

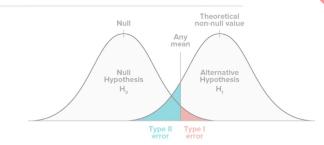


DATA SCIENCE

TRAINING PROGRAM

Hypothesis Testing

Larissa Leite Kodit.io











Outline

- What is hypothesis testing?
- Steps
 - a. Make assumptions
 - b. Conduct fact based tests
 - Types of tests
 - c. Evaluate results
 - d. Reach a conclusion









What is hypothesis testing?

First things first

- Hypothesis ≈ assumption
 - o If I...(do this to an *independent variable*)....then... (this will happen to the *dependent variable*)

- What types of assumptions?
 - Distribution
 - Normal
 - Sampling
 - Data sample is randomly selected, no bias
 - Linearity
 - Two variables have a linear relationship









What is hypothesis testing?

- The process of verifying whether a hypothesis should be accepted or rejected by performing statistical tests
 - More specifically, whether an initial hypothesis can be rejected

- Test on the results of a survey or experiment to see if they are meaningful
 - O What are the odds that the results happened by chance?









What is hypothesis testing?

- In the industry, it is widely used to test the effect of a new feature, a new campaign
 - Basically, determining whether something has a significant impact on a given question that needs to be answered, or statement that needs to be validated:

"We think customers order different quantities of products when offered a discount"

In data science, it is often used to test relationship between variables







What is hypothesis testing? Steps

- 1. Make assumptions
 - a. Take an initial position
 - b. Determine the alternate position
- Conduct fact based tests
 - a. Sampling
 - b. Decide which test is appropriate
 - c. Set acceptance criteria
- 3. Evaluate results
 - a. Does the evaluation support the initial position? Are we confident that the result is not due to chance?
- 4. Reach one of the following conclusions:
 - a. Reject the original position in favor of alternate position or fail to reject the initial position









What is hypothesis testing? Steps

- Make assumptions
 - Take an initial position a.
 - Determine the alternate position









H0: NULL hypothesis

Initial position (default, what is already known) that needs to be proven wrong







H1(a): Alternative hypothesis

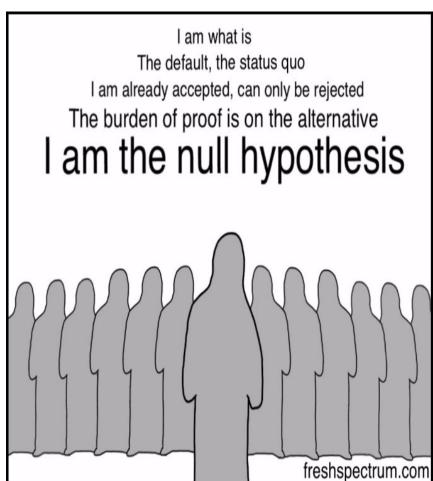
Contrary position to the NULL hypothesis























Example

"We think customers order different quantities of products when offered a discount"

H0: Discount does not have an effect on the number of products ordered by a customer.

H1: Discount has an effect on the number of products ordered by a customer.









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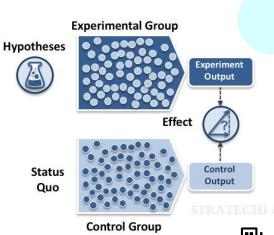




Data collection Sampling

- Getting enough observations from a larger population that allows conclusions to be drawn
 - Often random
 - Representative
 - Stratified sampling

Control vs experimental group











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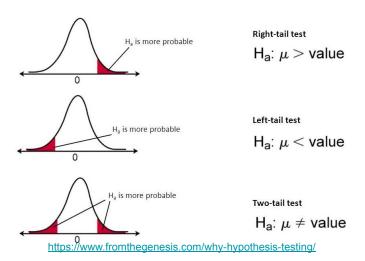






Decide which test is appropriate

 A test statistic is selected in order to quantify, within observed data, the distinction between the null and the alternative hypothesis











Decide which test is appropriate

Highly depends on the type of the problem and on the data

Check the test's assumptions before using them!









