

## Unit 2

### Introduction to quantum computing

→ qubit

symbols for states in QC

States 0, 1

Classical bit

→ pure state

$|0\rangle, |1\rangle$

→ qubits / quantum bits

- Superimposition (combination of both)

$$\alpha|0\rangle + \beta|1\rangle$$

real

complex

ex - Tomorrow there will belec or not of QC

Tomorrow lec - Yes, No

0.8 0.1

$0.8|0\rangle$

b

yes

$0.2|1\rangle$

↓

No

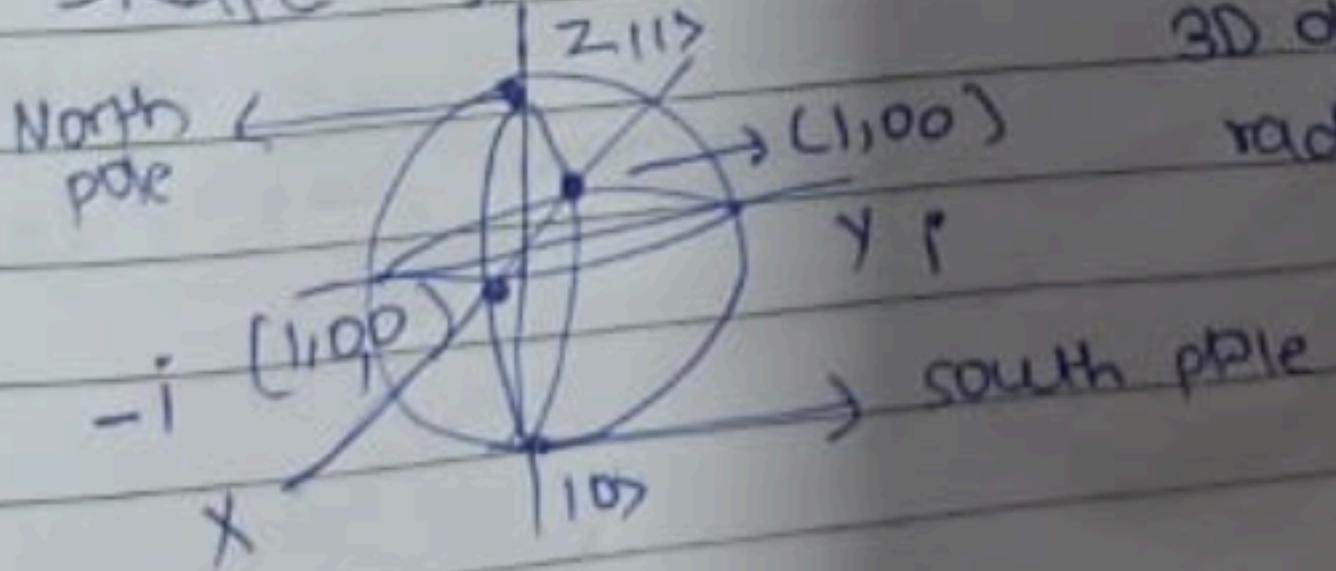
yesterday lec - yes

ket  $\rightarrow 0$

ket  $\rightarrow 1$

\* geometrical interpretation / visualising qubit

Shape  $\rightarrow$  sphere [Bloch]



3D object  
radius

$r = \text{mm/cm/km}$   
1 unit



$$|\psi\rangle = \frac{1}{\sqrt{2}}(|+> + |->)$$

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|+> - |->)$$

$$\frac{\sqrt{3}}{2}|\psi\rangle + \frac{1}{2}|n\rangle$$

$$\frac{\sqrt{3}}{2}|\psi\rangle + \frac{1}{2}|n\rangle +$$

$$\frac{\sqrt{3}-1}{2}\frac{1+i}{\sqrt{2}} + \frac{\sqrt{3}-1}{2}\frac{1-i}{\sqrt{2}} = \frac{-i}{2\sqrt{2}}|1> + \frac{1}{2\sqrt{2}}|1-i>$$

$$\frac{1}{2}\cdot\frac{1}{\sqrt{2}}|+> + \frac{1}{2}\cdot\frac{1}{\sqrt{2}}|->$$

$$\frac{\sqrt{3}-1}{2}\frac{1+i}{\sqrt{2}} + \frac{\sqrt{3}+1}{2\sqrt{2}}|1>$$

$$\frac{\sqrt{3}+1}{2\sqrt{2}}|1+i> + \frac{\sqrt{3}-1}{2\sqrt{2}}|1-i>$$

$$|\psi\rangle = \left(\frac{\sqrt{3}+1}{2\sqrt{2}}\right)^2 = \frac{(\sqrt{3}+1)^2}{2\sqrt{2}}$$

$$|\psi\rangle = \frac{\sqrt{3}+1}{2\sqrt{2}} \quad |\psi|^2 = \frac{(\sqrt{3}+1)(\sqrt{3}+1)}{2\sqrt{2}} = \frac{1}{2}$$

$$= 0.93$$

$$= 0.207$$

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|+> + |->)$$

$$|\psi\rangle = \frac{1}{\sqrt{2}}(|+> - |->)$$

• Normalization

$$\alpha^2 + \beta^2 = 1 \rightarrow \text{Normalized quantum state}$$

$$2 \cdot \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$

$$\left(\frac{1}{\sqrt{2}}\right)^2 + \left(\frac{1}{\sqrt{2}}\right)^2 = \frac{1}{2} + \frac{1}{2} = 1 \quad \checkmark$$

