



**BITS** Pilani

Hyderabad Campus

Department of Electrical Engineering



# **EEE/ECE F311**

# **Communication Systems**

## **Tutorial-11**

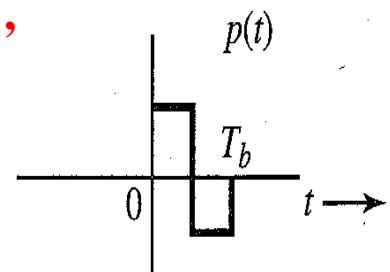
**Date : 30/10/2025**

**Date : 04/11/2025**



## Tutorial-11

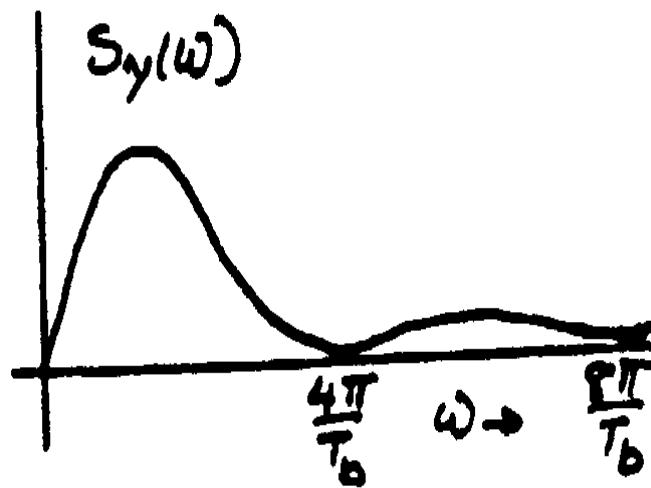
1. Derive  $S_y(w)$ , the PSD of the manchester (split phase) signal , assuming 1 and 0 are equally likely. Sketch the PSD



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## Solution 1

$$S_y(\omega) = \frac{|P(\omega)|^2}{T_b} = T_b \operatorname{sinc}^2\left(\frac{\omega T_b}{4}\right) \sin^2\left(\frac{\omega T_b}{4}\right)$$





## Tutorial-11

2. A leased telephone of bandwidth 3 kHz is used to transmit binary data. Calculate the data rate (in bits per second) that can be transmitted if we use:
- (a) Polar signal with rectangular half-width pulses.
  - (b) Polar signal with rectangular full-width pulses.
  - (c) Polar signal using Nyquist criterion pulses of  $r = 0.25$ .
  - (d) Bipolar signal with rectangular half-width pulses.
  - (e) Bipolar signal with rectangular full-width pulses.



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## Solution 2

(a) For Polar Signal:

$$R_b = B_T / 2 = 1.5 \text{ kbits/sec}$$

(b)  $p(t) = \text{rect}(t/T_b)$ ;

$\Rightarrow$  Essential BW ( $B_T$ ) =  $R_b$  : Hence, transmission bit rate = 3Kbits/sec



# Tutorial-11

## Solution 2

c)  $BT = 4800 \text{ bits/sec}$

d) Essential  $BW = R_b$  : Bit rate possible is 3 kbits/s

e)

Again for Bipolar Signal:

$\Rightarrow$  Essential  $BW = R_b$  :  $BT$  ; Hence, transmission bit rate = 3Kbits/sec



## Tutorial-11

**3. A 64 Kbps binary PCM Bipolar NRZ signal is passed through a communication system with a raised cosine filter with roll off factor 0.25. Determine the bandwidth of the PCM signal and the bandwidth of the filtered PCM signal.**



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## Solution 3

Nyquist BW= 32 KHz

BW of filtered PCM signal = 40 KHz



## Tutorial-11

**4. For the Gaussian random variable, X with mean and standard deviation values are given as  $\mu=5$  and  $\sigma=2$ , respectively. Find the probability values such as (a)  $P(X>8)$ , (b)  $P(X<8)$  and (c)  $P(3<X<8)$ .**

