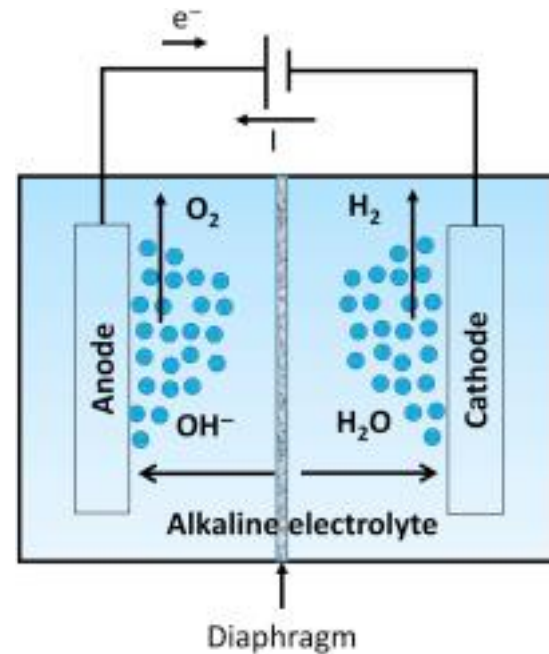


# Heat transfer issues in large-scale electrolysis

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# Motivation

EU target of 80%–95% greenhouse gas reductions by 2050 compared with the 1990 levels



