	85.591715
##	beta[3,74]	36.520008	12.942036	9.465940951	64.439258
##	beta[4,74]	67.011043	12.250510	42.102533514	93.556858
	beta[5,74]	30.950975	13.247195	3.862107925	56.923023
	beta[6,74]	58.792671		32.649687665	84.857500
	beta[7,74]	38.231942	12.470705	12.165510732	64.076279
	beta[8,74]	47.348046		37.251180494	55.568351
	beta[9,74]	49.459961	10.060066	30.657190794	71.021424
	beta[10,74]	29.184352	12.281924	3.420815648	54.323875
	beta[11,74]	47.463473		34.628183337	61.251493
	beta[12,74]	68.889007		42.615350553	95.895221
	beta[13,74]	30.331375	12.363635	4.960443263	55.846072
	beta[1,75]	58.434137		30.394348276	84.352801
	beta[2,75]	59.263301		33.439190924	85.487078
##	beta[3,75]	36.506027	13.024933	9.125295795	64.452571

	beta[4,75]	67.027579	12.294680	41.817997232	94.363861
##	beta[5,75]	30.957306	13.526832	3.553272651	57.181566
##	beta[6,75]	58.806512	12.187032	32.904725204	85.320917
##	beta[7,75]	38.244119	12.578479	11.746589641	63.913766
##	beta[8,75]	47.361629	4.387525	37.441233029	55.237735
##	beta[9,75]	49.487540	10.020795	29.914458405	71.205841
##	beta[10,75]	29.199321	12.284474	2.863219821	55.071708
##	beta[11,75]	47.469991	5.968461	34.302432028	61.262171
##	beta[12,75]	68.850578	12.730594	41.985190023	96.106345
	beta[13,75]	30.339860	12.389446	4.247127217	56.113875
	beta[1,76]	58.474796	12.772836	30.159055192	85.414651
	beta[2,76]	59.253370	12.504782	32.921076769	86.101379
	beta[3,76]	36.471748	13.134295	8.315161521	64.852105
	beta[4,76]	67.071777	12.361497	41.465248810	93.968322
	beta[5,76]	30.989195	13.577187	2.961328379	58.097902
	beta[6,76]	58.792099		32.671086447	86.096819
	beta[7,76]	38.228862		11.142634379	65.086725
	beta[8,76]	47.380522		37.476536224	55.116488
	beta[9,76]	49.512021		29.345030677	71.536225
	beta[3,76] beta[10,76]	29.246713	12.329187	3.676782078	54.261305
	beta[10,76] beta[11,76]	47.449339		34.406261691	61.103637
	beta[11,76] beta[12,76]	68.818546		42.340259523	96.016407
	beta[12,76] beta[13,76]	30.348127	12.484313	4.029957544	56.098686
	beta[13,70] beta[1,77]	58.440115		30.194062579	84.842276
	beta[1,77] beta[2,77]	59.285687		33.074322410	85.726805
##	beta[2,77] beta[3,77]	36.458178	13.145206	9.857862274	65.602520
	beta[3,77] beta[4,77]	67.075767		41.643106008	93.944982
	beta[4,77] beta[5,77]	30.995338	13.668198	2.777438536	58.093984
	beta[6,77]	58.803491		32.929037354	85.831217
	beta[0,77] beta[7,77]	38.217071		11.537155924	65.494304
	beta[7,77] beta[8,77]	47.354370		37.327727416	55.048040
	beta[0,77] beta[9,77]	49.489741		28.625434689	71.959150
	beta[3,77] beta[10,77]	29.231871		3.612038822	54.266606
	beta[10,77] beta[11,77]	47.451691		34.211588926	61.428655
	beta[11,77] beta[12,77]	68.821310		42.445271876	97.086950
	beta[12,77] beta[13,77]	30.361160	12.497925	3.894510184	56.419447
	beta[1,78]	58.442399		30.286695099	84.665727
##		59.297688		33.438602249	86.420344
	· ·	36.501079	13.260490	8.946310993	65.639211
	beta[3,78]	67.079286		41.254533868	
	beta[4,78] beta[5,78]	31.030724	14.130040	2.330889531	94.069775
	· ·				58.781413
##	- / -	58.710647		32.579096109	85.523627
	beta[7,78]	38.227864		10.985115421	66.055869
	beta[8,78]	47.336597		37.359393957	55.136432
	beta[9,78]	49.499875		29.162125590	72.437681
	beta[10,78]	29.231761	12.487892	2.873191906	54.678556
	beta[11,78]	47.480486		34.457122278	61.027930
	beta[12,78]	68.774596		41.726635381	97.127861
	beta[13,78]	30.326017	12.526485	3.673811482	56.419497
	beta[1,79]	58.418095		30.262801135	84.313174
	beta[2,79]	59.281973		32.299275965	86.800214