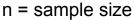
How to test our hypothesis? **Z**-test

- Compares the sample to the population
- Test proportion
 - Outlier removal
- Assumptions
 - Data points should be independent from each other
 - Random sampling from a population
 - Sample is assumed to be normally distributed (N > 30)
 - Population mean and standard deviation are known
- Z-score is measured in standard deviations (standardization)

$$Z = \frac{X - \mu}{\sigma / \sqrt{n}}$$

$$X$$
= sample mean μ = population mean σ = population standard deviation

$$\sigma$$
 = population standard deviation











T-test

- When comparing two samples: is there a statistically significant difference?
- Assumptions
 - Population standard deviation is unknown, samples are from a normally distributed population
 - Variance between the samples must be equal, otherwise use Welch's t-test
- T-score
 - Ratio of the difference between two groups: the larger the t-score, the larger the difference
- Different types
 - Independent samples t-test which compares mean for two different groups
 - Paired sample t-test which compares means from the same group at different times
- Hypothesis:
 - H0: the means of the samples are equal
 - H1: the means of the samples are different











- Analysis of variance, used to compare multiple samples with a single test
 - Compares the difference between the three or more samples/groups of a single independent variable
- Assumptions
 - The samples are independent
 - Each sample is from a normally distributed population
 - Variance between the samples must be equal
 - o If the assumptions are not met, Kruskal-Wallis test could be an alternative
- Hypothesis:
 - H0: all pairs of samples are same, i.e. all sample means are equal
 - H1: at least one pair of samples is significantly different











How to test our hypothesis? Chi-square

Used to compare categorical variables

- Goodness of fit test
 - Determines if a sample matches the population

- A chi-square test for two independent variables
- Hypothesis:
 - H0: Variable A and Variable B are independent
 - o H1: Variable A and Variable B are not independent











How to test our hypothesis? Chi-square

Example

 In an election survey, voters might be classified by gender (male or female) and voting preference (Democrat, Republican, or Independent)

- We could use a chi-square test for independence to determine whether gender is related to voting preference
 - Correlation between categorical variables







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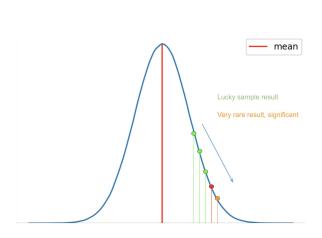






Significance level

- Output from the test statistics
- Select a significance level (α), a probability threshold below which the null hypothesis will be rejected. Common values are 5% (standard) and 1%









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Tests results

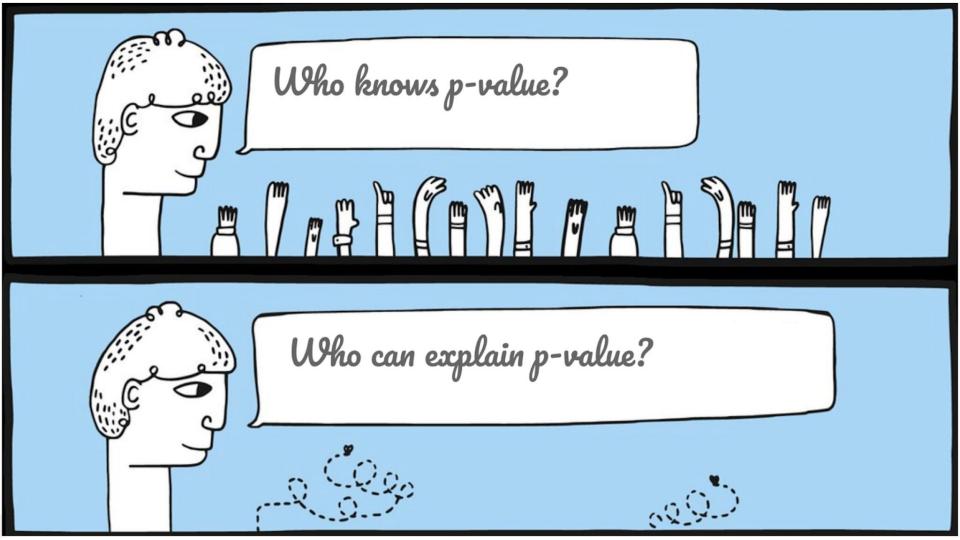
- From the scores, we can calculate the p-values
 - o Z-table, t-table

