NBA_EDA

December 12, 2022

[ ]:
```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import matplotlib.patches as mpatches
import seaborn as sns
```

[ ]:
```
pd.set_option("display.max_columns", None)
```

##Games Data

[ ]:
```
all_games = pd.read_csv("/content/drive/MyDrive/Machine Learning NBA /Final␣
↪Data/games_with_features.csv", index_col="id")
```

[ ]:
```
all_games.head()
```

[ ]:
```
             date  home_team_score  period  postseason  season status  \
id
47179  2019-01-30              126       4       False    2018  Final
48751  2019-02-09              112       4       False    2018  Final
48739  2019-02-08              117       4       False    2018  Final
48740  2019-02-08              119       4       False    2018  Final
48746  2019-02-08              102       4       False    2018  Final

       visitor_team_score  home_team.id home_team.abbreviation  \
id
47179                  94             2                    BOS
48751                 123             2                    BOS
48739                 110            23                    PHI
48740                 106            30                    WAS
48746                  96            26                    SAC

      home_team.conference home_team.division home_team.full_name  \
id
47179                 East           Atlantic      Boston Celtics
48751                 East           Atlantic      Boston Celtics
48739                 East           Atlantic  Philadelphia 76ers
48740                 East          Southeast  Washington Wizards
48746                 West            Pacific    Sacramento Kings
```

```
       visitor_team.id visitor_team.abbreviation visitor_team.conference  \
id
47179               4                       CHA                     East
48751              13                       LAC                     West
48739               8                       DEN                     West
48740               6                       CLE                     East
48746              16                       MIA                     East

      visitor_team.division visitor_team.full_name  winner  \
id
47179             Southeast      Charlotte Hornets       1
48751               Pacific            LA Clippers       0
48739             Northwest         Denver Nuggets       1
48740               Central    Cleveland Cavaliers       1
48746             Southeast             Miami Heat       1

       home_team_avg_score_historical  visitor_team_avg_score_historical  \
id
47179                           105.7                               98.4
48751                           105.7                              100.6
48739                           103.2                              104.2
48740                           103.4                               98.4
48746                           105.5                               96.1

      home_team_id_year visitor_team_id_year  home_team_avg_score  \
id
47179           2 2018              4 2018                112.8
48751           2 2018             13 2018                112.8
48739          23 2018              8 2018                117.9
48740          30 2018              6 2018                116.4
48746          26 2018             16 2018                114.9

       visitor_team_avg_score  home_avg_score_diff  visitor_avg_score_diff
id
47179                   108.3             3.620000               -3.831707
48751                   113.1             3.620000                0.581818
48739                   108.2             8.725532               -4.670213
48740                   103.8             7.429268               -8.419512
48746                   105.4             5.129268               -6.670732
```

[ ]:
```
all_seasons = np.sort(all_games["season"].unique())
all_seasons
```

[ ]:
```
array([1979, 1980, 1981, 1982, 1983, 1984, 1985, 1986, 1987, 1988, 1989,
       1990, 1991, 1992, 1993, 1994, 1995, 1996, 1997, 1998, 1999, 2000,
       2001, 2002, 2003, 2004, 2005, 2006, 2007, 2008, 2009, 2010, 2011,
```

```
       2012, 2013, 2014, 2015, 2016, 2017, 2018, 2019, 2020, 2021])
```

###Percent of home team win

[ ]:
```
n_home_wins = all_games[all_games["home_team_score"].
 ↪gt(all_games["visitor_team_score"])].shape[0]  # number of games where home␣
 ↪team won
n_games = all_games.shape[0]  # number of games
home_win_pct = round(n_home_wins/n_games, 2)

print(n_home_wins, n_games, home_win_pct, sep="\n")
```

```
30529
49995
0.61
```

[ ]:
```
home_win_pcts = []
for season in all_seasons:
    season_games = all_games[all_games["season"].eq(season)]
    n_home_wins = season_games[season_games["home_team_score"].
 ↪gt(season_games["visitor_team_score"])].shape[0]  # number of games where␣
 ↪home team won
    n_games = season_games.shape[0]  # number of games
    home_win_pct = round(n_home_wins/n_games, 2) * 100
    home_win_pcts.append(home_win_pct)
    print(season, n_home_wins, n_games, home_win_pct)
```

```
1979 622 950 65.0
1980 612 995 62.0
1981 592 989 60.0
1982 612 986 62.0
1983 687 1022 67.0
1984 642 1011 64.0
1985 662 1010 66.0
1986 677 1014 67.0
1987 697 1023 68.0
1988 729 1087 67.0
1989 767 1179 65.0
1990 773 1175 66.0
1991 751 1180 64.0
1992 725 1183 61.0
1993 729 1184 62.0
1994 700 1178 59.0
1995 764 1257 61.0
1996 733 1261 57.99999999999999
1997 746 1252 60.0
1998 492 791 62.0
1999 775 1264 61.0
```

```
2000 752 1260 60.0
2001 744 1260 59.0
2002 800 1277 63.0
2003 789 1271 62.0
2004 791 1314 60.0
2005 802 1319 61.0
2006 778 1309 59.0
2007 803 1316 61.0
2008 805 1315 61.0
2009 786 1312 60.0
2010 797 1311 61.0
2011 637 1074 59.0
2012 806 1314 61.0
2013 764 1319 57.99999999999999
2014 755 1311 57.99999999999999
2015 782 1316 59.0
2016 763 1309 57.99999999999999
2017 770 1312 59.0
2018 774 1311 59.0
2019 623 1142 55.00000000000001
2020 311 558 56.00000000000001
2021 410 774 53.0
```