##	beta[3,79]	36.462680	13.365958	8.404600955	66.662058

##	beta[4,79]	67.117670	12.594917	41.711344061	94.735824
##	beta[5,79]	30.982659	13.717177	1.829955961	58.189314
##	beta[6,79]	58.750004	12.537748	32.701258175	85.517729
##	beta[7,79]	38.264444	12.820554	10.454754609	65.887888
##	beta[8,79]	47.315194	4.401318	37.180134967	55.269292
##	beta[9,79]	49.532062	10.542824	29.136100369	72.491871
##	beta[10,79]	29.222979	12.502015	3.044710347	54.166543
##	beta[11,79]	47.547716	5.872066	34.735857209	60.955238
##	beta[12,79]	68.773562	12.962920	41.316164105	96.779547
##	beta[13,79]	30.303660	12.574035	3.202266224	56.557982
##	beta[1,80]	58.450192	13.202012	31.153967472	85.372306
##	beta[2,80]	59.270896	12.739603	32.643423179	86.528572
##	beta[3,80]	36.447746	13.374385	8.607800548	65.990425
##	beta[4,80]	67.133856	12.682451	41.207539943	95.340824
##	beta[5,80]	30.996376	13.982576	1.414040497	59.429336
##	beta[6,80]	58.764803	12.611418	31.640037146	86.333946
##	beta[7,80]	38.243988	12.896864	10.788548998	66.071397
##	beta[8,80]	47.271060	4.452798	37.109150453	55.201199
##	beta[9,80]	49.545967	10.597010	28.982333137	72.511281
##	beta[10,80]	29.295029	12.514982	2.754774552	54.495338
##	beta[11,80]	47.514720	5.725496	34.965498472	60.871616
##	beta[12,80]	68.792624	13.032590	41.493209905	96.587079
##	beta[13,80]	30.306317	12.608364	3.062780582	56.320468
##	beta[1,81]	58.442139	13.340047	30.628266799	85.095463
##	beta[2,81]	59.307031	12.922564	32.496577079	86.561729
##	beta[3,81]	36.471298	13.445158	8.511642093	66.355875
##	beta[4,81]	67.132254	12.744687	40.886507530	94.692614
##	beta[5,81]	31.010128	14.031865	1.068535156	58.413731
##	beta[6,81]	58.720344	12.717022	31.496459500	86.777700
##	beta[7,81]	38.263884	13.018900	10.594698851	66.461683
##	beta[8,81]	47.287926	4.482460	37.291124907	55.367806
##	beta[9,81]	49.567884	10.651740	28.480436150	72.808832
##	beta[10,81]	29.294580	12.680438	2.603868098	55.451300
##	beta[11,81]	47.536844	5.599482	35.140365008	59.818959
##	beta[12,81]	68.831353	13.101126	41.547322992	97.338746
##	beta[13,81]	30.298639	12.665924	2.226043615	57.201053
##	beta[1,82]	58.446079	13.313209	30.104044759	85.376755
##	beta[2,82]	59.344437	12.957502	32.188058657	86.701779
##	beta[3,82]	36.474577	13.599161	8.633338176	66.686279
##	beta[4,82]	67.100393	12.843710	41.158613904	94.848676
##	beta[5,82]	31.014529	14.226937	2.045232788	59.299384
##	beta[6,82]	58.734116	12.831532	31.087698640	87.498141
##	beta[7,82]	38.244843	13.046531	10.190872996	66.530521
##	beta[8,82]	47.325448	4.442578	37.191517119	55.069577
##	beta[9,82]	49.627856	10.755914	28.994929267	74.046594
##	beta[10,82]	29.353550	12.726875	1.712609381	55.530820
	beta[11,82]	47.526263	5.448350	35.421864097	58.877770
##	beta[12,82]	68.800796	13.138503	41.169607961	97.028130
	beta[13,82]	30.295392	12.743703	1.841897214	56.323586
	beta[1,83]	58.451397	13.309849	29.804767288	85.255314
	beta[2,83]	59.318403	13.002163	31.920984149	87.272427
	beta[3,83]	36.495897	13.632266	8.216115795	67.438267

##	beta[4,83]	67.078619	12.860300	40.502382408	95.625360
##	beta[5,83]	31.064226	14.614560	1.838264011	59.385550
##	beta[6,83]	58.773653	12.910748	31.733657930	86.939983
##	beta[7,83]	38.196548	13.170629	9.736291597	67.105815
##	beta[8,83]	47.320611	4.421482	37.124546160	54.806194
##	beta[9,83]	49.632754	10.920383	28.457661251	74.219645
##	beta[10,83]	29.357860	12.809497	1.491561971	56.300331
##	beta[11,83]	47.551638	5.370239	35.332850154	59.287343
##	beta[12,83]	68.828486	13.217327	41.510878793	96.420626
	beta[13,83]	30.320098	12.809140	1.519127453	56.574302