Aim: current densities **>200**  
**mA cm<sup>-2</sup>**

Current operational range:  
 $\sim 35 \text{ mA cm}^{-2}$

CO<sub>2</sub>

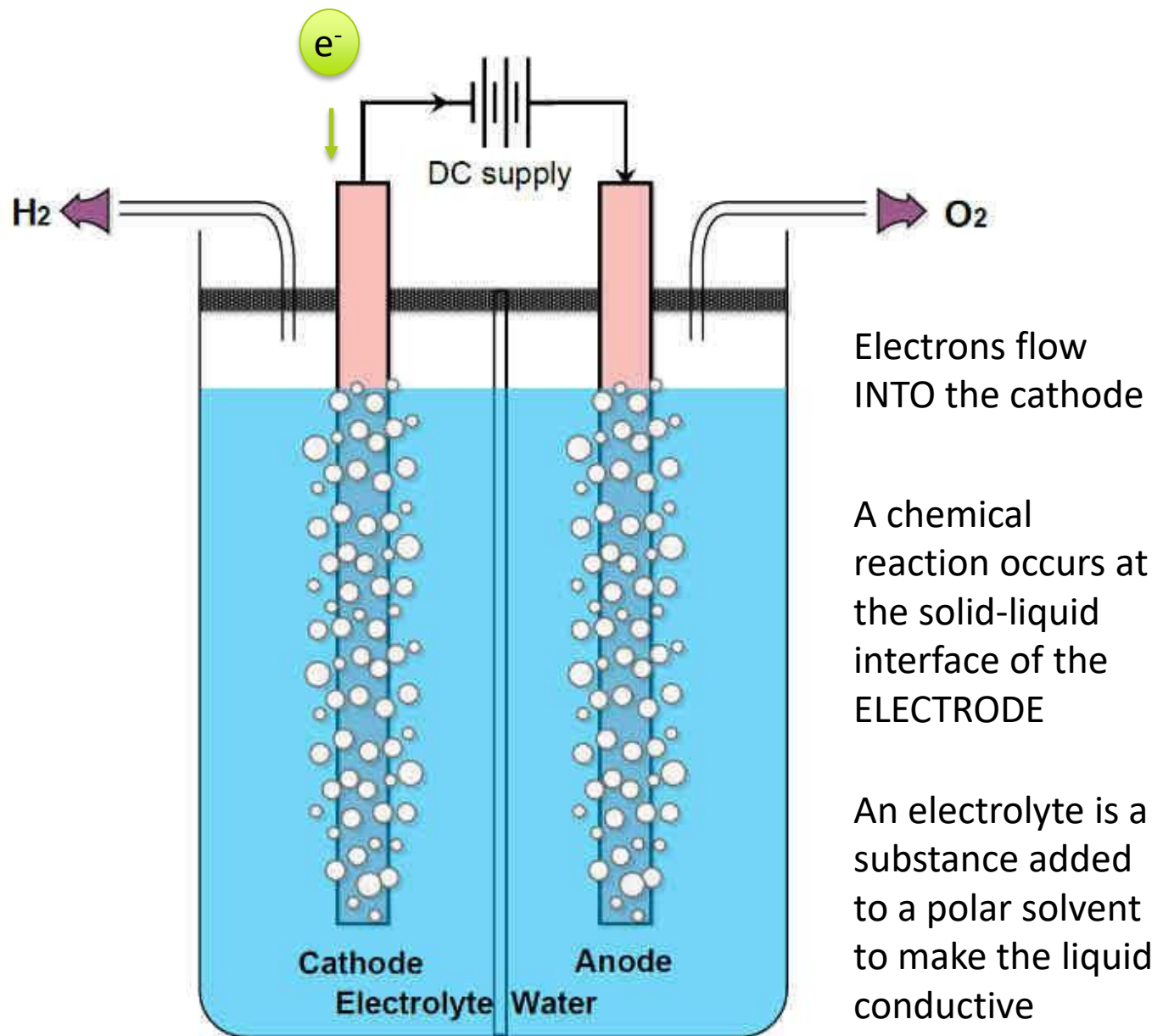


**Electrolysis**



Fuels

Chemical precursors  
(e.g. methane,  
ethylene)

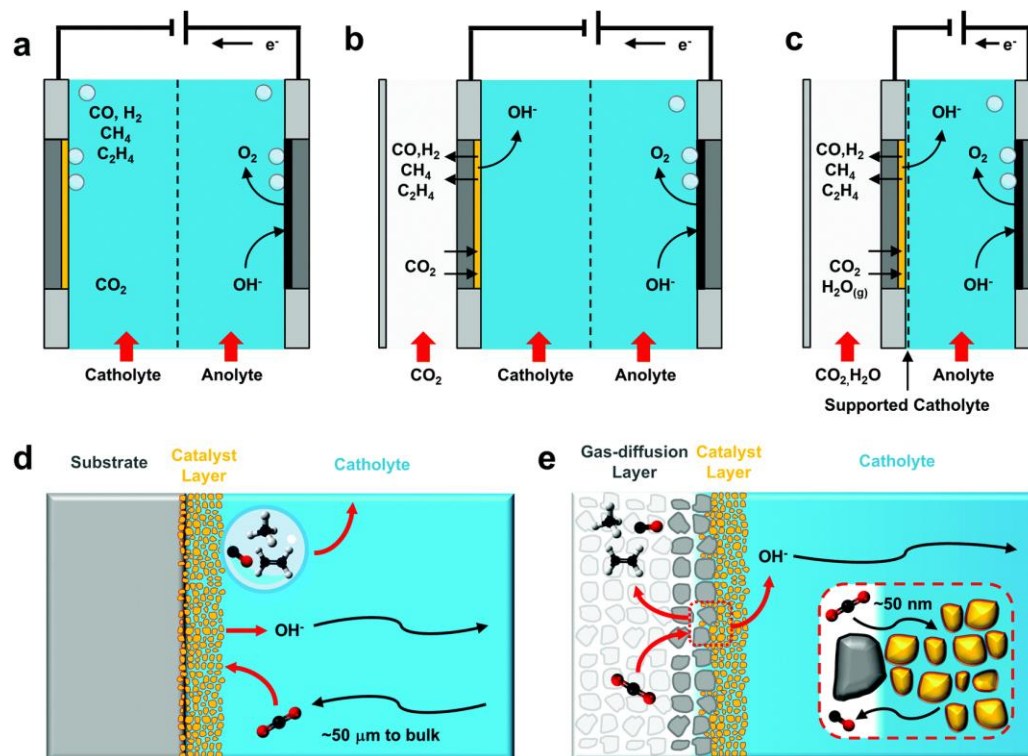


Modelling literature focussed on **ALKALINE WATER ELECTROLYSIS**. **CO<sub>2</sub>**?



Thomas Burdyny

## CO<sub>2</sub> electrolysis



Reaction "at the wall"

Reaction at a gas-fluid interface inside a porous medium

Configurations can be very different (reduction of CO<sub>2</sub> saturated catholyte vs gas-diffusion layer; flowing or non-flowing catholyte)

Bubbles can form (reaction products, e.g. methane CH<sub>4</sub>; oxygen at the anode)

