

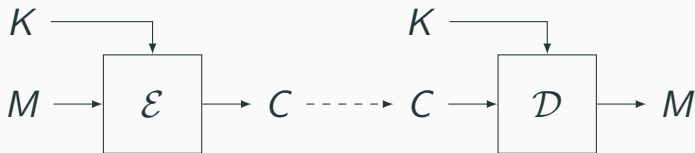
# **(Im)Possibility of Symmetric Encryption against Coordinated Algorithm Substitution Attacks and Key Exfiltration**

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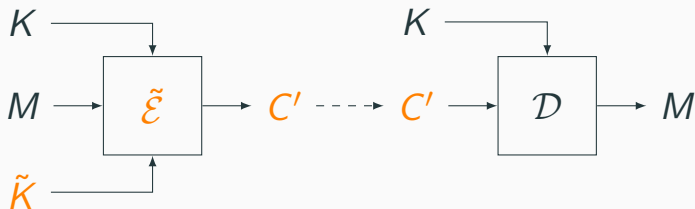
Simone Colombo and Damian Vizàr

LATINCRYPT 2025

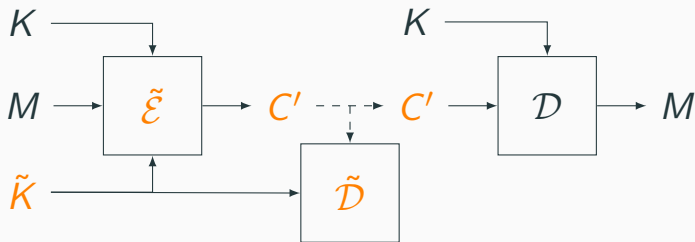
(Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]



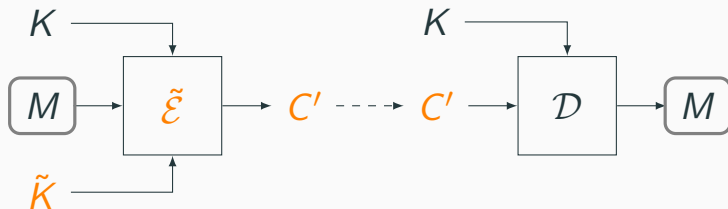
# (Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]



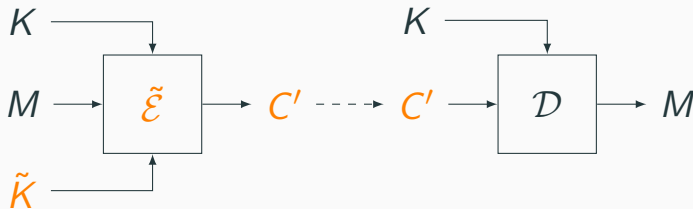
# (Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]



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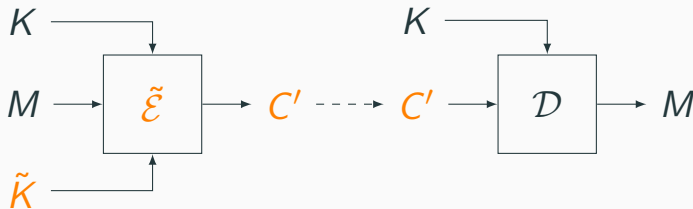


# (Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]



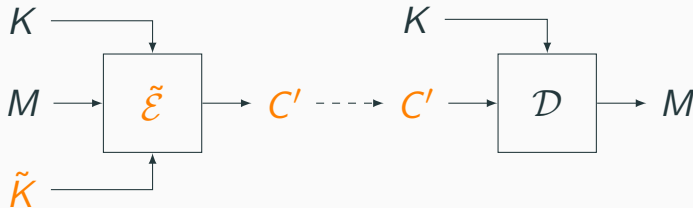
**Theorem 4.** Let  $\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  be a unique ciphertext symmetric encryption scheme. Let  $\tilde{\Pi} = (\tilde{\mathcal{K}}, \tilde{\mathcal{E}}, \tilde{\mathcal{D}})$  be a subversion of  $\Pi$  that obeys the decryptability condition relative to  $\Pi$ . Let  $\mathcal{B}$  be an adversary. Then  $\text{Adv}_{\Pi, \tilde{\Pi}}^{\text{sr}}(\mathcal{B}) = 0$ .

# (Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]



**Theorem 4.** Let  $\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  be a **unique ciphertext symmetric encryption scheme**. Let  $\tilde{\Pi} = (\tilde{\mathcal{K}}, \tilde{\mathcal{E}}, \tilde{\mathcal{D}})$  be a subversion of  $\Pi$  that obeys the decryptability condition relative to  $\Pi$ . Let  $\mathcal{B}$  be an adversary. Then  $\text{Adv}_{\Pi, \tilde{\Pi}}^{\text{srV}}(\mathcal{B}) = 0$ .

