

1. What quantity of water should be added to the milk water mixture so that the milk water ratio changes from 2:3 to 4:11. The quantity of milk in the mixture is 40 litres?

solution:

Initially the milk water ratio=2/3

After adding water to the milk water mixture the milk water ratio is 4/11

The quantity of milk in the mixture = 40 litres

Assume quantity of water in mixture initially is X litres and after adding water is X+Y.

$$40/X=2/3$$

$$X=60 \text{ litres}$$

$$40/(X+Y) = 4/11$$

$$40/(60+Y) = 4/11$$

$$Y=50$$

50 litres

2. Linear equation $2x+3y=0$ meets the x & y-axis at the point?

Ans: (0,0)

3. a & b are positive integers such that $a^2-b^2=19$. Find a & b?

Solution:

$$a^2-b^2=19$$

$$(a+b)(a-b)=19$$

19 is prime number and a and b are positive intergers so

$$a+b=19 \text{ and } a-b=1$$

after solving above equation

$$a=10$$

$$b=9$$

4. Find $a^3+b^3+c^3-3abc$, where $a+b+c=5$ & , $a^2+b^2+c^2=10$?

Solution:

$$(a+b+c)^2 = a^2+b^2+c^2+2(ab+bc+ca)$$

$$5^2=10+2(ab+bc+ca)$$

$$ab+bc+ca=15/2$$

$$a^3+b^3+c^3-3abc=(a+b+c)(a^2+b^2+c^2-bc-ab-ac)=5(10-15/2)=12.5$$

5. Sum of two, two-digit numbers is a perfect square. The digits of the first two-digit number are two consecutive positive integers; also, when the digits of the first number are reversed, the second number is formed. Find these numbers & the square root of their sum.

Solution:

$$\text{Assume first two-digit number} = X*10+(X+1)$$

$$\text{Then second two-digit number} = (X+1)*10+X$$

sum of these two number= $22X+11$

According to question $22X+11$ is a perfect square, so

$$11(2X+1)$$

for a perfect square $2X+1$ must be 11

therefore $X=5$

first two-digit number= 56

second two-digit number= 65

square root of their sum= 11