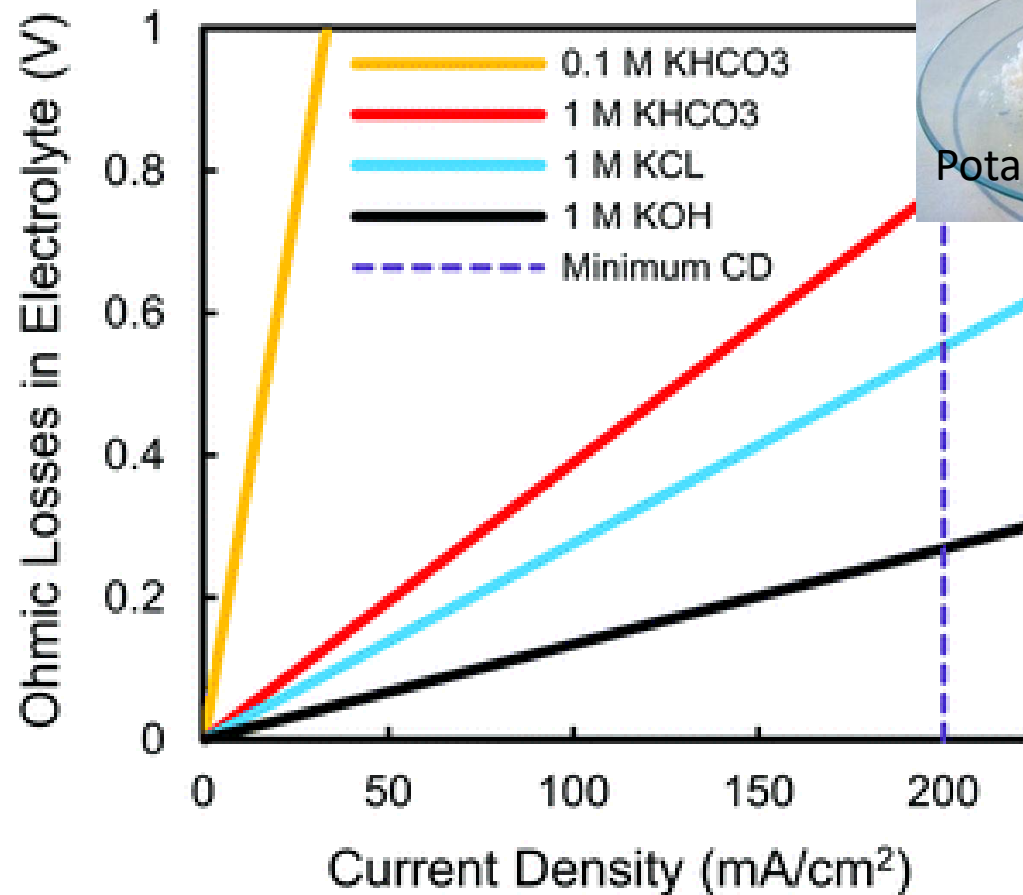
Loss: drop  
in voltage  
due to an  
inefficiency  
in the  
process

## WB3595 Final Report Group 1

### Scaling Up Electrolysis: Multiphase and Heat Transfer Problems

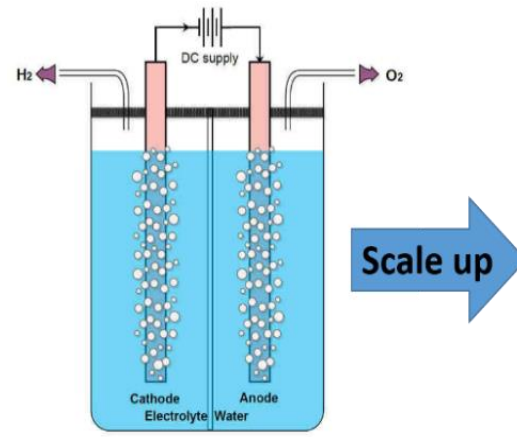
Frederieke Backelandt 4978501  
Pepijn van den Bent 4660390  
Rohit Bisumbhar 4565606  
Wout Dekkers 4928377  
Dirk Jacobs 4872509

- The **Ohmic overpotential** is an overpotential due to the transport of the ions between the electrodes. The resistance that these ions will endure comes out in the form of heat and can be derived from Ohm's law (Wang and Sun, 2015).
- The **electric overpotential** is caused by the resistance the electrons encounter flowing through the electrodes. Since the electrodes' material is highly conductive, this overpotential has a small contribution to the heat generation (Cretti, 2020).
- The **activation overpotential** is caused by the activation energy for the cell reaction at the electrode-electrolyte interface. The activation energy barrier is caused by multiple phenomena, such as the activation energy of the chemical reactions, the absorption and desorption mechanisms of the molecule on the electrode surface, and the molecules' rearrangement after the reaction etc (Menictas et al., 2014).
- The **concentration overpotential** is caused by the limited rate of mass transport, the product accumulates on the surface of the electrodes and creates a lack of the reactant in order for the process to continue. This phenomenon can occur when the mass transfer is relatively slow compared to the conversion (Cretti, 2020)
- the **decomposition overpotential** correlates with a increasing potential. When this occurs the anodic dissolution starts and the so-called **decomposition overpotential** is obtained (Wang and Sun, 2015).



**Expected ohmic losses** as a function of current density for commonly-used electrolytes in an electrochemical cell with a combined 3 mm catholyte and anolyte thickness at 25 °C.