# (Im)possibility of simultaneous resistance to **ASAs** and key exfiltration [BPR14]

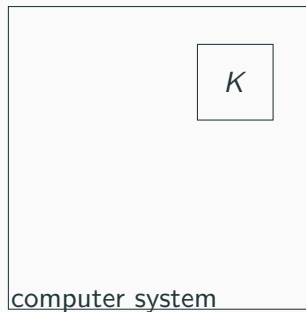


**Theorem 4.** Let  $\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  be a **unique ciphertext symmetric encryption scheme**. Let  $\tilde{\Pi} = (\tilde{\mathcal{K}}, \tilde{\mathcal{E}}, \tilde{\mathcal{D}})$  be a subversion of  $\Pi$  that obeys the decryptability condition relative to  $\Pi$ . Let  $\mathcal{B}$  be an adversary. Then  $\text{Adv}_{\Pi, \tilde{\Pi}}^{\text{srV}}(\mathcal{B}) = 0$ .

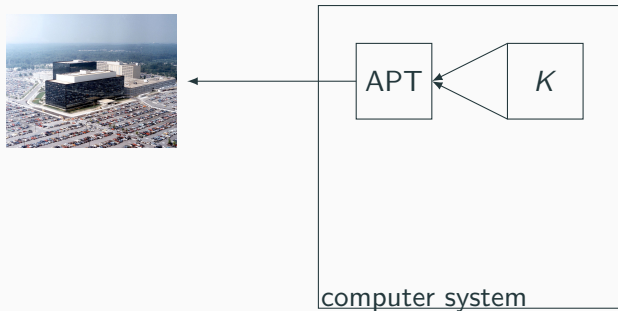
Due to the correctness condition, any unique-ciphertext scheme is **deterministic**.



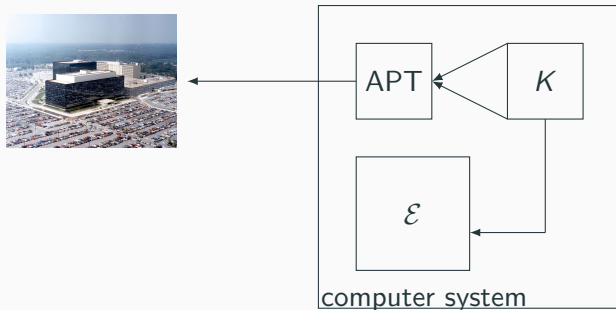
## (Im)possibility of simultaneous resistance to ASAs and **key exfiltration** [BKR16]



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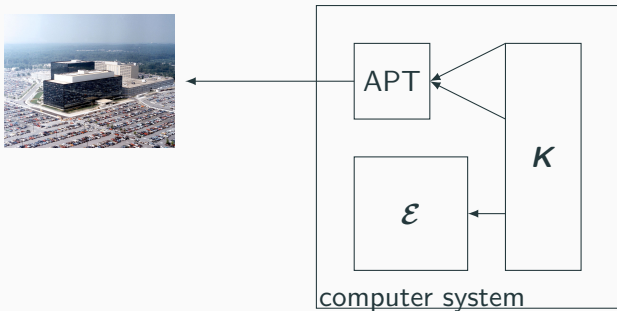


# (Im)possibility of simultaneous resistance to ASAs and **key exfiltration** [BKR16]



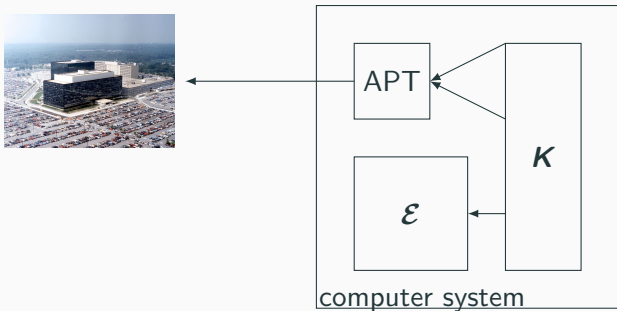
# (Im)possibility of simultaneous resistance to ASAs and **key exfiltration** [BKR16]

$$\text{APT} \approx L \leftarrow \$ Lk^{\text{RO}}(\mathbf{K}), \text{ where } |L| \leq \ell < k, \mathbf{K} \in \{0,1\}^k$$



# (Im)possibility of simultaneous resistance to ASAs and **key exfiltration** [BKR16]

$\text{APT} \approx L \leftarrow \$ \text{Lk}^{\text{RO}}(\mathbf{K})$ , where  $|L| \leq \ell < k$ ,  $\mathbf{K} \in \{0,1\}^k$



Algorithm **SE.Enc**<sup>RO</sup>( $K, M$ )