##	beta[1,84]	58.479495	13.369851	30.577309577	85.751641
##	beta[2,84]	59.328970	13.099365	31.718523608	86.892667
##	beta[3,84]	36.501320	13.733241	8.427217125	67.274308
##	beta[4,84]	67.117476	12.955959	40.185280012	96.244169
##	beta[5,84]	31.074040	14.692053	2.177909512	59.044887
##	beta[6,84]	58.779312	12.969305	31.435276279	87.202697
##	beta[7,84]	38.199893	13.253178	9.564712697	66.728874
	beta[8,84]	47.310601	4.383836	36.908493658	54.861786
##	beta[9,84]	49.658444	11.016255	28.170202380	74.361974
	beta[10,84]	29.344164	12.910673	1.653413421	56.376747
	beta[11,84]	47.549821	5.276159	35.367699322	59.122216
	beta[12,84]	68.863841	13.243987	41.304902907	96.575641
	beta[13,84]	30.315187	12.912650	1.373321751	57.488981
	beta[1,85]	58.450981	13.446973	30.170860361	85.594329
##	beta[2,85]	59.319050	13.257428	32.360578257	87.450596
##	beta[3,85]	36.482719	13.740438	7.957199609	67.556561
##	beta[4,85]	67.164678	13.013702	40.719959879	96.006662
##	beta[5,85]	31.073472	14.555819	1.888448595	59.792780
##	beta[6,85]	58.779733	12.999525	31.890488762	87.790030
##	beta[7,85]	38.192673	13.453433	9.154076625	66.328917
##	beta[8,85]	47.349584	4.353061	36.756278448	54.969211
##	beta[9,85]	49.617940	11.169704	27.719251817	74.494411
##	beta[10,85]	29.346789	13.061989	1.594366474	56.869497
##	beta[11,85]	47.561990	5.121236	35.386786642	58.332326
##	beta[12,85]	68.866892	13.303604	41.998672753	97.146323
##	beta[13,85]	30.254567	13.016166	1.939608534	58.090779
##	beta[1,86]	58.472047	13.515010	29.719558080	86.016975
##	beta[2,86]	59.315879	13.331707	31.537552222	87.756812
##	beta[3,86]	36.463548	13.888965	7.182969407	68.353288
##	beta[4,86]	67.176013	13.109186	40.870965281	95.888008
##	beta[5,86]	31.086835	14.560016	1.553743888	60.146822
##	beta[6,86]	58.781629	13.069621	31.365959452	87.812980
##	beta[7,86]	38.191801	13.444150	8.838913672	66.563783
##	beta[8,86]	47.351458	4.361169	36.713539351	54.929296
##	beta[9,86]	49.640554	11.280721	27.944028588	74.673949
##	beta[10,86]	29.338459	13.094629	1.181589780	56.322007
##	beta[11,86]	47.517310	4.959121	35.321525812	57.853291
##	beta[12,86]	68.888690	13.292049	41.688129982	97.103812
##	beta[13,86]	30.297120	13.069863	1.922848588	58.858301
##	beta[1,87]	58.450824	13.591812	30.343039121	86.450893
##	beta[2,87]	59.299618	13.449319	30.804740647	88.040584
##	beta[3,87]	36.417415	13.934157	6.979624160	68.039295

##	beta[4,87]	67.225310	13.221147	40.792196519	96.938613
##	beta[5,87]	31.075939	14.709691	1.771144810	59.991173
	beta[6,87]	58.782616	13.157511	31.286870200	87.842434
	beta[7,87]	38.186399	13.533528	8.294664597	66.734514
##	beta[8,87]	47.363533		36.652024423	54.483616
##	beta[9,87]	49.613345	11.365495	27.603298939	74.483422
##	beta[10,87]	29.327194	13.180760	1.279026979	56.392973
##	beta[11,87]	47.512452	4.821468	35.279910431	56.765063
##	beta[12,87]	68.900888	13.388940	41.240044693	96.975178
##	beta[13,87]	30.321100	13.177257	1.948253278	58.525529
##	beta[1,88]	58.455364	13.657766	29.963649679	87.392755
##	beta[2,88]	59.298919	13.499998	31.243585377	88.184607
##	beta[3,88]	36.415218	13.969182	7.108364831	67.769917
##	beta[4,88]	67.232183	13.254010	40.419797044	97.475984
##	beta[5,88]	31.066556	14.521748	1.099408845	60.309538
##	beta[6,88]	58.773534	13.312460	30.061747979	88.519206
##	beta[7,88]	38.163138	13.630254	8.136026309	67.202803
##	beta[8,88]	47.379579	4.337303	36.483659657	54.707998
##	beta[9,88]	49.583559	11.499147	26.873136594	74.419207
##	beta[10,88]	29.370933	13.289700	0.982845701	56.486055
##	beta[11,88]	47.463292	4.672813	35.360682726	56.014810
##	beta[12,88]	68.921394	13.439166	41.491560507	97.139183
##	beta[13,88]	30.284860	13.267151	2.251015829	58.779831
##	beta[1,89]	