For 0.1 M KHCO<sub>3</sub> (a common concentration) **loss is 6V!**



## Project E-Heat:

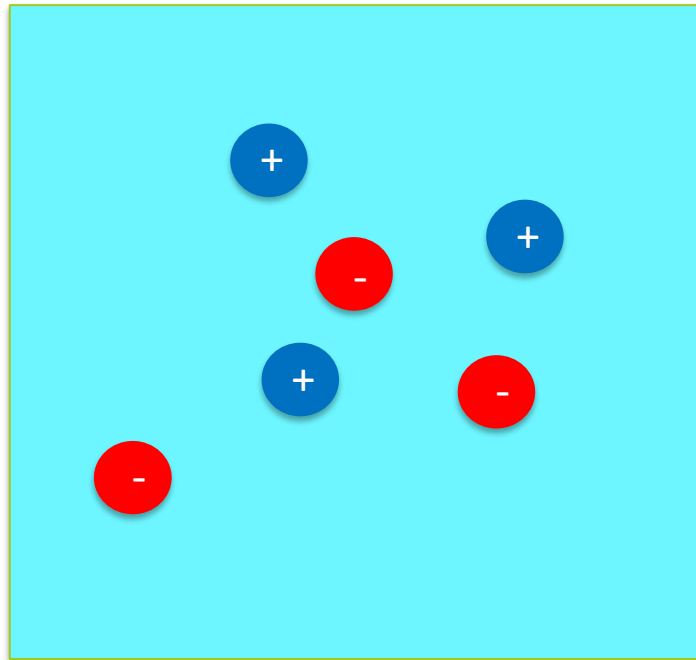
understanding/quantifying heat production in CO<sub>2</sub> electrolytes

- A BIG fraction (30%) of the input electrical power is LOST in heat
- If we understand the physics, we can mitigate ohmic loss or REUSE THE WASTE HEAT

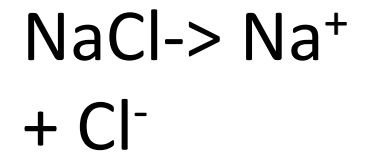
# Microphysics of heat loss due to ion migration



No  
electric  
field

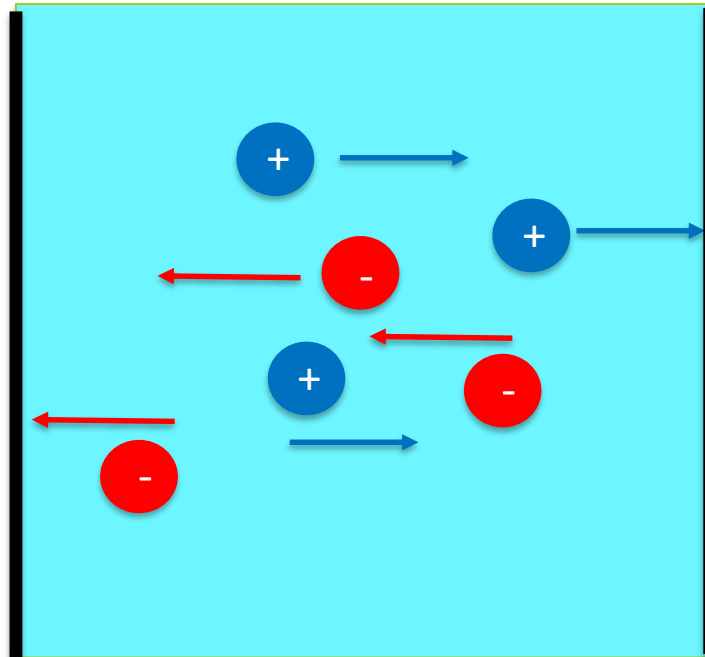


Dissociated  
ions, e.g.:



Electric  
field  
applied

+



-

# Single-ion hydrodynamics

Force balance:  $\mathbf{F}_{ext} + \mathbf{F}_{hd} = 0$

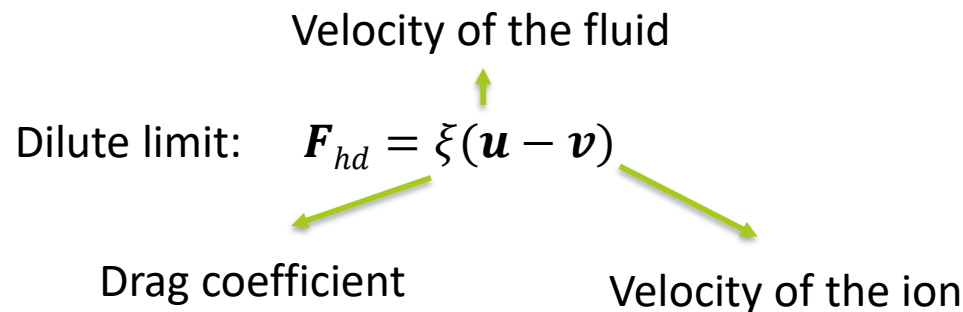
Closure for the drag:

Velocity of the fluid

Dilute limit:  $\mathbf{F}_{hd} = \xi(\mathbf{u} - \mathbf{v})$

Drag coefficient

Velocity of the ion

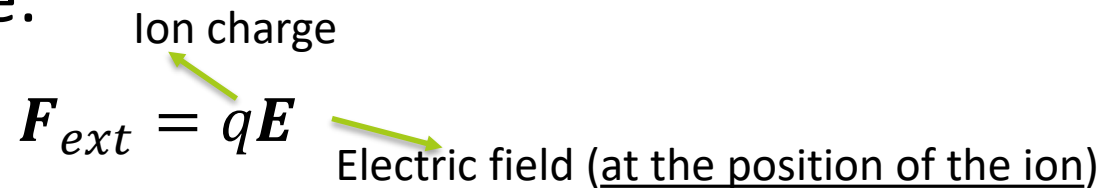


External force:

Ion charge

$\mathbf{F}_{ext} = q\mathbf{E}$

Electric field (at the position of the ion)



# Link with notion of ion mobility

If fluid velocity is zero, and  $E$  is uniform:

$$v = qE/\xi \quad (\text{unidirectional motion})$$

Definition: **electrical mobility**

$$\mu_e = v/E$$

Drag coefficient is related to mobility:  $\mu_e = q/\xi$

The mobility of the sodium ion ( $\text{Na}^+$ ) in water at 25 °C is  $5.19 \times 10^{-8} \text{ m}^2/(\text{V} \cdot \text{s})$ . A sodium ion in an electric field of 1 V/m has an average drift velocity of  $5.19 \times 10^{-8} \text{ m/s}$ .

Can be measured by measuring [ionic conductivity](#)

# Effect of ion migration on the fluid

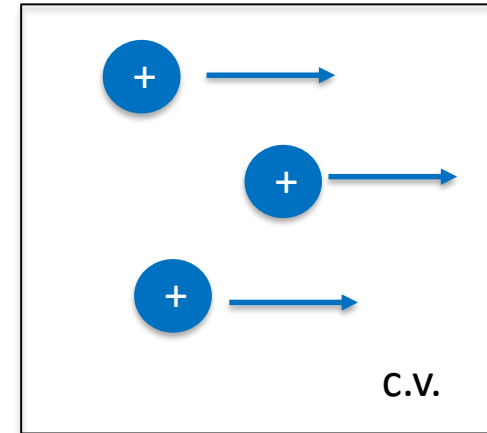
Hydrodynamic force per unit volume on the fluid by multiple ions

$n^k$ : number density of ion species k

$$\frac{1}{V} \sum \mathbf{F}_{hd}^k = n^k q^k \mathbf{E}$$



$$(\partial_t \mathbf{u} + \mathbf{u} \cdot \nabla \mathbf{u}) = (\nabla \cdot \boldsymbol{\sigma} + \rho^{(f)} \mathbf{E})$$



See e.g. Russel, William Bailey, et al. *Colloidal dispersions*.  
Cambridge university press, 1991 (pag 216).

Can we calculate heat loss from this expression?

# Viscous dissipation by moving ions

$$\mathbf{u} \cdot (\text{momentum equation}) = 0$$

$$\mathbf{u} \cdot (\partial_t \mathbf{u} + \mathbf{u} \cdot \nabla \mathbf{u}) = \mathbf{u} \cdot (\nabla \cdot \boldsymbol{\sigma} + \rho^{(f)} \mathbf{E})$$

$$\partial_t \left( \frac{1}{2} \rho u^2 \right) + \mathbf{u} \cdot \nabla \left( \frac{1}{2} \rho u^2 \right) = \nabla \cdot (\mathbf{u} \cdot \boldsymbol{\sigma}) - \nabla \mathbf{u} : \boldsymbol{\sigma} + \rho^{(f)} \mathbf{E} \cdot \mathbf{u}$$

$< 0$ : viscous dissipation (loss of mechanical energy of the fluid)

$$\rho^{(f)} \mathbf{E} \cdot \mathbf{u} = ?$$

Electric body force in general is NOT in the same direction of the fluid velocity

# Electrokinetic dissipation term

$\rho^{(f)} \mathbf{E} \cdot \mathbf{u} = ?$  A component of this work must be dissipated.  
Let's calculate it..

$$\mathbf{u} = \mathbf{v}^k + \underbrace{(\mathbf{u} - \mathbf{v}^k)}_{-q^k \mathbf{E} / \xi^k}$$

$$\rho^{(f)} \mathbf{E} \cdot \mathbf{u} = \sum_k n^k q^k \mathbf{E} \cdot (\mathbf{v}^k - q^k \mathbf{E} / \xi^k)$$

$$= \sum_k n^k q^k \mathbf{E} \cdot \mathbf{v}^k - \sum_k q^{k2} n^k |\mathbf{E}|^2 / \xi^k$$