 Libraries often provide the score and the corresponding p-value as part of the output of an statistical test

from scipy.stats import ...

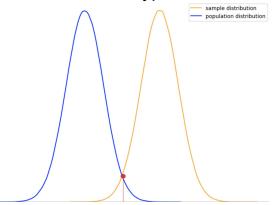








- Probability value (p-value) is the probability that, when the null hypothesis is true, the statistical-test result would be equal to (or more extreme than) the actual observed results
- p-value does not hold any value by itself
 - A large p-value implies that sample scores are more aligned or similar to the population score:
 our data is highly consistent with our null hypothesis













- How do you interpret a p-value?
- How much importance should we place in the p-value?
- How will you explain the significance of p-value to a non-data science person (a stakeholder for example)?







p-values in Data Science

- p-value is an important metric in the process of feature selection
 - Find out the best subset of the independent variables to build the model
 - Throwing in redundant and non-contributing variables adds complexity to the model
 - They can reduce the model performance in terms of accuracy and runtime







p-values in Data Science

Example

- Consider a dataset that contains the following information about different startups, for which we wanna predict the profit:
 - State California
 - O State Florida
 - O R&D spend
 - Administration
 - Marketing spend
- **H0**: The independent variable has no significant effect over the target variable
- **H1**: The independent variable has a significant effect on the target variable











p-values in Data Science

Example

 All the variables, except R&D Spend have a p-value over 0.05

Can they be removed from the dataset?

OLS Regression Results

Dep. Variable:	У	R-squared:	0.951					
Model:	OLS	Adj. R-squared:	0.945					
Method:	Least Squares	F-statistic:	169.9					
Date:	Tue, 03 Sep 2019	Prob (F-statistic):	1.34e-27					
Time:	09:22:23	Log-Likelihood:	-525.38					
No. Observations:	50	AIC:	1063.					
Df Residuals:	44	BIC:	1074.					
Df Model:	5							
Covariance Type:	nonrobust							

	coef	std err	t	P> t	[0.025	0.975]
Intercept	5.013e+04	6884.820	7.281	0.000	3.62e+04	6.4e+04
data[0]	198.7888	3371.007	0.059	0.953	-6595.030	6992.607
data[1]	-41.8870	3256.039	-0.013	0.990	-6604.003	6520.229
data[2]	0.8060	0.046	17.369	0.000	0.712	0.900
data[3]	-0.0270	0.052	-0.517	0.608	-0.132	0.078
data[4]	0.0270	0.017	1.574	0.123	-0.008	0.062
					'	







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Outcomes

- 1. Reject the NULL hypothesis
 - If there are statistically significant evidences that suggest that the alternate hypothesis is valid,
 then the NULL hypothesis is rejected

2. Fail to reject the NULL hypothesis







Type I and Type II errors

- Type I error (false positive)
 - Rejection of a true null hypothesis

 Usually leads to the conclusion that a supposed effect or relationship exists when in fact it does not

Type II error (false negative)

The failure to reject a false null hypothesis

Table of error types		Null hypothesis (H_0) is		
		True	False	
Decision about null hypothesis (<i>H</i> ₀)	Don't reject	Correct inference (true negative) (probability = 1 - a)	Type II error (false negative) (probability = β)	
	Reject	Type I error (false positive) (probability = a)	Correct inference (true positive) (probability = 1 - β)	



