Math 112 LQuiz 11

2022-03-01 (T)

Your name:	

Exercise

(4 pt) Take as given the following "infinite polynomial" expression for cos x:

$$\cos x = 1 - \frac{1}{2}x^2 + \frac{1}{24}x^4 - \frac{1}{720}x^6 + \frac{1}{40320}x^8 - \dots$$

$$= 1 - \frac{1}{2}x^2 + \frac{1}{24}x^4 + O(x^6)$$
(1)

(Recall that $O(x^6)$ means "terms involving x to powers 6 and higher".) Consider the limit

$$\lim_{x \to 0} \frac{1 - \cos x - \frac{1}{2}x^2}{x^4} \tag{2}$$

(a) (2 pt) Compute the limit in (2) by substituting (1) for $\cos x$, simplifying, and evaluating.

(b) (2 pt) Compute the limit in (2) by iteratively applying l'Hôpital's rule. (You should apply l'Hôpital's rule four times. Briefly show it applies each time you use it!) Confirm you get the same result you got in part (a).