# Electrokinetic dissipation term

$$\Phi_E = \sum_k q^k{}^2 n^k |E|^2 / \xi^k$$

Dissipation due to  
friction of ions with the  
fluid during migration

Similar term used in the literature:

$$\rho C_p \left( \frac{\partial T}{\partial t} + (\vec{u} \nabla) T \right) = \nabla(k \nabla T) + \Phi + \frac{(\vec{u} \rho_e - \lambda \nabla \phi)^2}{\lambda}$$

Cetin, Barbaros, and Dongqing Li. "Effect of Joule heating on electrokinetic transport." *Electrophoresis* 29.5 (2008): 994-1005

(derived using the "ohm's law"  $\frac{I^2}{\lambda}$ , where  $I$  is the current and  $\lambda$  is the ion conductivity,

Tang, G. Y., et al. "Modeling of electroosmotic flow and capillary electrophoresis with the joule heating effect: The Nernst– Planck equation versus the Boltzmann distribution." *Langmuir* 19.26, 2003)

Proportional to ion concentration

Proportional to square of LOCAL electric field

# Transport equations for electrolysis

Cetin, Barbaros, and Dongqing Li. "Effect of Joule heating on electrokinetic transport." *Electrophoresis* 29.5 (2008): 994-1005

$$\nabla(\lambda(T)\nabla\phi) = 0 \quad (13)$$

$$\nabla\vec{u} = 0 \quad \text{This should be a divergence} \quad (14)$$

$$\nabla(\mu(T)\nabla\vec{u}) = \nabla P \quad \text{conductivity} \quad (15)$$

$$\rho C_p \left( \frac{\partial T}{\partial t} + (\vec{u}\nabla)T \right) = \nabla(k(T)\nabla T) + \lambda(T)(\nabla\phi)^2 \quad (16)$$

$$\frac{\partial C}{\partial t} + \nabla((\vec{u} + \vec{u}_{ep})C - D(T)\nabla C) = 0 \quad \text{Nernst-Planck equation}$$

$$\vec{u}_{ep} = \mu_{ep}\nabla\phi \quad (18)$$

The electrophoretic velocity is RELATIVE TO THE FLUID; the electrophoretic mobility of the ions is equal to  $1/\xi$

+ B. C. for C, T, phi and u



# Analogy mass/heat transport

$$\nabla(\lambda(T)\nabla\phi) = 0 \quad (13)$$

$$\nabla\vec{u} = 0 \quad (14)$$

$$\nabla(\mu(T)\nabla\vec{u}) = \nabla P \quad (15)$$

$$\rho C_p \left( \frac{\partial T}{\partial t} + (\vec{u}\nabla)T \right) = \nabla(k(T)\nabla T) + \lambda(T)(\nabla\phi)^2 \quad (16)$$

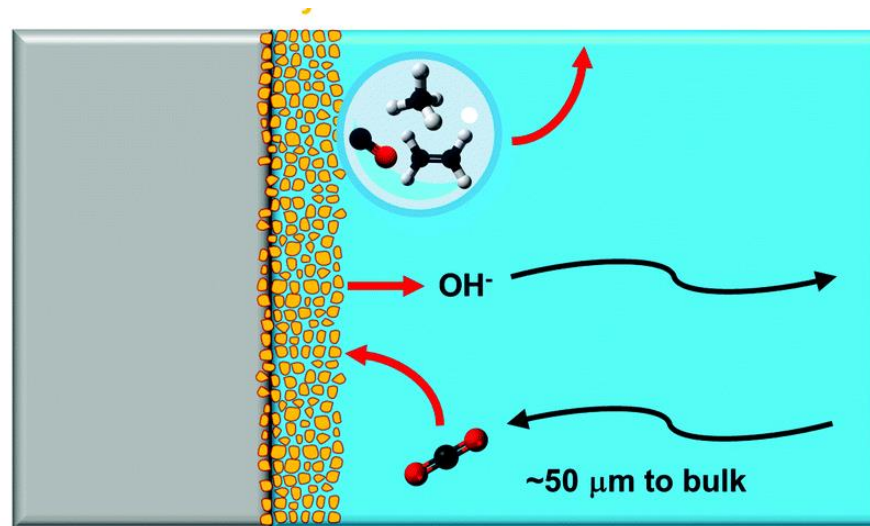
$$\frac{\partial C}{\partial t} + \nabla((\vec{u} + \vec{u}_{ep})C - D(T)\nabla C) = 0 \quad (17)$$

