



BITS Pilani

Hyderabad Campus

Department of Electrical Engineering



EEE/ECE F311

Communication Systems

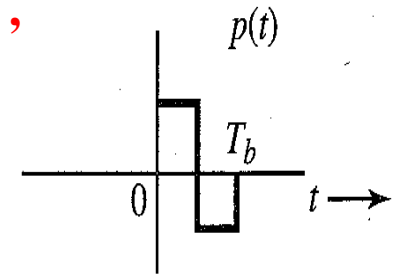
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Date : 30/10/2025

Date : 04/11/2025

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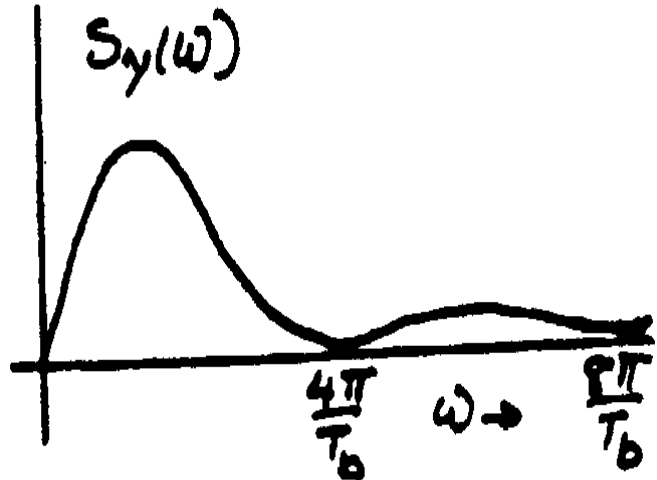
1. Derive $S_y(w)$, the PSD of the manchester (split phase) signal , assuming 1 and 0 are equally likely. Sketch the PSD



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Solution 1

$$S_y(\omega) = \frac{|P(\omega)|^2}{T_b} = T_b \operatorname{sinc}^2\left(\frac{\omega T_b}{4}\right) \sin^2\left(\frac{\omega T_b}{4}\right)$$



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2. A leased telephone of bandwidth 3 kHz is used to transmit binary data. Calculate the data rate (in bits per second) that can be transmitted if we use:
- (a) Polar signal with rectangular half-width pulses.
 - (b) Polar signal with rectangular full-width pulses.
 - (c) Polar signal using Nyquist criterion pulses of $r = 0.25$.
 - (d) Bipolar signal with rectangular half-width pulses.
 - (e) Bipolar signal with rectangular full-width pulses.

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Solution 2

(a) For Polar Signal:

$$R_b = B_T / 2 = 1.5 \text{ kbits / sec}$$

$$(b) p(t) = \text{rect}(t/T_b);$$

\Rightarrow Essential BW (B_T) = R_b : Hence, transmission bit rate = 3Kbits/sec

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Solution 2

c) $BT = 4800 \text{ bits/sec}$

d) $\text{Essential BW} = R_b$: Bit rate possible is 3 kbits/s

e)

Again for Bipolar Signal:

$\Rightarrow \text{Essential BW} = R_b$: BT ; Hence, transmission bit rate = 3Kbits/sec

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3. A 64 Kbps binary PCM Bipolar NRZ signal is passed through a communication system with a raised cosine filter with roll off factor 0.25. Determine the bandwidth of the PCM signal and the bandwidth of the filtered PCM signal.

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Solution 3

Nyquist BW= 32 KHz

BW of filtered PCM signal = 40 KHz

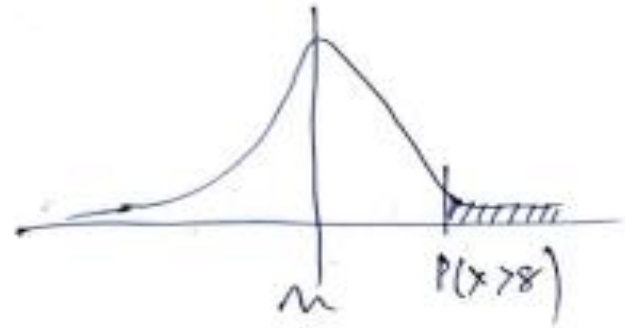
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4. For the Gaussian random variable, X with mean and standard deviation values are given as $\mu=5$ and $\sigma=2$, respectively. Find the probability values such as (a) $P(X>8)$, (b) $P(X<8)$ and (c) $P(3<X<8)$.

