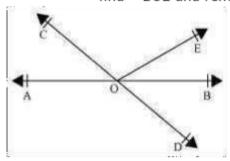
<u>Class IX Chapter 6 – Lines and</u> <u>Angles Maths</u>

Exercise 6.1 Question 1:

In the given figure, lines AB and CD intersect at O. If $\angle AOC + \angle BOE = 70^{\circ}$ and a = 2x, and b = 3x

 $\angle BOD = 40^{\circ}$, find $\angle BOE$ and reflex $\angle COE$.



Answer:

AB is a straight line, rays OC and OE stand on it.

$$\Rightarrow$$
 ($\angle AOC + \angle BOE$) + $\angle COE = 180^{\circ}$

$$\Rightarrow$$
 70° + \angle COE = 180°

$$\Rightarrow \angle COE = 180^{\circ} - 70^{\circ} = 110^{\circ}$$

Reflex
$$\angle COE = 360^{\circ} - 110^{\circ} = 250^{\circ}$$

CD is a straight line, rays OE and OB stand on it.

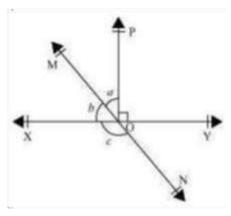
$$\Rightarrow$$
 110° + \angle BOE + 40° = 180°

$$\Rightarrow \angle BOE = 180^{\circ} - 150^{\circ} = 30^{\circ}$$

Question 2:

In the given figure, lines XY and MN intersect at O. If \angle POY = $\frac{90^{\circ}}{}$ and a:b = 2 : 3,

find c.



Answer:

Let the common ratio between a and b be x. $\dot{}$ XY is a straight line, rays OM and OP stand on it.

$$^{\circ}$$
 $^{\prime}$ XOM + MOP + $^{\prime}$ POY = 180° b + a + POY = 180°
3x + 2x + 90° = 180° 5x = 90° x = 18° a =

$$2x = 2 \times 18 = 36^{\circ} b =$$

$$3x = 3 \times 18 = 54^{\circ}$$

MN is a straight line. Ray OX stands on it.

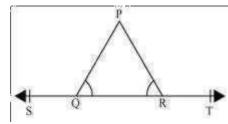
$$ab + c = 180^{\circ}$$
 (Linear Pair)

$$54^{\circ} + c = 180^{\circ} c = 180^{\circ} -$$

$$54^{\circ} = 126^{\circ} \therefore c = 126^{\circ}$$

Question 3:

In the given figure, \angle PQR = \angle PRQ, then prove that \angle PQS = \angle PRT.



Answer:

In the given figure, ST is a straight line and ray QP stands on it.

PQS + PQR = 180° (Linear Pair)

PQR = 180° - PQS (1)

PRT +
$$\angle$$
PRQ = 180° (Linear Pair)

PRQ = 180° - PRT (2)

It is given that $\stackrel{\angle}{PQR} = _{\angle} PRQ$.

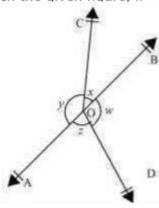
Equating equations (1) and (2), we obtain

= ∠PRT

Question 4:

x+y=w+z,

In the given figure, if



Answer:

It can be observed that, x + y + z + w then prove that AOB is a line.

= 360° (Complete angle) It is given

that,
$$x + y = z + w \therefore x + y + x + y$$

 $= 360^{\circ}$

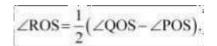
$$2(x + y) = 360^{\circ} x$$

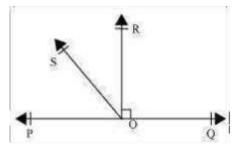
$$+ y = 180^{\circ}$$

Since x and y form a linear pair, AOB is a line.

Question 5:

In the given figure, POQ is a line. Ray OR is perpendicular to line PQ. OS is another ray lying between rays OP and OR. Prove that





Answer:

It is given that OR PQ

: ::POR = 90°

$$\therefore ROS = 90^{\circ} - \therefore POS \dots (1)$$

$$\therefore$$
QOR = 90° (As OR \therefore PQ)

$$\therefore QOS - \therefore ROS = 90^{\circ}$$

$$::ROS = ::QOS - 90^{\circ} ... (2)$$

On adding equations (1) and (2), we obtain

$$\frac{1}{1}$$

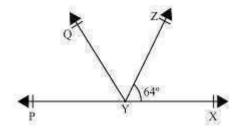
$$ROS = \frac{2}{2}OS - POS 2$$

$$ROS = QOS - POS) ($$

Question 6:

It is given that $AXYZ = 64^{\circ}$ and XY is produced to point P. Draw a figure from the given information. If ray YQ bisects AXYQ and reflex AXYQ and reflex AXYQ.

Answer:



It is given that line YQ bisects "PYZ.