$$\vec{u}_{ep} = \mu_{ep}\nabla\phi \quad (18)$$

# Research questions

## Single-phase flow

Distribution of heat generation in a channel with reacting walls

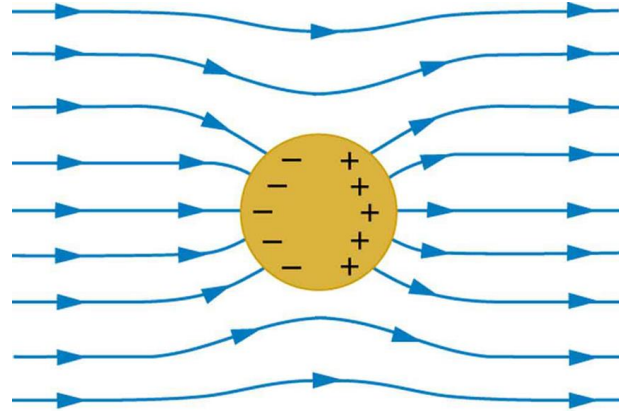


There will be an excess/defect of reactants or products near the wall

-> Concentration overpotential

# Multi-phase flow

Effect on  $E$

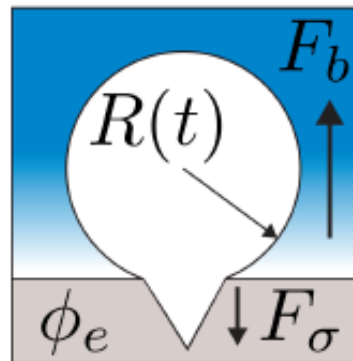


Distortion of a uniform electric field by a conducting sphere

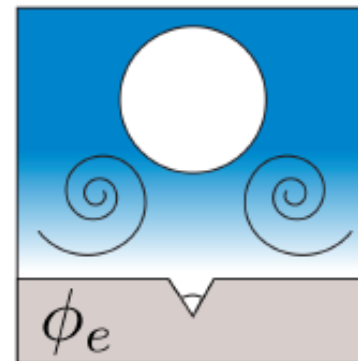
Bubbles can become local heat generators

Effect on  $n^k$

B) Growth



C) Detachment



van der Linde, Peter, et al. "Gas bubble evolution on microstructured silicon substrates." *Energy & environmental science* 11.12 (2018): 3452-3462.

<https://youtu.be/T-OwWOYHhMI?t=184>

High concentration of bubbles near the wall,  
low concentration far

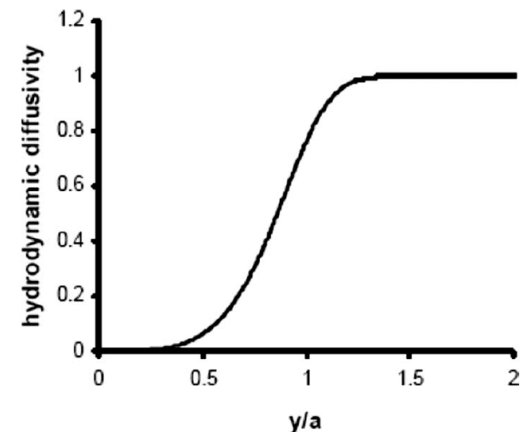
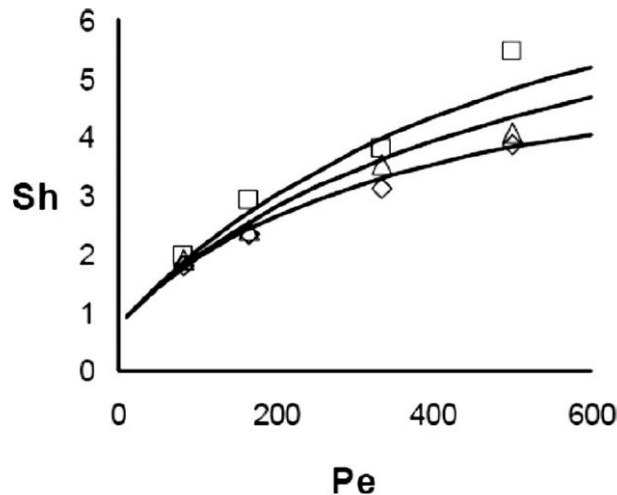
Bubbles translate because of buoyancy,  
mixing the fluid

Bubbles are EXTREMELY polydispersed (as in  
BOILING)

# Multi-phase flow

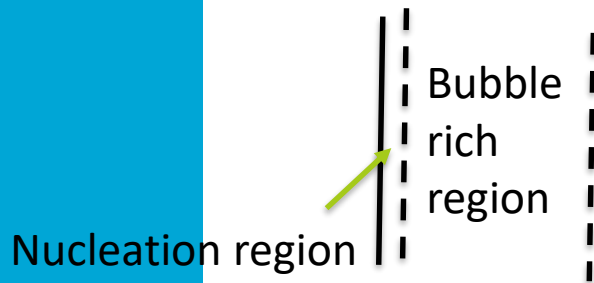
How does a mono or polydispersed suspension of spheres enhance mixing of a passive scalar (heat, concentration)?