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Solution 4

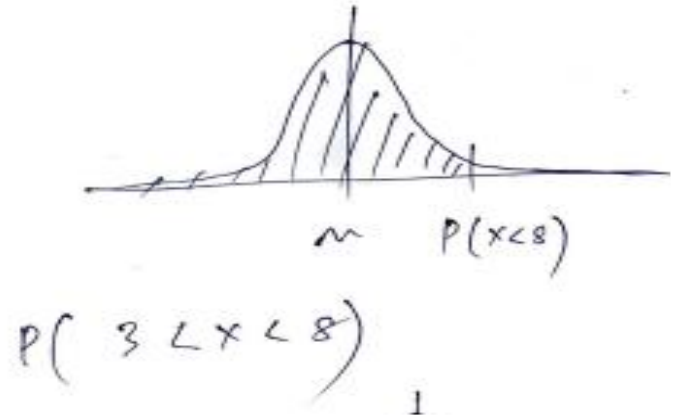
$$P(x > 8) = Q((x - \mu)/\sigma) = 0.066807$$



$$P(x < 8) = 1 - P(x > 8) = 1 - Q(1.5) = 0.933193$$

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Solution 4



$$P(3 < x < 8) = 1 - Q(1.5) - Q(1)$$

$$= 1 - 0.066807 - 0.15866 = 0.774533$$

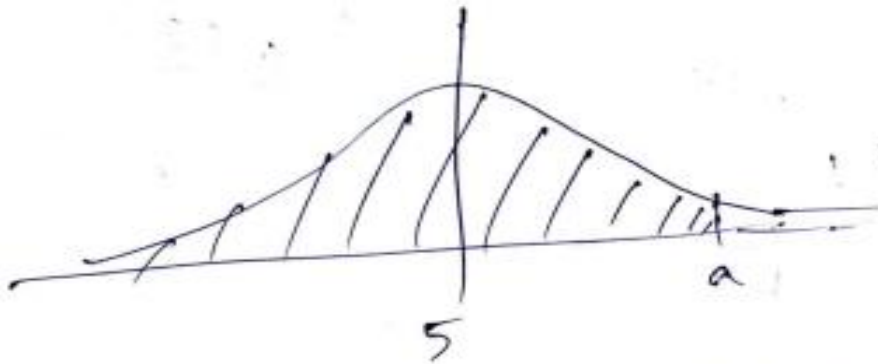
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5. For the Gaussian random variable, X with mean and standard deviation values are given as $\mu=5$ and $\sigma=3$, respectively. Find the factor a such that $P(X < a) = 0.9$

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Solution 5

Ans



$$P(X < a) = 0.9 \quad \Rightarrow \quad P(X > a) = 0.1$$

$$\Rightarrow \quad Q\left(\frac{a-5}{3}\right) = 0.1$$

Thus $\frac{a-5}{3} \approx 1.25$

$$\Rightarrow a = (1.25 \times 3) + 5$$

$$= 3.75 + 5 = 8.75$$

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6. For the Gaussian random variable, X with mean and standard deviation values are given as $\mu=5$ and $\sigma=3$, respectively. Find the factor a such that $P(3 < X < a) = 0.7$

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Solution 6

$$\begin{aligned} 2) \quad P(X > a) &= 1 - 0.95 = 0.05 \\ \Rightarrow Q\left(\frac{a-5}{3}\right) &= 0.05 & \Rightarrow \frac{a-5}{3} &= 1.60 \\ & & \Rightarrow a &= 4.8 + 5 \\ & & &= 9.8 \end{aligned}$$