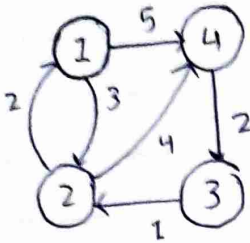


# Floyd Warshall Algorithm.

Floyd Warshall algorithm is an algorithm for finding shortest path between all the pairs of vertices in a weighted graph. This algorithm works for both the directed and undirected weighted graphs. But it does not work for graphs with negative cycles.

Steps:-



1. Create matrix  $A_0[n][n]$ ,  $\{n$  is number of vertices $\}$  if edge exists, write the weight, else  $\infty$ .

$$A_0 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & \infty & 4 \\ \infty & 1 & 0 & \infty \\ \infty & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

2. Now create another matrix  $A_1$  using  $A_0$ , keep the first row and first column as it is, change the values of other cells, consider  $k$  as the node on vertex in between  $A[i][k]$  and  $A[k][j]$ ,

$$A[i][j] = (A[i][k] + A[k][j]) \text{ if } (A[i][j] > A[i][k] + A[k][j])$$

if sum of path of via, via  $k$  weight is less than change  $A[i][j]$  to that weight.

$$A_1 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & \infty & 5 \\ 2 & 0 & 9 & 4 \\ \infty & 1 & 0 & 8 \\ \infty & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

3. create  $A_2$  using  $A_1$ , keep 2,2 same

$$A_2 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 9 & 5 \\ 2 & 0 & 9 & 4 \\ 3 & 1 & 0 & 5 \\ \infty & \infty & 2 & 0 \end{bmatrix} \end{matrix}$$

4. same for  $A_3$ ,

$$A_3 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 9 & 5 \\ 2 & 0 & 9 & 4 \\ 3 & 1 & 0 & 5 \\ 5 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

5. Now  $A_4$ ,

$$A_4 = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 3 & 7 & 5 \\ 2 & 0 & 6 & 4 \\ 3 & 1 & 0 & 5 \\ 5 & 3 & 2 & 0 \end{bmatrix} \end{matrix}$$

You have to iterate 0 to  $n$  times, to get the final answer.

← This is the final matrix containing shortest paths between each nodes.