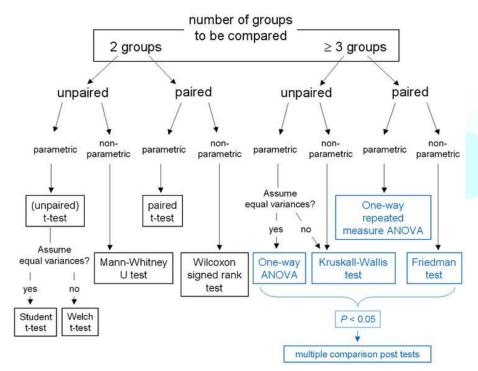






Summary

Continuous variables













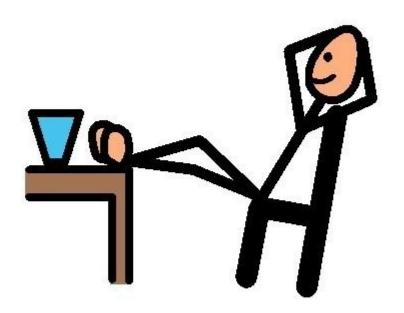
References

- [1] Test statistic
- [2] Hypothesis testing
- [3] Your guide to master hypothesis testing in statistics
- [4] <u>T-test</u>
- [5] Python for Data Analysis: Hypothesis testing and t-test
- [6] Chi-square test for Machine Learning
- [7] Statistical hypothesis testing in Python
- [8] Type I and Type II errors





break









(More) Data Visualization

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Know <u>what</u> you want to communicate and <u>who</u> you want to communicate to

- Should be concise
 - All the information
 - As simply as possible
- Should be perceivable
 - Easy to interpret







Libraries

import matplotlib.pyplot as plt

- Sometimes external libraries provide more options
- Seaborn
 - More visualizations than matplotlib; visually better defaults and color schemes
- Bokeh
 - Browser based; interactive visualizations
- Plot.ly
 - Online service with Python API
- D3.js
- Highcharts, Sigma JS (graphs)
- Tableau









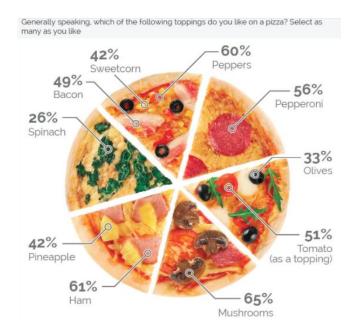
- ✓ Univariate distribution plots (histograms, densities)
- ✓ Scatter plots
- ✓ Summary statistic plots (bar charts)





