- Normalization constant =  $\frac{1}{\sqrt{3}}$

$$\begin{bmatrix} \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \\ \frac{1}{\sqrt{3}} \end{bmatrix}$$

$$\frac{4}{9} + \frac{5}{9} = 1 - 2 \cdot \frac{4}{9} \cdot \frac{5}{9} = \frac{5}{9}$$

$$\alpha = \frac{2}{3}$$

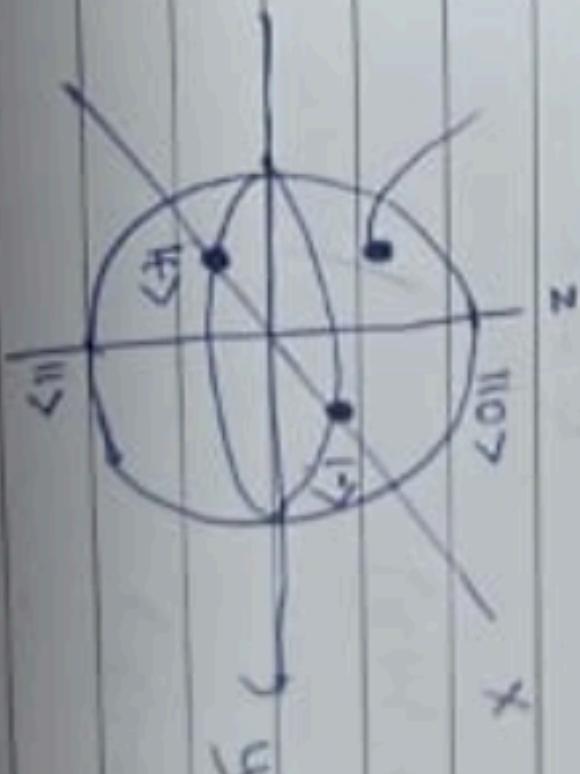
$$\beta = \frac{1-2i}{3}$$

$$|\psi\rangle = \frac{1}{\sqrt{3}} (|0\rangle - 2i|1\rangle + |2\rangle)$$

$$3.3.$$

$$\frac{1}{\sqrt{3}} (|0\rangle + i|1\rangle)$$

- Measurement collapses to a qubit
- Measurement w.r.t X-axis



$$|\psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle + e^{-i\pi/6}|1\rangle)$$

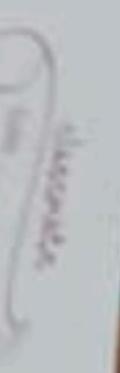
$$\frac{1}{\sqrt{2}} |0\rangle + \frac{e^{i\pi/6}}{\sqrt{2}} |1\rangle$$

$$\alpha = \frac{1}{\sqrt{2}}, \quad |\beta|^2 = \frac{e^{-i\pi/6}}{\sqrt{2}}$$

$$|\beta|^2 = \frac{1}{2} = e^{-i\pi/6} \times e^{i\pi/6} = 1$$

$$\frac{1}{2} + \frac{1}{2} = 1$$

X Complex num calculation of superposition



Dipole

$$|10\rangle \rightarrow (0,0,1) \quad |11\rangle = \frac{1}{\sqrt{2}}(|10\rangle + |11\rangle) \rightarrow (1,0,0); \quad |10\rangle + \frac{|10\rangle}{\sqrt{2}}$$

D

$$|10\rangle \rightarrow (0,0,-1) \quad |1\rangle = \frac{1}{\sqrt{2}}(|10\rangle + |11\rangle) \rightarrow (-1,0,0); \quad \frac{|10\rangle - |11\rangle}{\sqrt{2}} = \frac{|1\rangle}{\sqrt{2}}$$

B

A

C

D

E

F

G

H

I

J

K

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Q

R

S

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V

W

X

Y

Z

$$|11\rangle = \frac{1}{\sqrt{2}}(|10\rangle + |11\rangle)$$

Complex Num

$$2 = \frac{3}{2} + \frac{i\sqrt{3}}{2} \quad i = \sqrt{-1}$$

Real

Imag

$$2 = 3 + i\sqrt{3}$$

$$\alpha^2 + \beta^2 = 1 \quad \alpha = \frac{3}{2}, \beta = \frac{\sqrt{3}}{2}$$

function

1) Real : complex  $\rightarrow$  real

2) Imag : complex  $\rightarrow$  imag

\* complex number

Complex language	Rectangular
Cartesian	$z = x + iy$

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