Neutrally-buoyant spheres in simple shear flow

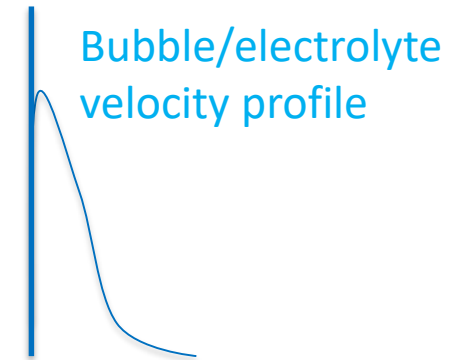


Wang, Luying, et al. "Hydrodynamic diffusion and mass transfer across a sheared suspension of neutrally buoyant spheres." *Physics of Fluids* 21.3 (2009): 033303.

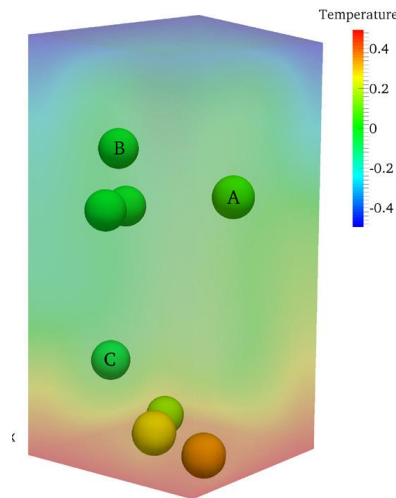
Polydispersity has not been considered



Clear fluid



Combined effect of shear/pseudo-turbulence?



Sun, Bo, et al. "Pseudo-turbulent heat flux and average gas-phase conduction during gas-solid heat transfer: flow past random fixed particle assemblies." *Journal of Fluid Mechanics* 798 (2016): 299.

Project of Shyam with Physalis code

# Summary

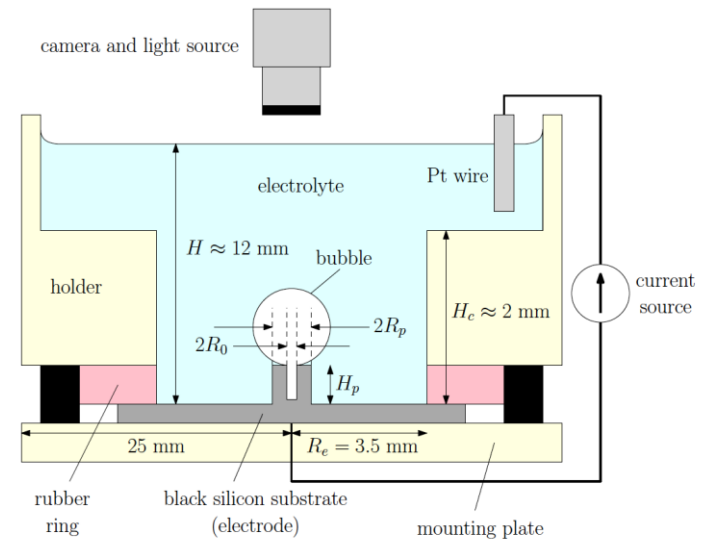
- Expression for heat loss by moving ions (electrokinetic viscous loss) derived from simple hydrodynamic considerations
- Need to understand how dispersed phase (bubble) affect ion transport and heat transport (current work of Shyam)
- Need to better understand the link between heat generation by electrokinetic viscous loss and ohmic overpotential

$$\overline{\Delta\Phi}_{\text{ohm}} = \frac{iL(1 - K_m)}{\kappa K_m} + \frac{iL}{\kappa}$$

Leistra, James A., and Paul J. Sides. "Voltage components at gas evolving electrodes." *Journal of The Electrochemical Society* 134.10 (1987): 2442.

At TU Twente:

van der Linde, Peter. "On electrolytic bubbles." (2019).





$$\rho C_p \left( \frac{\partial T}{\partial t} + (\vec{u} \nabla) T \right) = \nabla(k \nabla T) + \Phi + \frac{(\vec{u} \rho_e - \lambda \nabla \phi)^2}{\lambda}$$

See also: Tang, G. Y., et al. "Modeling of electroosmotic flow and capillary electrophoresis with the joule heating effect: The Nernst- Planck equation versus the Boltzmann distribution." *Langmuir* 19.26 (2003): 10975-10984.

Important:

Ohmic dissipation proportional to square of LOCAL electric field

Need to know distribution of electric field

Ohmic dissipation proportional to electrolyte concentration

Need to know how electrolyte concentration depends on diffusion, convection and presence of a dispersed phase

Heat is also transported

Local temperature depends on diffusion, convection and presence of a d