[ ]:
```
fontdict = {'weight' :'bold', 'size' :'16'

}
```

[ ]:
```
y = home_win_pcts * 100
print(y)
ax = plt.figure(figsize=(16,8))
ax  = sns.barplot(all_seasons, home_win_pcts, palette = 'inferno')
ax.bar_label(ax.containers[0], fmt='%.f%%')
ax.set_xticklabels(all_seasons, rotation = 45)
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Figures/Home Team Win␣
 ↪% by Year.png")
ax.set_xlabel("Year", fontdict = {'weight' : 'bold', 'size' : 13})
```

```
[65.0, 62.0, 60.0, 62.0, 67.0, 64.0, 66.0, 67.0, 68.0, 67.0, 65.0, 66.0, 64.0,
61.0, 62.0, 59.0, 61.0, 57.99999999999999, 60.0, 62.0, 61.0, 60.0, 59.0, 63.0,
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57.99999999999999, 59.0, 57.99999999999999, 59.0, 59.0, 55.00000000000001,
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```
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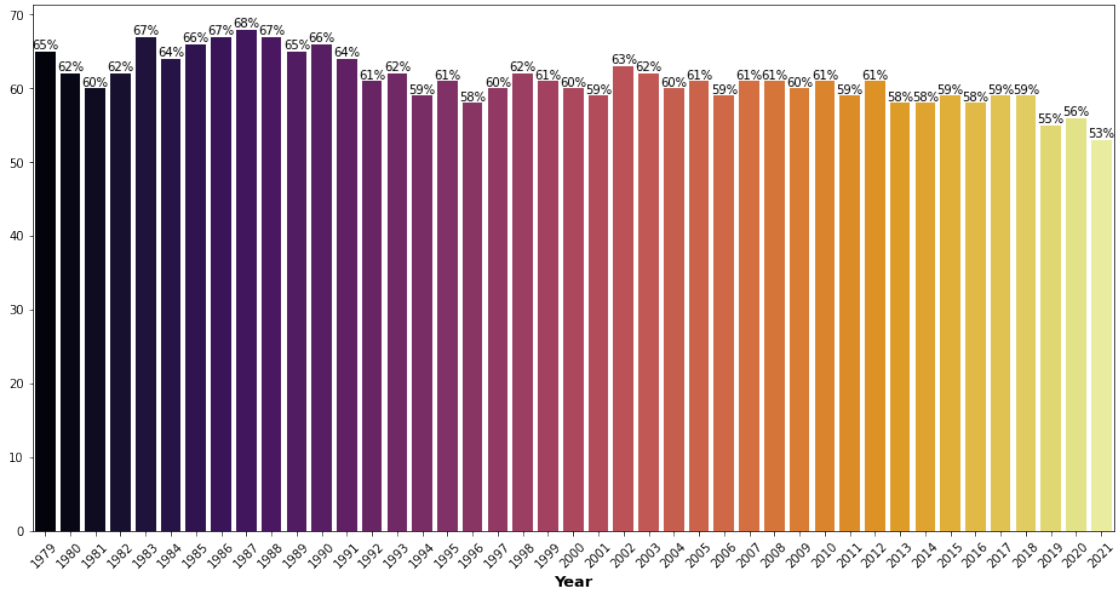
57.99999999999999, 59.0, 57.99999999999999, 59.0, 59.0, 55.00000000000001,
56.00000000000001, 53.0]

/usr/local/lib/python3.7/dist-packages/seaborn/_decorators.py:43: FutureWarning:
Pass the following variables as keyword args: x, y. From version 0.12, the only
valid positional argument will be `data`, and passing other arguments without an
explicit keyword will result in an error or misinterpretation.
  FutureWarning
```

[ ]: `Text(0.5, 35.89770926787756, 'Year')`



##Points scores when playing at home

[ ]:
```
home_avg = all_games[["home_team.full_name", "season", "home_team_avg_score"]].
 ↪groupby(["home_team.full_name", "season"]).mean().values
```

[ ]:
```
visiting_avg = all_games[["visitor_team.full_name", "season",␣
 ↪"visitor_team_avg_score"]].groupby(["visitor_team.full_name", "season"]).
 ↪mean().values
```

