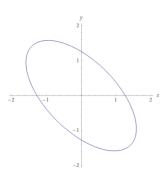
Math 112 ReQuiz 07A

2022-04-03 (N)

Exercise

(4 pt) Consider the ellipse graphed below, given by the equation

$$5x^2 + 6xy + 5y^2 = 8 (1)$$



(a) (1 pt) From the graph, the points $(x,y)=(\pm\sqrt{2},\mp\sqrt{2})\approx(\pm1.414,\mp1.414)$ appear to be on the ellipse. Prove this, algebraically.

(b) (1 pt) From the graph, what do you predict about the slope of the tangent line to the graph at the point $(-\sqrt{2}, \sqrt{2})$?

(c) (2 pt) Compute the rule of assignment for y'. (Your answer will involve both x and y.) Show that y' evaluated at the point $(x,y) = (-\sqrt{2},\sqrt{2})$ equals 1. How does this relate to part (b)?