

```

1 import numpy as np
2 import matplotlib.pyplot as plt
3
4 # Parameters
5 n_states = 16
6 n_actions = 4
7 goal_state = 15
8
9 Q_table = np.zeros((n_states, n_actions))
10
11 learning_rate = 0.8
12 discount_factor = 0.95
13 exploration_prob = 0.2
14 epochs = 1000
15
16 # Q-learning process
17 for epoch in range(epochs):
18     current_state = np.random.randint(0, n_states)
19
20     while current_state != goal_state:
21
22         # Exploration vs. Exploitation (ε-greedy policy)
23         if np.random.rand() < exploration_prob:
24             action = np.random.randint(0, n_actions)
25         else:
26             action = np.argmax(Q_table[current_state])
27
28         # Transition to the next state (circular movement for simplicity)
29         next_state = (current_state + 1) % n_states
30
31         # Reward function (1 if goal_state reached, 0 otherwise)
32         reward = 1 if next_state == goal_state else 0
33
34         # Q-value update rule (TD update)
35         Q_table[current_state, action] += learning_rate * \
36             (reward + discount_factor * np.max(Q_table[next_state]) - Q_table[current_state,
action])
37
38         current_state = next_state # Update current state
39
40 # Visualization of the Q-table in a grid format
41 q_values_grid = np.max(Q_table, axis=1).reshape((4, 4))
42
43 # Plot the grid of Q-values
44 plt.figure(figsize=(6, 6))
45 plt.imshow(q_values_grid, cmap='coolwarm', interpolation='nearest')
46 plt.colorbar(label='Q-value')
47 plt.title('Learned Q-values for each state')
48 plt.xticks(np.arange(4), ['0', '1', '2', '3'])
49 plt.yticks(np.arange(4), ['0', '1', '2', '3'])
50 plt.gca().invert_yaxis() # To match grid layout
51 plt.grid(True)
52
53 # Annotating the Q-values on the grid
54 for i in range(4):
55     for j in range(4):
56         plt.text(j, i, f'{q_values_grid[i, j]:.2f}', ha='center', va='center', color='black')
57
58 plt.show()
59
60 # Print learned Q-table
61 print("Learned Q-table:")
62 print(Q_table)

```