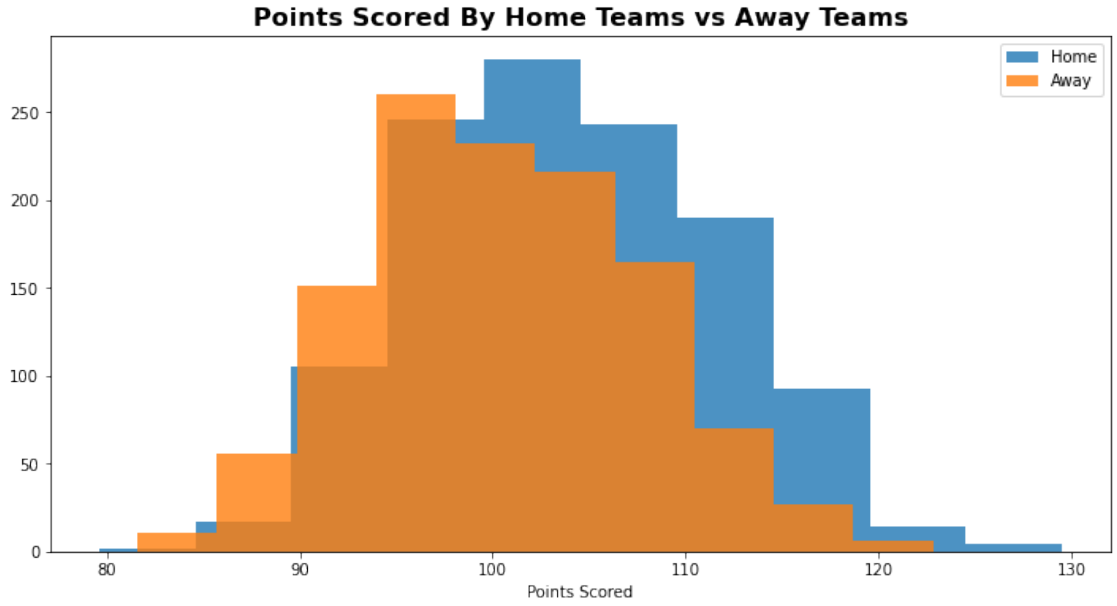
[ ]:
```
avg_score_by_team = all_games[["home_team.full_name", "season",␣
 ↪"home_team_avg_score"]].groupby(["home_team.full_name", "season"]).mean()

avg_score_by_team.columns = ["avg_score_as_home"]

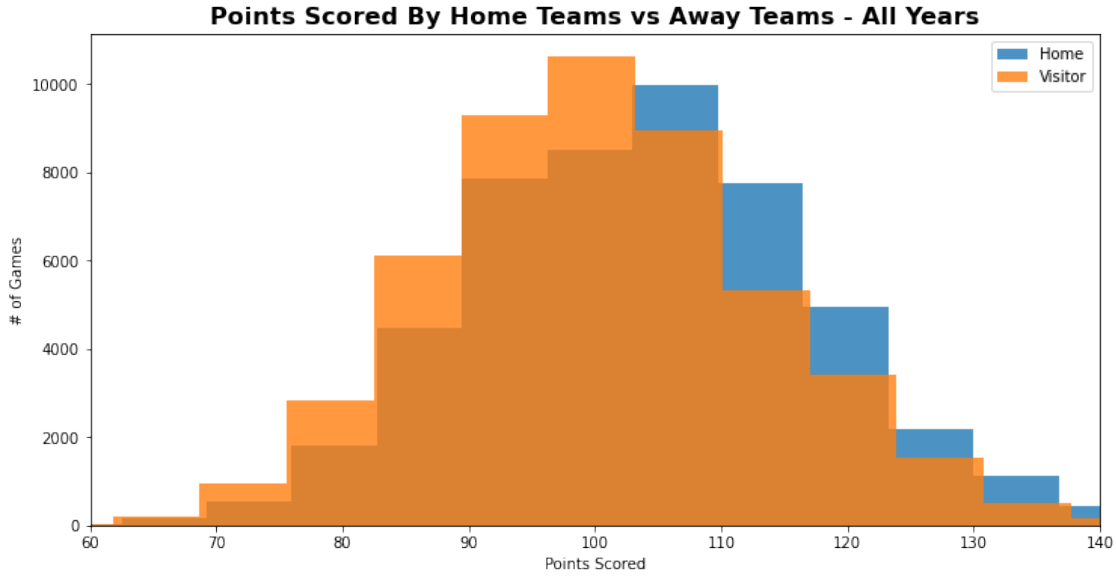
avg_score_by_team["avg_score_as_home"] = home_avg
avg_score_by_team["avg_score_as_visitor"] = visiting_avg
avg_score_by_team["avg_score_mean"] = (home_avg + visiting_avg) / 2
avg_score_by_team["avg_score_diff"] = (home_avg - visiting_avg)
avg_score_by_team.reset_index(inplace=True)
```

[ ]:
```
plt.figure(figsize=(12,6))
plt.hist(avg_score_by_team["avg_score_as_home"], alpha=0.8, label="Home",␣
 ↪bins=10)
plt.hist(avg_score_by_team["avg_score_as_visitor"], alpha=0.8, label="Away",␣
 ↪bins=10)
plt.title("Points Scored By Home Teams vs Away Teams", fontdict)
plt.xlabel("Points Scored")
```

```
plt.legend()
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Figures/Points Scored␣
 ↪By Home Teams vs Away Teams.png")
plt.show()
```



[ ]:
```
plt.figure(figsize=(12,6))
plt.hist(all_games["home_team_score"], alpha=0.8, label="Home", bins=20)
plt.hist(all_games["visitor_team_score"], alpha=0.8, label="Visitor", bins=20)
plt.xlim(60,140)
plt.title("Points Scored By Home Teams vs Away Teams - All Years", fontdict)
plt.xlabel("Points Scored")
plt.ylabel("# of Games")
plt.legend()
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Figures/Points Scored␣
 ↪By Home Teams vs Away Teams - All Years.png")
plt.show()
```



[ ]:
```
avg_score_by_team[avg_score_by_team["avg_score_as_home"].gt(120)]
```

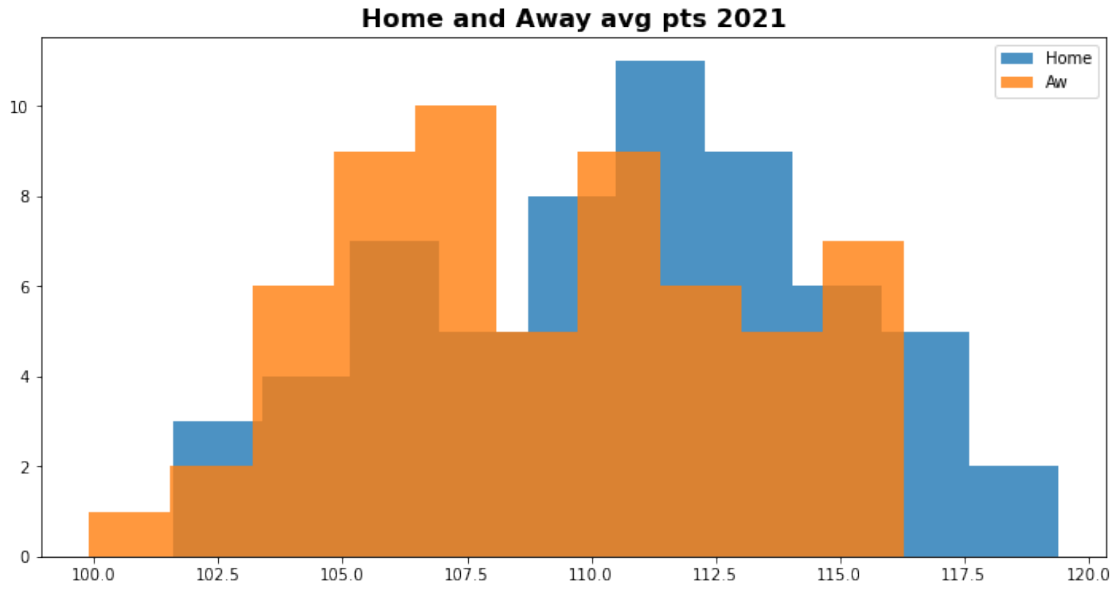
[ ]:

	home_team.full_name	season	avg_score_as_home	avg_score_as_visitor	\
253	Dallas Mavericks	1986	120.7	112.6	
290	Denver Nuggets	1980	124.7	118.9	
291	Denver Nuggets	1981	129.5	122.8	
292	Denver Nuggets	1982	125.5	119.9	
293	Denver Nuggets	1983	126.7	120.6	
294	Denver Nuggets	1984	122.8	117.8	
296	Denver Nuggets	1986	122.1	110.8	
298	Denver Nuggets	1988	122.5	113.2	
300	Denver Nuggets	1990	120.1	119.6	
385	Golden State Warriors	1989	121.4	111.2	
387	Golden State Warriors	1991	120.5	116.7	
552	Los Angeles Lakers	1984	123.6	115.7	
553	Los Angeles Lakers	1985	120.2	113.7	
554	Los Angeles Lakers	1986	121.2	115.0	
918	Phoenix Suns	1988	120.2	116.9	
1038	San Antonio Spurs	1979	122.2	115.5	
1042	San Antonio Spurs	1983	122.7	117.7	
1192	Washington Wizards	2020	121.5	112.0	

	avg_score_mean	avg_score_diff
253	116.65	8.1
290	121.80	5.8
291	126.15	6.7
292	122.70	5.6
293	123.65	6.1

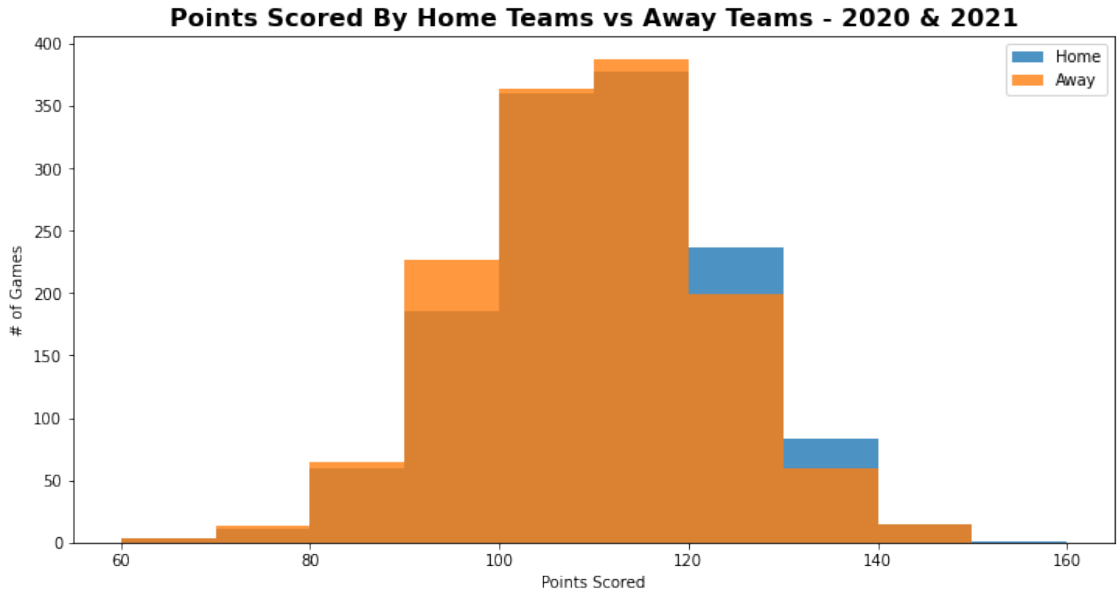
294	120.30	5.0
296	116.45	11.3
298	117.85	9.3
300	119.85	0.5
385	116.30	10.2
387	118.60	3.8
552	119.65	7.9
553	116.95	6.5
554	118.10	6.2
918	118.55	3.3
1038	118.85	6.7
1042	120.20	5.0
1192	116.75	9.5

[ ]:
```
plt.figure(figsize=(12,6))
plt.hist(avg_score_by_team[avg_score_by_team["season"].
 ↪isin([2019,2021])]["avg_score_as_home"], alpha=0.8, label="Home")
plt.hist(avg_score_by_team[avg_score_by_team["season"].
 ↪isin([2019,2021])]["avg_score_as_visitor"], alpha=0.8, label="Aw")
plt.title("Home and Away avg pts 2021", fontdict)
plt.legend()
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Figures/Home and Away␣
 ↪avg pts 2021.png")
plt.show()
```



[ ]:
```
plt.figure(figsize=(12,6))
```

```
plt.hist(all_games[all_games["season"].isin([2020,2021])]["home_team_score"],␣
 ↪alpha=0.8, label="Home",
         bins=[60,70,80,90,100,110,120,130,140,150,160])
plt.hist(all_games[all_games["season"].
 ↪isin([2020,2021])]["visitor_team_score"], alpha=0.8, label="Away",
        bins=[60,70,80,90,100,110,120,130,140,150,160])
plt.title("Points Scored By Home Teams vs Away Teams - 2020 & 2021", fontdict)
plt.xlabel("Points Scored")
plt.ylabel("# of Games")
plt.legend()
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Points Scored By Home␣
 ↪Teams vs Away Teams - 2020 & 2021.png")
plt.show()
```