58.490435	13.734478	29.073572307	86.508526
##	beta[2,89]	59.275649	13.684315	30.701411466	88.392121
##	beta[3,89]	36.409046	14.010696	6.486718581	67.311473
##	beta[4,89]	67.228914	13.344590	40.438214172	97.156912
##	beta[5,89]	31.015448	14.512065	1.188575826	60.600105
##	beta[6,89]	58.797814	13.427819	30.570428238	88.359945
##	beta[7,89]	38.160310	13.717254	8.042544992	66.394773
##	beta[8,89]	47.419292	4.331050	36.572815906	54.474855
##	beta[9,89]	49.600551	11.655872	26.556160027	74.833353
##	beta[10,89]	29.379659	13.334638	0.777739093	56.611651
##	beta[11,89]	47.442683		35.550487136	55.237011
##	beta[12,89]	68.911740	13.533632	41.390790421	97.602479
##	beta[13,89]	30.269347	13.395703	2.107129687	58.666754
	beta[1,90]	58.503702	13.828103	28.524807485	87.025442
##	beta[2,90]	59.256433	13.797696	30.277394685	88.306656
##	beta[3,90]	36.381748	14.195180	5.450641477	67.550584
	beta[4,90]	67.239086	13.452026	39.787298646	97.315084
##	beta[5,90]	31.026342	14.588261	0.538517549	60.441714
##	beta[6,90]	58.786394	13.496273	30.352589842	88.382582
##	beta[7,90]	38.125724	13.842857	7.501782909	66.891963
##	beta[8,90]	47.437551	4.368079	36.694080236	54.809547
##	beta[9,90]	49.619771	11.739493	25.578959090	74.673209
	beta[10,90]	29.459543	13.452899	1.096111340	57.344588
##	beta[11,90]	47.384902	4.289008	35.605570979	54.545550
##	beta[12,90]	68.910305	13.601626	41.475952669	97.699939
	beta[13,90]	30.263290	13.504422	2.207613559	58.962556
	beta[1,91]	58.481698	13.814705	28.720929554	87.079811
##	beta[2,91]	59.284588	13.872279	29.956252266	88.149971
##	beta[3,91]	36.419896	14.316089	5.942044071	68.488022

##	beta[4,91]	67.223129	13.492837	40.068851229	97.497651
##	beta[5,91]	31.089511	14.773280	0.147549870	61.019326
	beta[6,91]	58.767858		29.353352911	88.540321
	beta[7,91]	38.137107		7.219636029	67.046431
##	beta[8,91]	47.501993		37.015406041	54.803213
##	beta[9,91]	49.602096		25.656752845	75.005149
	beta[10,91]	29.457050		-0.431972067	57.249462
##	beta[11,91]	47.374163		35.372902753	54.704423
##	beta[12,91]	68.898816	13.654034	40.756598685	98.653165
##	beta[13,91]	30.269491	13.551687	1.570205521	59.404653
##	beta[1,92]	58.487072	13.886613	28.144193822	86.565171
	beta[2,92]	59.300380	13.917326	28.815908071	88.213779
##	beta[3,92]	36.465951	14.350817	5.866131724	68.794601
##	beta[4,92]	67.218516	13.605910	39.361666354	97.947839
##	beta[5,92]	31.096583	14.926044	0.790871303	60.589752
##	beta[6,92]	58.779828	13.692409	29.352800520	89.323443
##	beta[7,92]	38.157595	13.924427	7.072891348	67.230771
##	beta[8,92]	47.556838	4.259204	37.261004492	54.799448
##	beta[9,92]	49.591745	11.858030	26.315650160	75.688881
##	beta[10,92]	29.421657	13.540965	-0.401557400	58.776704
##	beta[11,92]	47.371563	4.592290	35.313944451	55.166417
##	beta[12,92]	68.904757	13.756313	40.350982444	98.438777
##	beta[13,92]	30.255230	13.593713	0.731245872	59.175457
##	beta[1,93]	58.505022	13.991163	28.882161558	87.859738
##	beta[2,93]	59.331251	13.928071	29.200141303	89.019961
##	beta[3,93]	36.487717	14.405551	6.165259593	69.177613
##	beta[4,93]	67.254018	13.705624	39.422730850	98.075588
##	beta[5,93]	31.083305	14.940060	0.784822563	60.977175
##	beta[6,93]	58.813315	13.676760	30.078270812	88.748184
##	beta[7,93]	38.159992	13.901255	7.103293309	67.443064
##	beta[8,93]	47.629225	4.158204	37.366183868	54.953121
##	beta[9,93]	49.551770	12.046538	24.786687215	75.260830
##	beta[10,93]	29.404384	13.511006	0.053257895	58.729657
##	beta[11,93]	47.329129	4.711456	35.110188947	55.259214
##	beta[12,93]	68.863087	13.899593	39.755665925	98.824786
##	beta[13,93]	30.238805	13.663890	