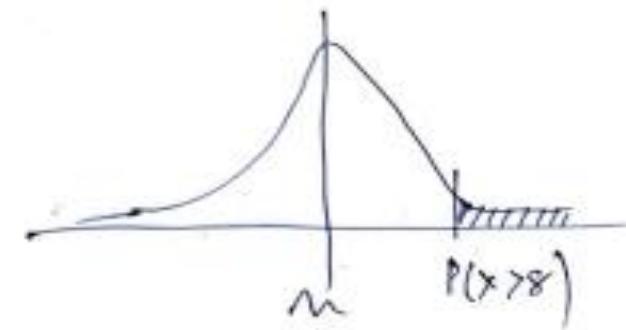


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## Solution 4

$$P(x>8) = Q \left( \frac{(x-\mu)}{\sigma} \right) = 0.066807$$

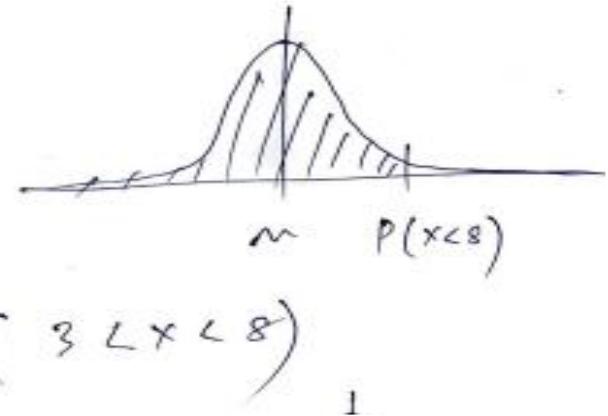


$$P(x<8) = 1 - P(x>8) = 1 - Q(1.5) = 0.933193$$



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## Solution 4



$$P(3 < x < 8) = 1 - Q(1.5) - Q(1)$$

$$= 1 - 0.066807 - 0.15866 = 0.774533$$



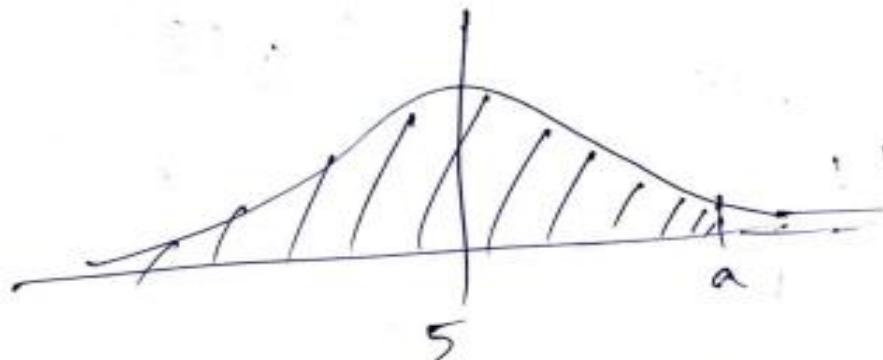
## Tutorial-11

5. For the Gaussian random variable, X with mean and standard deviation values are given as  $\mu=5$  and  $\sigma=3$ , respectively. Find the factor a such that  $P(X < a) = 0.9$



## Solution 5

Ans



$$P(X < a) = 0.9 \Rightarrow P(X > a) = 0.1$$

$$\Rightarrow \Phi\left(\frac{a-5}{3}\right) = 0.1$$

$$\text{Thus } a^{-5} \approx 1.25$$

$$\Rightarrow a = (1.25 \times 3) + 5 \\ = 3.75 + 5 = 8.75$$



## Tutorial-11

6. For the Gaussian random variable, X with mean and standard deviation values are given as  $\mu=5$  and  $\sigma=3$ , respectively. Find the factor a such that  $P(3 < X < a) = 0.7$



## Tutorial-11

### Solution 6

$$\begin{aligned} \Rightarrow P(X > a) &= 1 - 0.95 = 0.05 \\ \Rightarrow \Phi\left(\frac{a-5}{3}\right) &= 0.05 \end{aligned}$$

$$\begin{aligned} \Rightarrow \frac{a-5}{3} &= 1.60 \\ \Rightarrow a &= 4.8 + 5 \\ &= 9.8 \end{aligned}$$