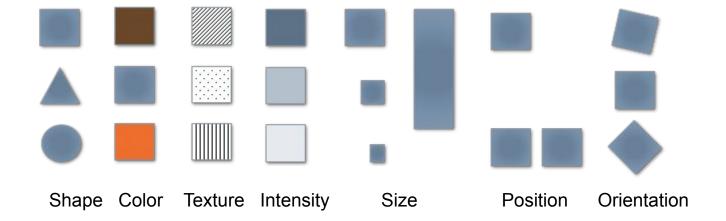








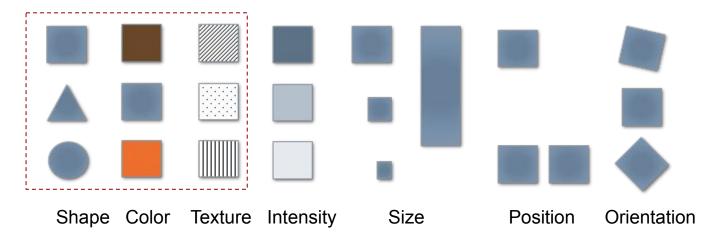










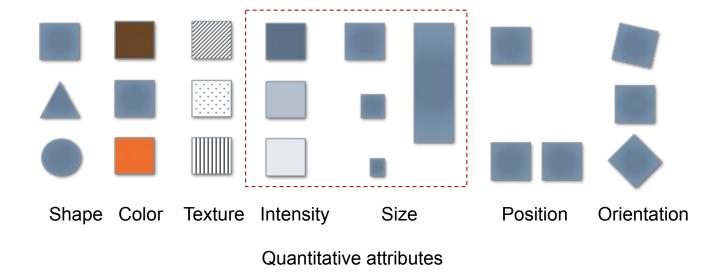


Distinguish different categories





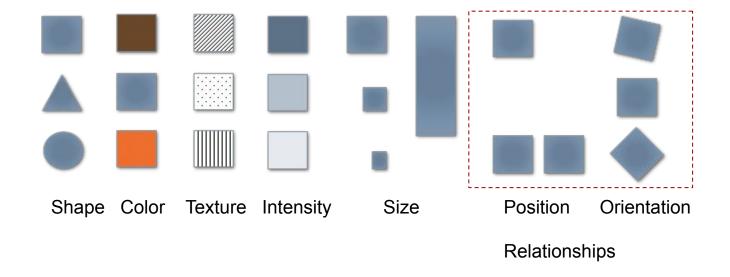








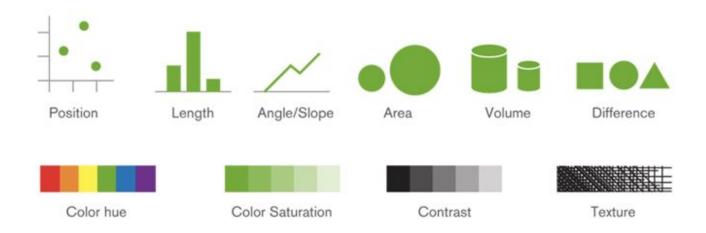










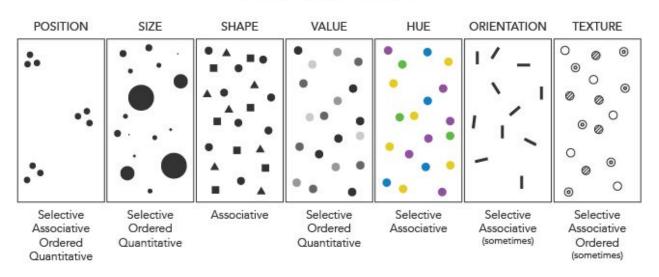








Bertin's Visual Variables



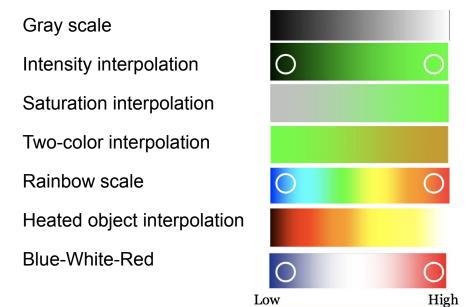






Color

 Given any 2 colors, make it intuitively obvious which represents "higher" and which represents "lower"











Color

Do not attempt to fight pre-established color meanings

Red	Green	Blue
Stop Off Dangerous Hot High stress Money loss	On Plants/nature Moving Money	Cool Safe Nitrogen







Visualization Color

Attention to contrast!!!









Visualization Color

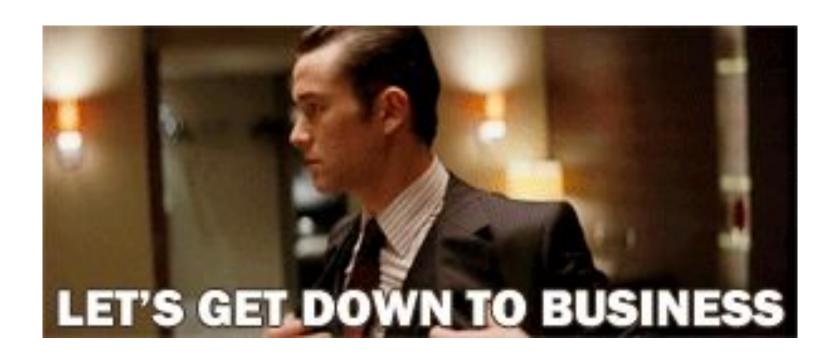
Attention to contrast!!!