1.424466846	59.465303
##	beta[1,94]	58.467914	14.059569	28.485090541	87.514468
##	beta[2,94]	59.345293	14.008480	29.280251184	88.909074
##	beta[3,94]	36.461428	14.473528	6.013463359	68.277224
##	beta[4,94]	67.299892	13.732530	39.418030383	97.799708
##	beta[5,94]	31.132974	14.972969	0.116464872	61.279563
##	beta[6,94]	58.779761	13.734265	30.422117162	88.864566
##	beta[7,94]	38.186749	14.012908	7.577535614	67.682480
##	beta[8,94]	47.732827	3.990566	38.463843577	55.041498
##	beta[9,94]	49.519404	12.144891	24.549838750	75.022243
##	beta[10,94]	29.371810	13.569355	-0.147888897	58.056595
##	beta[11,94]	47.361416	4.808430	35.244023668	55.564992
##	beta[12,94]	68.861086	14.014480	39.897491680	99.272416
##	beta[13,94]	30.222478	13.698995	0.755021410	59.035740
##	beta[1,95]	58.482808	14.175845	28.485783910	87.631161
##	beta[2,95]	59.351240	14.132131	28.652784587	89.370345
##	beta[3,95]	36.462526	14.512482	5.751421249	67.557621

##	beta[4,95]	67.291735	13.835573	38.635527609	98.114346
##	beta[5,95]	31.157622	14.798585	0.423109146	61.808388
	beta[6,95]	58.797763	13.760962	30.428505922	88.359082
##	beta[7,95]	38.219543	14.111109	7.659775227	68.122932
##	beta[8,95]	47.887089	3.881354	39.044230588	54.968705
##	beta[9,95]	49.479677	12.289840	24.946801583	75.346613
##	beta[10,95]	29.365906	13.664192	-0.213591842	58.101443
##	beta[11,95]	47.347834	4.890665	35.075989258	55.801208
##	beta[12,95]	68.907631	14.009427	39.882085597	98.965252
##	beta[13,95]	30.250757	13.794187	0.966625646	59.564176
##	beta[1,96]	58.470147	14.341229	28.007354065	88.063465
##	beta[2,96]	59.383379	14.237811	29.223881702	89.960092
##	beta[3,96]	36.475569	14.603313	5.961839464	67.878356
##	beta[4,96]	67.350706	13.927575	37.466005696	98.781810
##	beta[5,96]	31.162449	14.892975	0.126986471	62.037761
##	beta[6,96]	58.780786	13.841211	30.246819785	88.557202
##	beta[7,96]	38.221740	14.146828	7.631020547	68.156196
##	beta[8,96]	47.991230	3.794238	39.499304572	55.092858
##	beta[9,96]	49.464369	12.330496	24.615125709	75.509600
##	beta[10,96]	29.368463	13.689555	-0.216200567	58.211732
##	beta[11,96]	47.339879	4.907446	35.113948413	55.753835
##	beta[12,96]	68.898168	14.006979	40.346360446	99.261886
##	beta[13,96]	30.230053	13.894176	0.599638460	59.102963
##	beta[1,97]	58.422051	14.347631	27.440604529	87.708792
##	beta[2,97]	59.398398	14.426555	29.321168830	89.977041
##	beta[3,97]	36.505868	14.654644	6.446507279	68.574365
##	beta[4,97]	67.429649	13.999151	37.503238721	98.338374
##	beta[5,97]	31.144112	14.839137	0.589855152	62.221399
##	beta[6,97]	58.761657	13.933559	29.533231026	87.842365
##	beta[7,97]	38.225421	14.214132	7.572076666	68.382226
##	beta[8,97]	48.076125	3.620083	39.799179406	54.741156
##	beta[9,97]	49.474629	12.407843	24.576602727	75.102741
##	beta[10,97]	29.372509	13.779314	-0.445664576	58.307552
##	beta[11,97]	47.347251	4.941268	34.937497435	55.833838
##	beta[12,97]	68.906167	14.087631	39.478769479	99.224588
##	beta[13,97]	30.274044	13.866641	-0.427158997	59.006927
##	beta[1,98]	58.463782	14.395777	28.194444764	88.065125
##	beta[2,98]	59.413152	14.516360	28.938822420	90.159595
##	beta[3,98]	36.505273	14.664654	5.487817382	68.163572
##	beta[4,98]	67.406780	14.070760	37.725935495	98.268650
##	beta[5,98]	31.138782	14.779542	0.261473277	61.977819
##	beta[6,98]	58.772726	13.974799	28.728758701	88.659861
##	beta[7,98]	38.242399	14.276853	7.442526449	67.969882
##	beta[8,98]	48.043589	3.860131	39.149747167	55.251722
##	beta[9,98]	49.450973	12.425590	23.712587454	75.378349
##	beta[10,98]	29.401973	13.869587	-0.009670088	58.381403
##	beta[11,98]	47.395392	4.943761	35.110375281	56.209231
##	beta[12,98]	68.932335	14.140465	39.908564843	99.154203
##	beta[13,98]	30.268511	13.976989	-0.305729195	59.415597
##	beta[1,99]	58.499174	14.510359	28.097884337	89.147595
##	beta[2,99]	59.418196	14.563652	29.156445006	90.238250
##	beta[3,99]	36.490699	14.699476	5.878880701	69.284636

##	beta[4,99]	67.419464	14.146375	37.704625936	98.283254
##	beta[5,99]	31.165018	14.708415	0.301018704	61.902421
##	- , -	58.843354		29.205962075	88.766827
	beta[7,99]	38.220541		7.338553207	69.052431