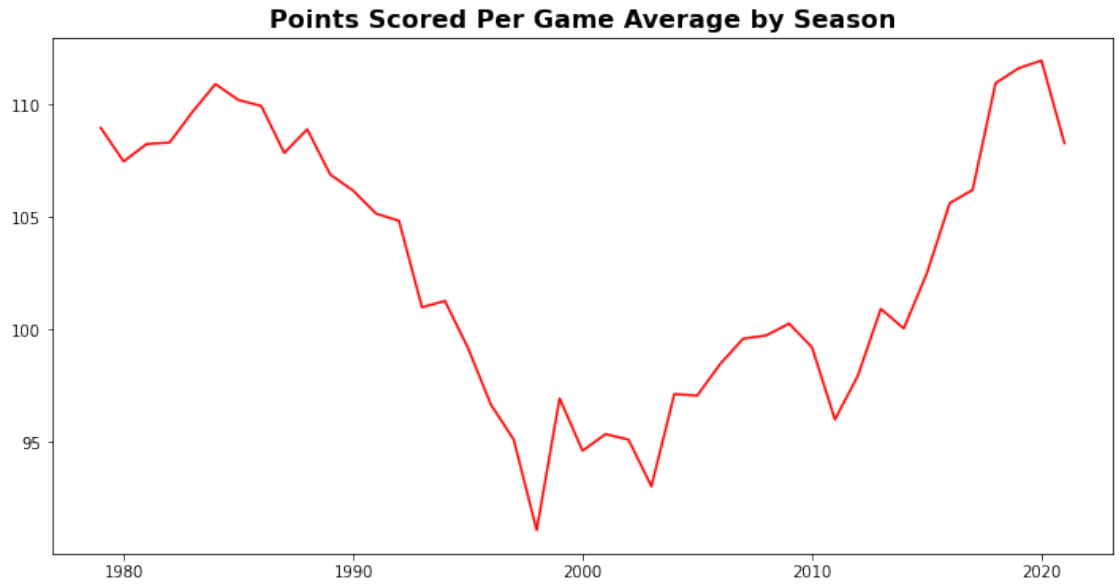


[ ]:
```
avg_score_by_team["avg_score_diff"].mean()
```

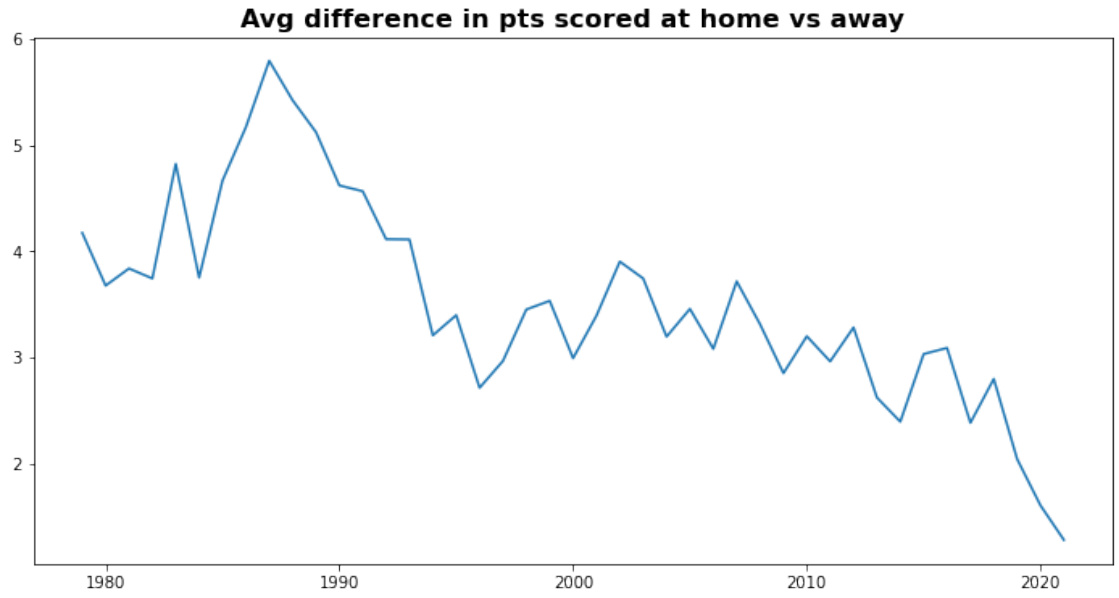
[ ]:
```
3.401926298157454
```

[ ]:
```
avg_score_by_season = all_games[["season", "home_team_avg_score",␣
 ↪"visitor_team_avg_score"]].groupby("season").mean()
avg_score_by_season["mean_avg_score"] =␣
 ↪(avg_score_by_season["home_team_avg_score"] +␣
 ↪avg_score_by_season["visitor_team_avg_score"]) / 2
avg_score_by_season["diff"] = avg_score_by_season["home_team_avg_score"] -␣
 ↪avg_score_by_season["visitor_team_avg_score"]
```

[ ]:
```
plt.figure(figsize=(12,6))
plt.title("Points Scored Per Game Average by Season", fontdict)
plt.plot(avg_score_by_season.index, avg_score_by_season["mean_avg_score"],␣
  ↪color="red")
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Points Scored Per␣
  ↪Game Average by Season.png")
plt.show()
```



[ ]:
```
plt.figure(figsize=(12,6))
plt.plot(avg_score_by_season.index, avg_score_by_season["diff"])
plt.title("Avg difference in pts scored at home vs away", fontdict)
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Points Scored Per␣
  ↪Game Average by Season.png")
plt.show()
```



