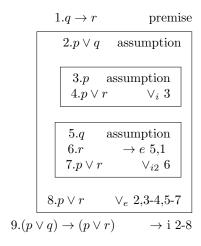
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Prove:  $q \to r \vdash p \lor q \to p \lor r$ 



## 5.3 "Copy" Rule

$$\begin{array}{c|c} \bot p \to (q \to p) \\ \hline \\ 1.p & \text{assumption} \\ \hline \\ 2.q & \text{assumption} \\ \hline \\ 3.p & \textbf{copy 1} \\ \hline \\ 4.q \to p & \to i \ 2\text{-}3 \\ \hline \\ 5.p \to (q \to p) & \to i \ 1\text{-}4 \end{array}$$

## 6 Rules for Negation

## 6.1 Contradiction

• Contradictions are expressions of the form  $\phi \land \neg \phi$  or  $\neg \phi \land \phi$  where  $\phi$  is any proposition.

- $\bullet~\bot$  represents a contradiction.
- Any proposition can be derived from contradiction.
- 6.2 Bottom Elimination

$$\frac{\perp}{\psi} \perp e$$

6.3 Not Elimination

$$\frac{\phi \neg \phi}{\Box} \neg e$$