I would prefer that my life depend on being able to read this quickly and accurately!





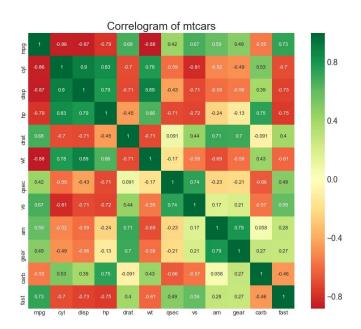






Visualization Correlogram

Plot correlations between (all) the variables, a specific kind of heat map

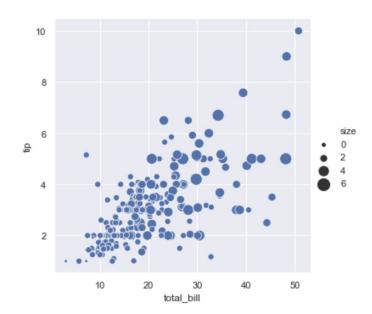








Relationship between two or more numerical variables

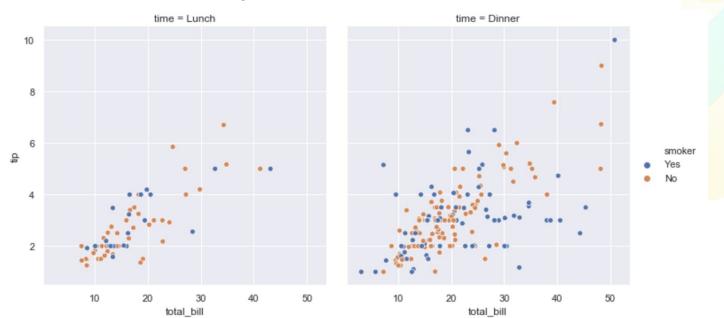








Relationship between categorical and numerical variables





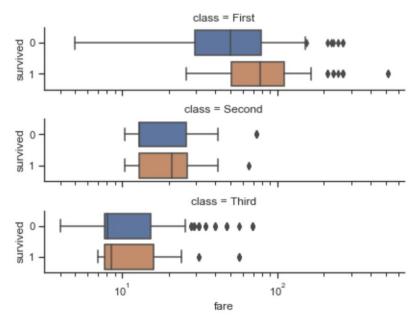






Visualization Facet plot

Multivariate relationships



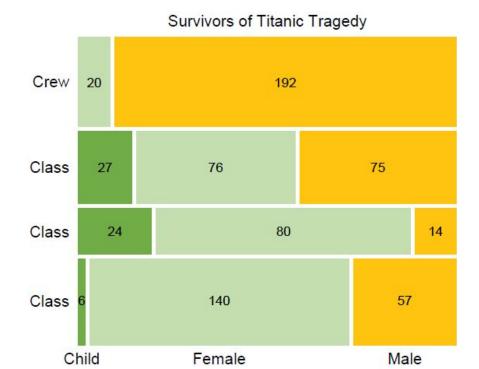






Visualization Mosaic Plot

Relationship between two or more categorical variables





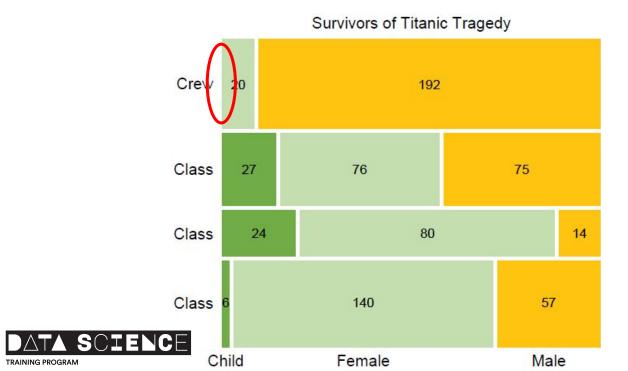






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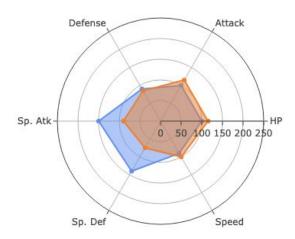