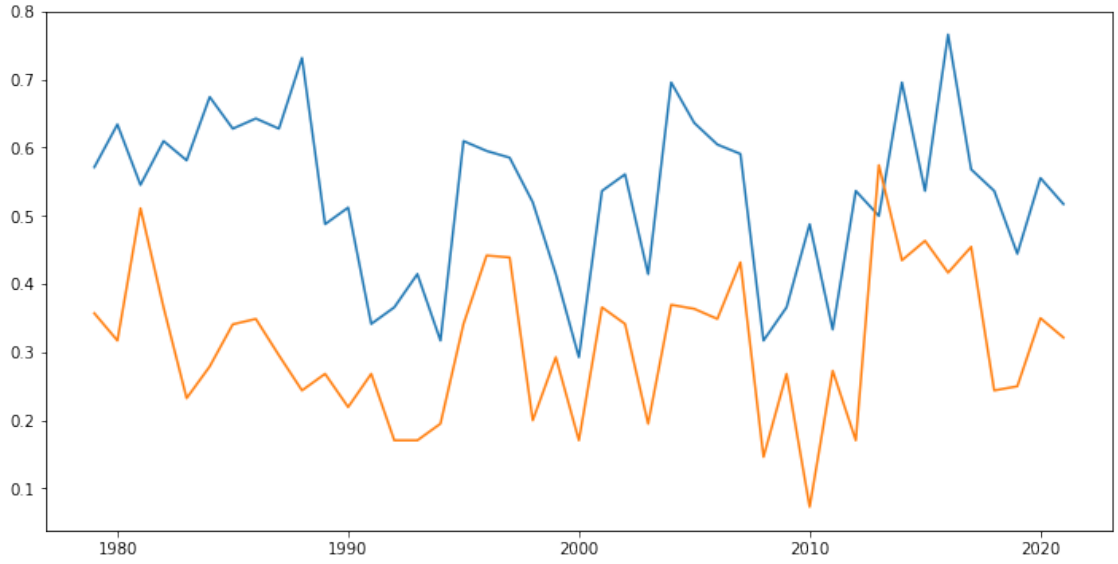
##Getting Washington Stats

[ ]:
```
washington_home = all_games[all_games["home_team.full_name"].eq("Washington␣
↪Wizards")]
washington_away = all_games[all_games["visitor_team.full_name"].eq("Washington␣
↪Wizards")]
washington = pd.concat([washington_home, washington_away])
```

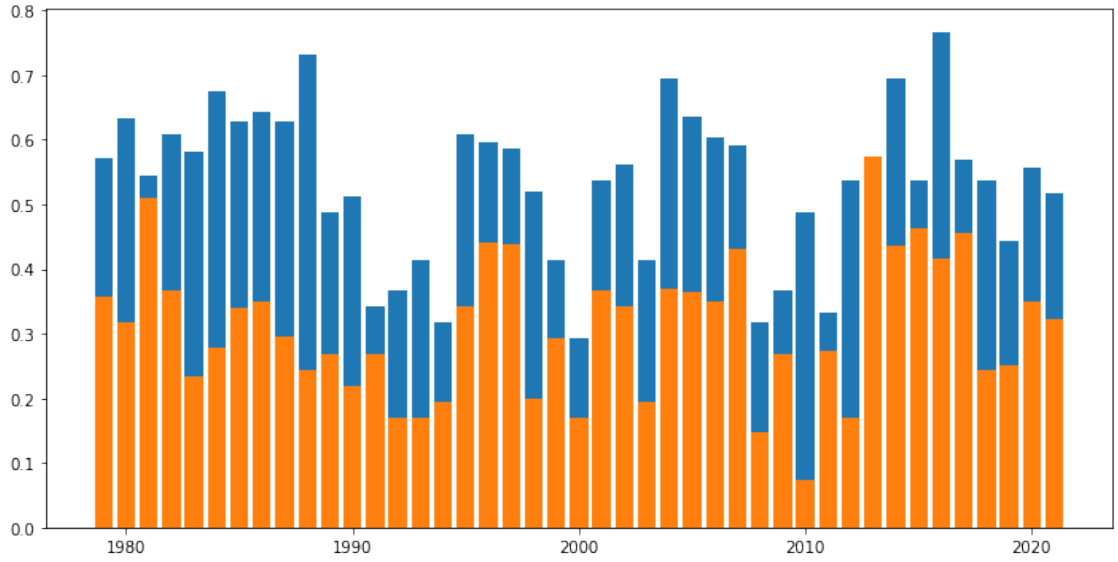
[ ]:
```
washington_home_win_pct = washington_home[["season", "winner"]].
↪groupby("season").sum() / washington_home[["season", "winner"]].
↪groupby("season").count()
```

[ ]:
```
washington_away_win_pct = 1 - washington_away[["season", "winner"]].
↪groupby("season").sum() / washington_away[["season", "winner"]].
↪groupby("season").count()
```

[ ]:
```
plt.figure(figsize = (12,6))
plt.plot(washington_home_win_pct)
plt.plot(washington_away_win_pct)
plt.savefig("/content/drive/MyDrive/Machine Learning NBA /Washington Game␣
↪Points.png")
plt.show()
```



[ ]:
```
plt.figure(figsize = (12,6))
plt.bar(washington_home_win_pct.index, washington_home_win_pct.winner)
plt.bar(washington_away_win_pct.index, washington_away_win_pct.winner)
plt.show()
```



##Stats Data

[ ]:
```
stats = pd.read_csv("/content/drive/MyDrive/Machine Learning NBA /Final Data/
↪stats_feats.csv")
```

```
stats
```