It can be observed that PX is a line. Rays YQ and YZ stand on it.

$$\dot{X}YZ + ZYQ + QYP = 180^{\circ}$$

$$^{..}$$
 64° + 2 QYP = 180°

Also,
$$Z\dot{Y}Q = QYP = 58^{\circ}$$

Reflex QYP =
$$360^{\circ} - 58^{\circ} = 302^{\circ}$$

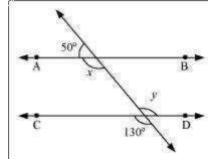
$$XYQ = XYZ + ZYQ$$

$$= 64^{\circ} + 58^{\circ} = 122^{\circ}$$

Exercise 6.2 Question

1:

In the given figure, find the values of x and y and then show that AB || CD.



Answer:

It can be observed that, 50°

$$+ x = 180^{\circ}$$
 (Linear pair) $x =$

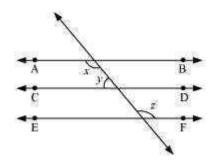
1300 ... (1)

Also, $y = 130^{\circ}$ (Vertically opposite angles)

As x and y are alternate interior angles for lines AB and CD and also measures of these angles are equal to each other, therefore, line AB \parallel CD.

Question 2:

In the given figure, if AB || CD, CD || EF and y: z = 3: 7, find x.



Answer:

It is given that AB || CD and CD || EF

.. AB || CD || EF (Lines parallel to the same line are parallel to each other)

It can be observed that x = z

(Alternate interior angles) ... (1)

It is given that y: z = 3:7

Let the common ratio between y and z be a. ..

y = 3a and z = 7a

Also, $x + y = 180^{\circ}$ (Co-interior angles on the same side of the transversal) z

 $+ y = 180^{\circ}$ [Using equation (1)]

 $7a + 3a = 180^{\circ}$

10a = 180° a =

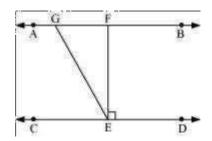
 $18^{\circ} \therefore x = 7a = 7 \times 18^{\circ} =$

126°

Question 3:

In the given figure, If AB || CD, EF $\stackrel{.}{..}$ CD and $\stackrel{.}{..}$ GED 126°, find $\stackrel{.}{A}$ GE, GEF and =

∴FGE.



Answer:

It is given that, AB || CD

$$\therefore$$
 GEF + 90° = 126°

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... AGE and GED are alternate interior angles.

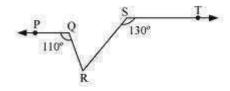
 \therefore However, AGE + FGE = 180° (Linear pair)

$$FGE = 180^{\circ} - 126^{\circ} = 54^{\circ}$$

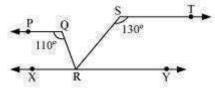
Question 4:

In the given figure, if PQ \parallel ST, \square PQR = 110° and \square RST = 130°, find \square QRS.

[Hint: Draw a line parallel to ST through point R.]



Answer:



Let us draw a line XY parallel to ST and passing through point R.

 $^{\circ}$ PQR + \dot{Q} RX = 180° (Co-interior angles on the same side of transversal QR)

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 110° + $\overset{1}{Q}$ RX = 180°

Also,

 ${}_{1}RST + {}_{2}SRY = 180^{\circ}$ (Co-interior angles on the same side of transversal SR)

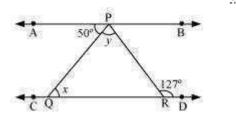
$$^{\circ} + \text{\dot{S}RY} = 180^{\circ} \ 130$$

 $^{\dot{\Box}}$
 $\text{$SRY} = 50^{\circ}$

XY is a straight line. RQ and RS stand on it.

$$^{\circ}$$
 $^{\circ}$ QRX + $^{\circ}$ QRS + $^{\circ}$ SRY = 180° $^{\circ}$ + QRS + 50° = 180° 70 $^{\circ}$ QRS = 180° - 120° = 60°

Question 5:



Answer:

 $^{\circ}$ APR = $^{\circ}$ PRD (Alternate interior angles) In the given figure, if AB || CD, APQ = 50° and PRD = 127°, find x and y.

 $50^{\circ} + y = 127^{\circ} y =$

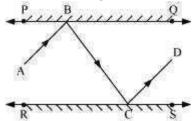
$$127^{\circ} - 50^{\circ} v =$$

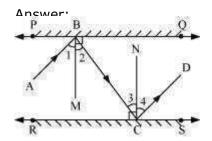
770

Also, APQ = PQR (Alternate interior angles)

$$50^{\circ} = x$$
 $x = 50^{\circ}$ and $y = 77^{\circ}$ Question 6:

In the given figure, PQ and RS are two mirrors placed parallel to each other. An incident ray AB strikes the mirror PQ at B, the reflected ray moves along the path BC and strikes the mirror RS at C and again reflects back along CD. Prove that AB || CD.





Let us draw BM "PQ and CN "RS.

As PQ || RS,

Therefore, BM || CN

Thus, BM and CN are two parallel lines and a transversal line BC cuts them at B and C respectively.

 $\dot{}$ $\dot{}$ = 3 (Alternate interior angles) 2

However, $\overset{.}{1} = 2$ and $3 = \overset{.}{4}$ (By laws of reflection)

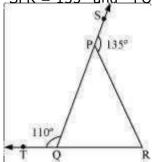
Also,
$$1 + 2 = 3 + 4$$

$$ABC = DCB$$

However, these are alternate interior angles. ${\tt ...}$

1:

In the given figure, sides QP and RQ of Δ PQR are produced to points S and T respectively. If Δ SPR = 135° and Δ PQT = 110°, find PRQ.