	beta[8,99]	48.042217	4.127688	38.219562586	55.815799
##	beta[9,99]	49.478334	12.547817	23.555054498	75.477932
##	beta[10,99]	29.414188	13.925284	-0.218125998	58.993668
	beta[11,99]	47.465187	4.987996	34.776077602	56.146041
##	beta[12,99]	68.923579	14.223529	39.798434781	99.758196
##	beta[13,99]	30.246880	14.110841	-0.572031303	60.071933
##	beta[1,100]	58.534356	14.670160	27.492948858	89.026205
##	beta[2,100]	59.460839	14.643741	29.342075834	91.052187
##	beta[3,100]	36.435958	14.797745	5.795247637	69.327556
##	beta[4,100]	67.454667	14.189188	37.535697856	98.773128
##	beta[5,100]	31.148354	14.851306	0.798445748	62.431481
##	beta[6,100]	58.827908	14.055433	29.144694590	89.412444
##	beta[7,100]	38.208685	14.532615	7.872218580	68.988919
##	beta[8,100]	48.073761	4.366229	38.166698215	56.229272
##	beta[9,100]	49.466808	12.539796	23.947357982	75.294324
##	beta[10,100]	29.371451	14.032972	-0.209541674	59.131644
##	beta[11,100]	47.501948	4.987343	34.834993438	56.538364
##	beta[12,100]	68.922751	14.295474	39.827583202	99.836571
##	beta[13,100]	30.348948	14.185084	-0.816649133	60.599818
##	beta[1,101]	58.529822	14.724542	27.827608597	89.306480
##	beta[2,101]	59.453514	14.723742	28.725260014	91.317838
##	beta[3,101]	36.423404	14.836332	5.729896311	68.904759
##	beta[4,101]	67.410830	14.314282	37.623476356	98.391202
##	beta[5,101]	31.174707	15.053658	0.462350540	62.434975
##	beta[6,101]	58.832297	14.126485	28.907162929	89.093957
##	beta[7,101]	38.222217	14.623938	7.644012334	69.202068
##	beta[8,101]	48.107596	4.542158	37.428722570	57.044382
##	beta[9,101]	49.413702	12.665056	23.668460312	75.561908
##	beta[10,101]	29.401776	14.115092	-1.331262971	58.578592
##	beta[11,101]	47.561980	5.012752	34.776263139	56.554404
##	beta[12,101]	68.901387	14.392575	39.213791642	100.067515
##	beta[13,101]	30.360479	14.249116	-0.712555535	60.370076
##	beta[1,102]	58.521702	14.913876	27.187243468	89.117030
##	beta[2,102]	59.457708	14.812161	28.746759008	91.098138
##	beta[3,102]	36.410562	14.844185	5.917651220	69.210490
##	beta[4,102]	67.415961	14.337409	37.846790360	98.265397
##	beta[5,102]	31.162766	15.211181	0.413221855	62.510389
##	beta[6,102]	58.859362	14.100761	28.848892298	90.078939
##	beta[7,102]	38.238055	14.680565	6.986384293	69.468690
##	beta[8,102]	48.106959	4.724519	37.344831468	57.142700
##	beta[9,102]	49.375945	12.804696	23.648705129	75.467155
##	beta[10,102]	29.440138	14.205465	-0.855583642	59.038375
##	beta[11,102]	47.617317		34.971509545	56.656813
##	beta[12,102]	68.889719		39.662058718	99.865979
##	beta[13,102]	30.369069		-0.266364472	61.134376
##	beta[1,103]	58.517287		28.930458941	89.328765
##	beta[2,103]	59.486934		29.014057882	91.565093
##	beta[3,103]	36.422907	14.861680	5.989911688	69.054668

	beta[4,103]	67.423203		37.246279328	98.364621
	beta[5,103]	31.144332		0.158879528	63.396573
	beta[6,103]	58.851272		29.200453354	89.785004
	beta[7,103]	38.313594		7.456951065	69.719509
	beta[8,103]	48.158270		37.094423327	57.823683
	beta[9,103]	49.388000		23.677683052	76.523458
	beta[10,103]	29.425878		-1.136299170	59.025516