Visualization Radar chart

Spider web that indicates variables and their values used to compare two (or more) entities; thresholds are often used

Kyogre vs. Entei





KyogreEntei



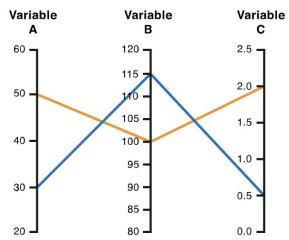


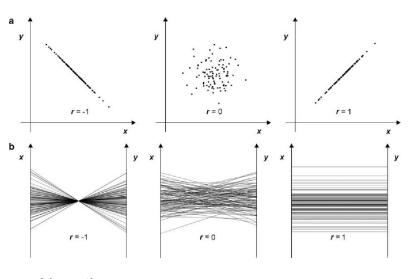


Visualization Parallel coordinates

Used to compare many numerical variables and their relationships

Data				
	Variable A	Variable B	Variable C	
	50	100	2.0	
Item 2	30	115	0.5	





Negative correlation

No correlation

Positive correlation



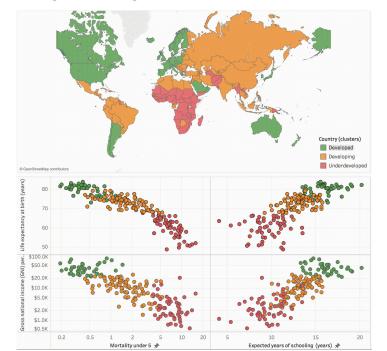






Visualization Clustering

If it gets too cluttered.... grouping can help!









Visualization Maps

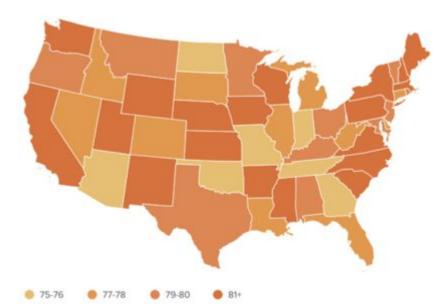
Leaflet.js, Mapbox

Zoomed-in map with points of interest



Number of sales by state

What about the color selection? Is it easy to tell them apart?