Answer:

It is given that,

Ålso, PQT
$$\stackrel{.}{+}$$
 PQR = 180° (Linear pair angles)
 $\stackrel{.}{\cdot}$ $\stackrel{.}{\cdot}$ 110° + PQR = 180°

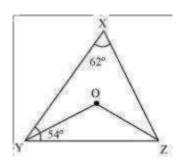
$$POR = 70^{\circ}$$

As the sum of all interior angles of a triangle is 180° , therefore, for ΔPQR ,

QPR + PQR
$$\stackrel{.}{+}$$
 PRQ = 180°
45° + 70° + PRQ = 180°
PRQ = 180° - 115°
PRQ = 65°

Question 2:

In the given figure, $\dot{A}X = 62^{\circ}$, $\dot{X}\dot{Y}Z = 54^{\circ}$. If YO and ZO are the bisectors of $\dot{A}XYZ$ and $\dot{A}XZY$ respectively of ΔXYZ , find OZY and $\dot{Y}QZ$.



Answer:

As the sum of all interior angles of a triangle is 180° , therefore, for ΔXYZ ,

$$^{\circ}X + XYZ + XZY = 180^{\circ}$$

$$^{\circ} + 54^{\circ} + XZY = 180^{\circ} 62$$

$$\therefore$$
 XZY = 180° - 116°

$$XZY = 64$$
 = 64°

$$OZY$$
 = 32° (OZ is the angle bisector of XZY) =

$$\frac{54}{2}$$
 Similarly, OYZ = = 27°

Using angle sum property for ΔOYZ , we obtain

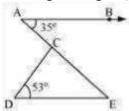
$$^{\circ}$$
OYZ + $^{\circ}$ OZ + $^{\circ}$ OZY = 180°

$$^{\circ}$$
 + YOZ + 32 $^{\circ}$ = 180 $^{\circ}$ 27

$$YOZ = 121^{\circ}$$

Question 3:

In the given figure, if AB \parallel DE, \triangle BAC = 35° and \triangle CDE = 53°, find \triangle DCE.



Answer:

AB || DE and AE is a transversal.

"BAC = CED (Alternate interior angles)

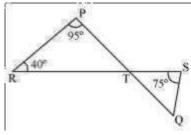
In ΔCDE,

$$\therefore$$
 CDE + \dot{CED} + \dot{DCE} = 180° (Angle sum property of a triangle)
° + 35° + \dot{DCE} = 180° 53
 \therefore
 \therefore DCE = 180° - 88°
DCE = 92°

Question 4:

In the given figure, if lines PQ and RS intersect at point T, such that $_{0}$ PRT = 40°,

RPT = 95° and $^{\circ}$ TSQ = 75°, find $^{\circ}$ SQT.



Answer:

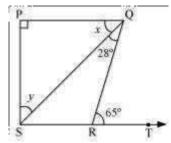
Using angle sum property for Δ PRT, we obtain

By using angle sum property for Δ STQ, we obtain

$$^{\circ}$$
STQ + $^{\circ}$ QT + QST = 180°
 $^{\circ}$ + $^{\circ}$ SQT + 75° = 180° 45
 $^{\circ}$
 $^{\circ}$ SQT = 180° - 120°
 $^{\circ}$ SQT = 60°

Question 5:

In the given figure, if PQ $\stackrel{.}{\sim}$ PS, PQ || SR, $\stackrel{.}{\sim}$ SQR = 2° and $\stackrel{.}{\sim}$ QRT = 65°, then find 8 the values of x and y.



Answer:

It is given that PQ || SR and QR is a transversal line.

$$\therefore$$
PQR = \therefore QRT (Alternate interior angles) x

$$+ 28^{\circ} = 65^{\circ} x = 65^{\circ} - 28^{\circ} x = 37^{\circ}$$

By using the angle sum property for ΔSPQ , we obtain

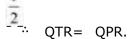
$$\Delta SPQ + x + y = 180^{\circ}$$

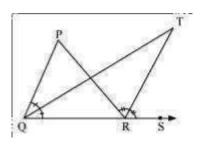
$$90^{\circ} + 37^{\circ} + y = 180^{\circ} y$$

=
$$180^{\circ} - 127^{\circ} \text{ y} = 53^{\circ} \text{ } \text{ } \text{x} = 37^{\circ}$$
 and y = 53° Question 6:

In the given figure, the side QR of ΔPQR is produced to a point S. If the bisectors of "PQR

and ::PRS meet at point T, then prove that ::





Answer:

In $\triangle QTR$, TRS is an exterior angle.

For $\triangle PQR$, PRS is an external angle.

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:. QPR + PQR = PRS
:. QPR + 2 TQR = 2 TRS (As QT and RT are angle bisectors)
:. QPR = 2( TRS - TQR)

QPR = 2 QTR [By using equation (1)]
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