[ ]:

	game.id	game.date	game.season	winner	home_ast	home_blk	\
0	1	2018-10-16	2018	1	23.40	5.35	
1	2	2018-10-16	2018	1	31.55	7.60	
2	3	2018-10-17	2018	0	21.35	5.15	
3	4	2018-10-17	2018	1	23.15	3.40	
4	5	2018-10-17	2018	1	22.55	4.25	
…	…	…	…	…	…		
46668	857658	2022-11-28	2022	0	25.85	4.40	
46669	857659	2022-11-28	2022	0	24.95	4.80	
46670	857660	2022-11-28	2022	0	22.90	6.00	
46671	857661	2022-11-28	2022	1	25.35	3.95	
46672	857662	2022-11-28	2022	1	29.55	3.05	

	home_dreb	home_fg3_pct	home_fg3a	home_fg3m	home_fg_pct	home_fga	\
0	36.05	0.283508	32.10	11.60	0.407498	85.30	
1	34.45	0.186014	27.60	11.35	0.511330	83.35	
2	35.85	0.211261	26.70	9.45	0.415333	87.05	
3	33.55	0.239457	28.45	11.50	0.431416	84.55	
4	33.20	0.291932	25.80	10.00	0.453450	84.70	
…	…	…	…	…	…	…	
46668	32.05	20.284341	33.80	12.50	32.655897	84.20	
46669	34.45	13.977462	39.25	14.65	28.952156	85.15	
46670	33.20	24.626431	33.05	10.85	42.398149	86.40	
46671	32.25	20.856653	32.15	10.60	42.469124	87.40	
46672	34.65	33.899859	37.75	14.35	45.480293	87.85	

	home_fgm	home_ft_pct	home_fta	home_ftm	home_oreb	home_pf	\
0	38.10	0.392525	21.45	16.35	8.80	20.20	
1	43.50	0.385137	20.15	16.35	8.60	18.85	
2	38.70	0.515664	27.40	21.25	9.75	17.05	
3	38.95	0.400628	20.05	14.95	9.30	17.85	
4	41.25	0.432828	20.20	15.30	9.40	18.80	
…	…	…	…	…	…		
46668	40.30	39.248915	25.65	20.35	6.95	19.10	
46669	41.65	29.378268	27.50	20.55	10.90	20.70	
46670	40.20	43.942857	22.15	16.05	9.90	19.20	
46671	43.05	44.212607	22.00	17.35	11.85	20.40	
46672	42.80	46.114460	21.25	17.05	8.75	19.65	