	beta[11,103]	47.672236		34.770470366	56.700244
##	beta[12,103]	68.871270		38.418041527	100.122615
##	beta[13,103]	30.411603		-1.139135510	60.704431
##	beta[1,104]	58.544594		26.909723825	90.038070
	beta[2,104]	59.515983	14.852131	28.966174975	91.372763
	beta[3,104]	36.434451	14.952258	5.650089117	68.880497
	beta[4,104]	67.437531		37.345534276	98.581485
	beta[5,104]	31.174100	15.365335	0.163437593	63.238677
##	beta[6,104]	58.854444	14.231139	28.978202559	90.022006
##	beta[7,104]	38.313777	14.902038	7.353152015	71.417893
##	beta[8,104]	48.148655	5.052438	36.621283000	58.037955
##	beta[9,104]	49.389890	12.927949	24.090460257	76.376971
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##	beta[11,104]	47.744162	4.990501	34.818052656	56.747213
##	beta[12,104]	68.878453	14.583227	37.113884658	99.586788
##	beta[13,104]	30.373950	14.371021	-0.757236832	61.354466
##	beta[1,105]	58.552910	15.130429	27.162968167	91.401876
##	beta[2,105]	59.496220	14.948010	28.535133470	92.355080
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##	beta[4,105]	67.405996	14.530614	37.242263226	98.466239
##	beta[5,105]	31.145710	15.594986	-0.460060907	63.726685
##	beta[6,105]	58.855607	14.311385	28.212065465	89.021862
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##	beta[11,105]	47.799051	5.029693	34.817944439	57.072574
##	beta[12,105]	68.872178	14.590462	37.946993600	99.943065
##	beta[13,105]	30.388877	14.463342	0.262617665	61.282308
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##	beta[2,106]	59.518113	14.994128	28.695201146	92.130398
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##	beta[7,106]	38.303126	14.996612	6.677285931	70.075741
##	beta[8,106]	48.156693	5.603683	35.936097054	58.794730
##	beta[9,106]	49.415531	13.073247	23.124763105	76.460347
##	beta[10,106]	29.448561		-1.463237263	59.269382
	beta[11,106]	47.846381		34.818447099	57.062207
	beta[12,106]	68.882775		38.077909283	99.770044
##	beta[13,106]	30.389892		-0.223573344	61.912249
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	beta[2,107]	59.526814		27.775031205	91.781373
	beta[3,107]	36.460840	15.142161	4.844790553	68.865694
11	2300[0,101]	20.100010	10.112101	1.011,00000	JJ.JJJJJ7

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                                             6.950172900
##
  beta[8,107]
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                                                           76.383584
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                     30.348519
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                                                           90.849436
## beta[2,108]
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                                                           92.331898
                     59.538989
## beta[3,108]
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                                             5.113834547
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## beta[4,108]
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                                                           98.880791
## beta[5,108]
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                                                           63.992782
## beta[6,108]
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                     58.874570
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                                                           71.870207
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                                                           76.848945