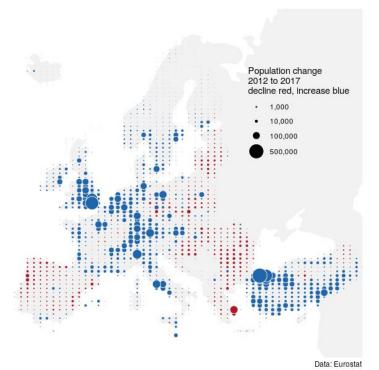


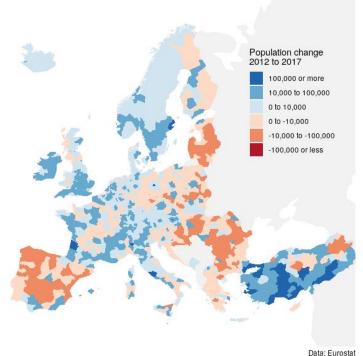






Visualization Maps





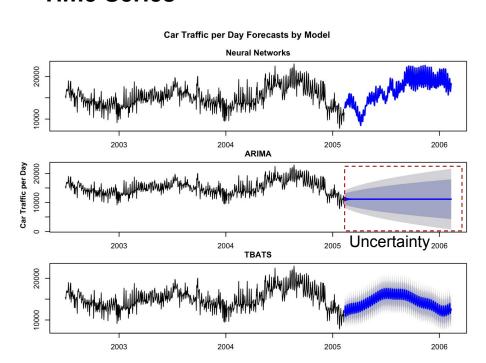


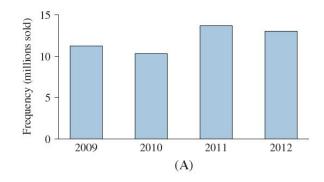


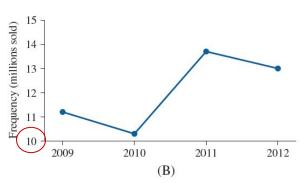




Visualization Time Series









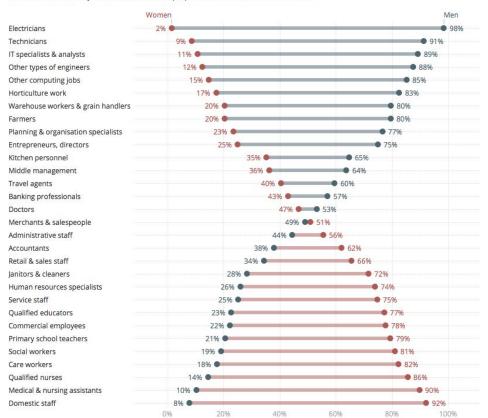








The 30 most common jobs in Switzerland and proportion of men and women in each



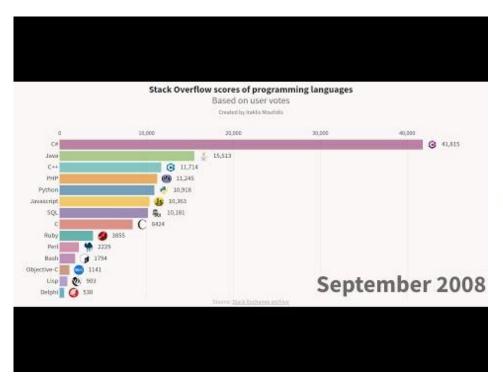










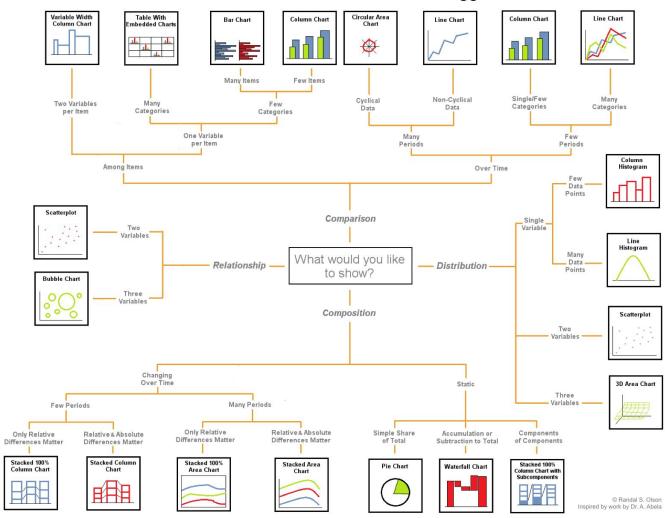








The chart selector — some basic chart suggestions





References

- [1] The Data Visualization Catalogue
- [2] From Data to Viz
- [3] Information Visualization
- [4] Introduction to Information Visualization
- [5] <u>Tamara Munzner: Data visualization talks</u>
- [6] 20 visualization tools
- [7] Seaborn tutorial