	home_pts	home_reb	home_stl	home_turnover	away_ast	away_blk	\
0	104.15	44.85	7.05	12.90	25.60	4.75	
1	114.70	43.05	7.65	15.25	22.55	5.60	
2	108.10	45.60	6.45	11.35	21.30	4.65	
3	104.35	42.85	7.90	13.30	21.60	4.10	
4	107.80	42.60	7.90	13.00	20.55	4.25	

```
…          …       …       …             …       …       …
46668   113.45   39.00    7.15         13.65   27.15    3.40
46669   118.50   45.35    7.00         13.60   24.30    4.80
46670   107.30   43.10    7.85         12.45   24.15    5.25
46671   114.05   44.10    8.10         12.95   23.00    4.00
46672   117.00   43.40    6.80         11.85   22.50    4.00

       away_dreb  away_fg3_pct  away_fg3a  away_fg3m  away_fg_pct  away_fga  \
0          34.20      0.242414      29.45      10.85     0.451425     83.50
1          32.80      0.235524      31.20      11.20     0.406164     90.10
2          32.00      0.226351      25.30       8.60     0.398101     82.05
3          35.45      0.249849      31.60      10.25     0.425655     85.15
4          30.00      0.276580      25.85       9.40     0.433132     81.05
…          …            …         …          …           …         …
46668      32.40     23.005717      29.45      10.50    42.006387     88.85
46669      33.65     26.124760      31.30      11.75    44.094360     87.80
46670      33.80     26.426683      35.45      12.15    39.111668     88.60
46671      35.10     26.378944      36.95      12.50    38.601197     89.50
46672      32.00     28.075487      39.15      13.50    42.805649     87.50

       away_fgm  away_ft_pct  away_fta  away_ftm  away_oreb  away_pf  \
0         39.20     0.477155     24.25     18.20      11.10    21.15
1         41.50     0.353259     22.60     16.20      12.50    20.05
2         37.80     0.433145     23.85     18.70       9.50    21.55
3         37.45     0.506771     25.15     19.70       9.15    20.65
4         35.85     0.429151     20.30     16.55       9.60    23.85
…         …           …        …         …          …       …
46668     43.20    39.141589     19.15     15.50       9.50    22.40
46669     41.45    40.042889     20.40     16.50       8.60    19.00
46670     38.70    41.549211     23.35     17.60      11.75    20.00
46671     39.10    37.552899     20.45     15.00      10.70    18.95
46672     39.50    46.193101     25.35     18.45      10.50    20.15

       away_pts  away_reb  away_stl  away_turnover  diff_away_ast  \
0        107.45     45.30      8.00          15.55          -2.20
1        110.40     45.30      7.80          12.10           9.00
2        102.90     41.50      8.80          14.30           0.05
3        104.85     44.60      7.30          16.60           1.55
4         97.65     39.60      6.75          14.50           2.00
…         …        …         …             …              …
46668    112.40     41.90      7.95          13.05          -1.30
46669    111.15     42.25      6.65          12.20           0.65
46670    107.15     45.55      6.80          14.25          -1.25
46671    105.70     45.80      7.95          13.30           2.35
46672    110.95     42.50      7.65          15.40           7.05

       diff_away_blk  diff_away_dreb  diff_away_fg3_pct  diff_away_fg3a  \
```

```
0               0.60            1.85           0.041094            2.65
1               2.00            1.65          -0.049510           -3.60
2               0.50            3.85          -0.015089            1.40
3              -0.70           -1.90          -0.010392           -3.15
4               0.00            3.20           0.015352           -0.05
…               …               …              …                  …
46668           1.00           -0.35          -2.721376            4.35
46669           0.00            0.80         -12.147298            7.95
46670           0.75           -0.60          -1.800252           -2.40
46671          -0.05           -2.85          -5.522291           -4.80
46672          -0.95            2.65           5.824371           -1.40

       diff_away_fg3m  diff_away_fg_pct  diff_away_fga  diff_away_fgm  \
0                0.75         -0.043927           1.80          -1.10
1                0.15          0.105166          -6.75           2.00
2                0.85          0.017233           5.00           0.90
3                1.25          0.005761          -0.60           1.50
4                0.60          0.020318           3.65           5.40
…                …             …              …              …
46668            2.00         -9.350490          -4.65          -2.90
46669            2.90        -15.142204          -2.65           0.20
46670           -1.30          3.286482          -2.20           1.50
46671           -1.90          3.867926          -2.10           3.95
46672            0.85          2.674644           0.35           3.30

       diff_away_ft_pct  diff_away_fta  diff_away_ftm  diff_away_oreb  \
0             -0.084629          -2.80          -1.85           -2.30
1              0.031878          -2.45           0.15           -3.90
2              0.082519           3.55           2.55            0.25
3             -0.106143          -5.10          -4.75            0.15
4              0.003677          -0.10          -1.25           -0.20
…                 …              …              …              …
46668          0.107326           6.50           4.85           -2.55
46669        -10.664621           7.10           4.05            2.30
46670          2.393646          -1.20          -1.55           -1.85
46671          6.659708           1.55           2.35            1.15
46672         -0.078641          -4.10          -1.40           -1.75

       diff_away_pf  diff_away_pts  diff_away_reb  diff_away_stl  \
0             -0.95          -3.30          -0.45          -0.95
1             -1.20           4.30          -2.25          -0.15
2             -4.50           5.20           4.10          -2.35
3             -2.80          -0.50          -1.75           0.60
4             -5.05          10.15           3.00           1.15
…             …              …              …              …
46668         -3.30           1.05          -2.90          -0.80
46669          1.70           7.35           3.10           0.35
```

```
46670         -0.80           0.15          -2.45           1.05
46671          1.45           8.35          -1.70           0.15
46672         -0.50           6.05           0.90          -0.85

       diff_away_turnover
0                   -2.65
1                    3.15
2                   -2.95
3                   -3.30
4                   -1.50
…                   …
46668                0.60
46669                1.40
46670               -1.80
46671               -0.35
46672               -3.55

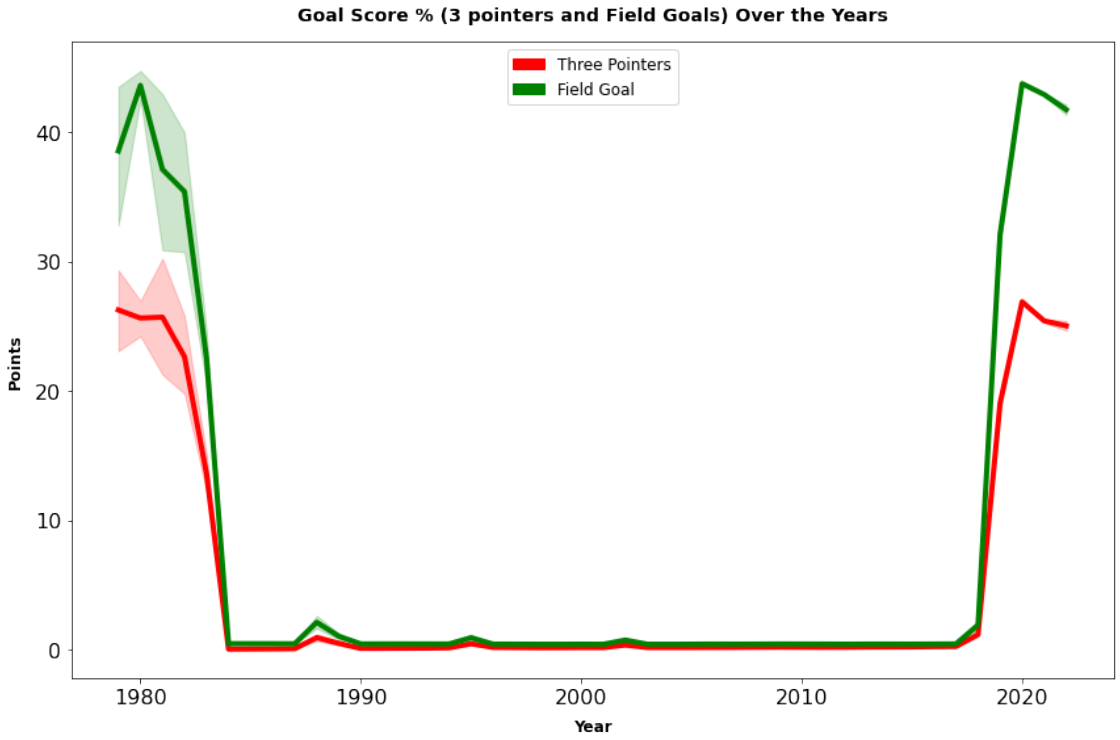
[46673 rows x 58 columns]
```

[ ]:
```
fig, ax = plt.subplots(figsize=(12, 8))
sns.lineplot(data=stats, x='game.season', y='home_fg3_pct', ax=ax, color='r',␣
 ↪linewidth=4)
sns.lineplot(data=stats, x='game.season', y='home_fg_pct', ax=ax, color='g',␣
 ↪linewidth=4)

ax.set_title('Goal Score % (3 pointers and Field Goals) Over the Years',␣
 ↪fontsize=14, pad=16, fontweight='bold')
ax.set_xlabel('Year', fontsize=12, labelpad=8, fontweight='bold')
ax.set_ylabel('Points', fontsize=12, labelpad=8, fontweight='bold')

red_patch = mpatches.Patch(color='r', label='Three Pointers')
green_patch = mpatches.Patch(color='g', label='Field Goal')
ax.legend(handles=[red_patch, green_patch], fontsize='large')

plt.xticks(fontsize=16)
plt.yticks(fontsize=16)
plt.tight_layout()
```


Goal Score % (3 pointers and Field Goals) Over the Years
Three Pointers
Field Goal
Points
Year
0
10
20
30
40
1980
1990
2000
2010
2020