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                                                           61.679571
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                     29.402153
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                                                           98.904479
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                                                           91.233327
## beta[2,111]
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                     59.515223
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                                                           69.400622
```

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                     59.553275
## beta[3,112]
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## beta[4,112]
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## beta[7,112]
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                                             6.068094473
                                                           72.499084
## beta[8,112]
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                                                           60.361278
## beta[9,112]
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                                                           77.500670
## beta[10,112]
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                     29.340805
                                                           59.783853
                     48.046158
## beta[11,112]
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## beta[13,112]
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                                                           62.138620
## beta[1,113]
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                                                           91.472426
## beta[2,113]
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## beta[3,113]
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                                                           70.483131
## beta[4,113]
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## beta[2,114]
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## beta[3,114]
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## beta[7,115]
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                                                           72.553018
## beta[8,115]
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## sigma2_beta[12]
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                                                            9.788253
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## sigma2_y[5]
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## sigma2_y[6]
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```

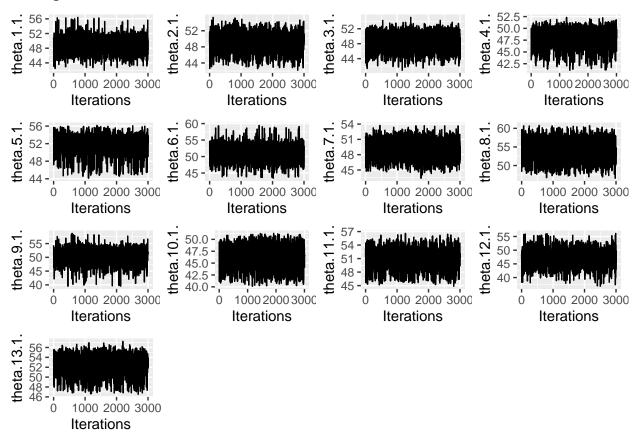
## mean Rhat: 1.12697

## mean effective sample size: 1698.656

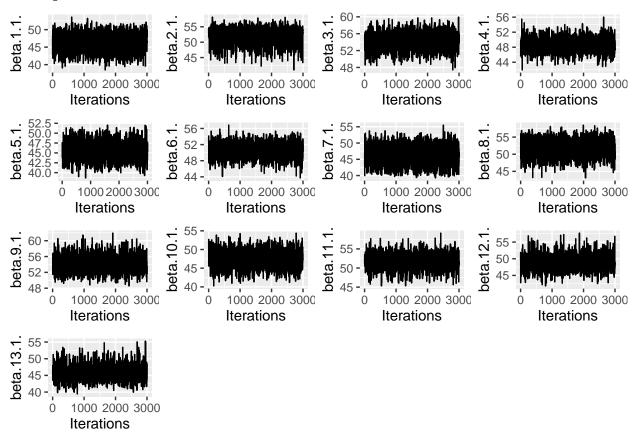
## Appendix B

# Appendix C

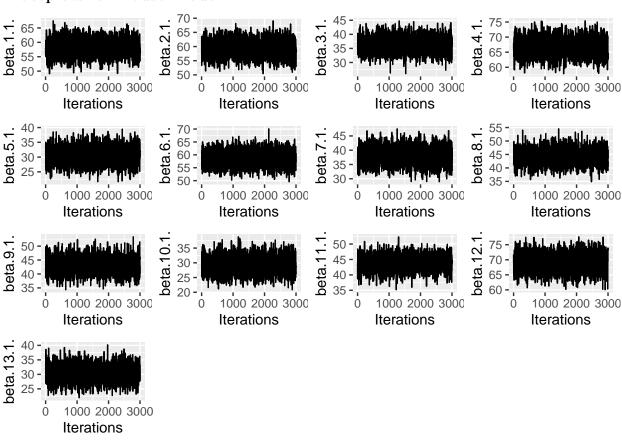
## Traceplots for Presidential Model



### Traceplots for Senate Model



#### Traceplots for House Model



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#### Additional EDA

#### Map For The Number of Filtered Polls Among States

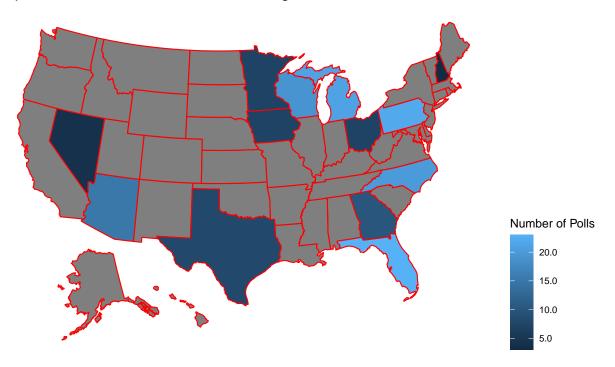


Figure 9: Additional Presidential Election Data Visualization

# Map For The Number of Filtered Polls Among States

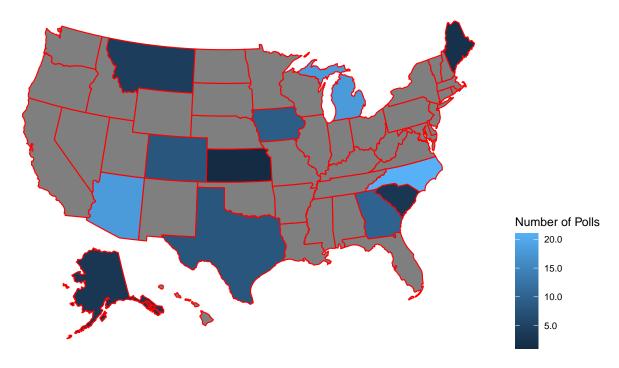


Figure 10: Additional Senate Election Data Visualization