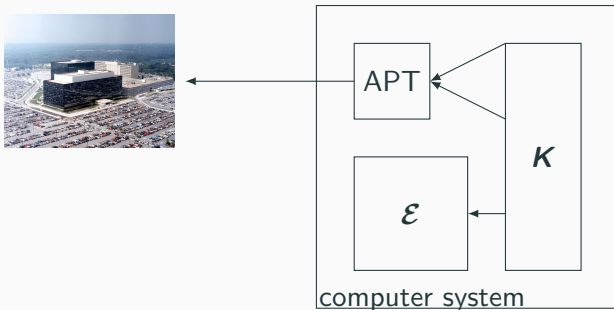
$R \leftarrow \{0,1\}^r$ ;  $K \leftarrow \text{KEY}^{\text{RO}}(\mathbf{K}, R)$   
 $C \leftarrow \text{SE.Enc}(K, M)$ ;  $\overline{C} \leftarrow (R, C)$   
Return  $\overline{C}$

Algorithm **SE.Dec**<sup>RO</sup>( $K, \overline{C}$ )

$(R, C) \leftarrow \overline{C}$   
 $K \leftarrow \text{KEY}^{\text{RO}}(\mathbf{K}, R)$   
 $M \leftarrow \text{SE.Dec}(K, C)$   
Return  $M$

# (Im)possibility of simultaneous resistance to ASAs and **key exfiltration** [BKR16]

$\text{APT} \approx L \leftarrow \$ \text{Lk}^{\text{RO}}(\mathbf{K})$ , where  $|L| \leq \ell < k$ ,  $\mathbf{K} \in \{0,1\}^k$



Algorithm **SE**.Enc<sup>RO</sup>( $\mathbf{K}, M$ )

$R \leftarrow \{0,1\}^r$ ;  $K \leftarrow \text{KEY}^{\text{RO}}(\mathbf{K}, R)$   
 $C \leftarrow \text{SE.Enc}(K, M)$ ;  $\overline{C} \leftarrow (R, C)$   
Return  $\overline{C}$

Algorithm **SE**.Dec<sup>RO</sup>( $\mathbf{K}, \overline{C}$ )

$(R, C) \leftarrow \overline{C}$   
 $K \leftarrow \text{KEY}^{\text{RO}}(\mathbf{K}, R)$   
 $M \leftarrow \text{SE.Dec}(K, C)$   
Return  $M$

## (Im)possibility of **simultaneous resistance** to ASAs and key exfiltration

Resisting ASAs requires deterministic encryption [BPR14].

Resisting key exfiltration with big keys requires randomized encryption [BKR16].

## (Im)possibility of **simultaneous resistance** to ASAs and key exfiltration

Resisting ASAs requires deterministic encryption [BPR14].

Resisting key exfiltration with big keys requires randomized encryption [BKR16].

*“Whether any defense against ASAs is possible in the big-key setting remains open.”*

[BKR16]



- ① Previous security definitions
- ② Security model for simultaneous ASAs and key exfiltration: SURV-LIND
- ③ Impossibility: generic attack
- ④ Possibility: big-key encryption with sessions
- ⑤ Conclusion and future work

## Previous security definitions

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## Surveillance security for ASAs [BPR14]

Game $\text{SURV}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle $\text{KEY}(i)$	Oracle $\text{ENC}(M, A, i)$
$b \leftarrow_{\$} \{0, 1\}$	<b>if</b> $(K_i = \perp)$ <b>then</b>	<b>if</b> $(K_i = \perp)$ <b>then return</b> $\perp$
$\tilde{K} \leftarrow_{\$} \tilde{\mathcal{K}}$	$K_i \leftarrow_{\$} \mathcal{K}$	<b>if</b> $(b = 1)$ <b>then</b> $(C, \sigma_i) \leftarrow_{\$} \mathcal{E}(K_i, M, A, \sigma_i)$
$b' \leftarrow \mathcal{B}^{\text{KEY}, \text{ENC}}(\tilde{K})$	$\sigma_i \leftarrow \varepsilon$	<b>else</b> $(C, \sigma_i) \leftarrow_{\$} \tilde{\mathcal{E}}(\tilde{K}, K_i, M, A, \sigma_i, i)$
<b>return</b> $(b = b')$	<b>return</b> $\varepsilon$	<b>return</b> $C$

Adversary  $\mathcal{B}$  with master key  $\tilde{K}$  must distinguish between correct  $\mathcal{E}$  and subverted  $\tilde{\mathcal{E}}$ .

## Another SURV definition [this work]

Game $\text{SURV}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle $\text{KEY}(i)$	Oracle $\text{ENC}(M, A, i)$
$b \leftarrow_{\$} \{0, 1\}$	<b>if</b> $(K_i = \perp)$ <b>then</b>	<b>if</b> $(K_i = \perp)$ <b>then return</b> $\perp$
$\tilde{K} \leftarrow_{\$} \tilde{\mathcal{K}}$	$K_i \leftarrow_{\$} \mathcal{K}$	$(C_0, \sigma_i) \leftarrow_{\$} \tilde{\mathcal{E}}(\tilde{K}, K_i, M, A, \sigma_i, i)$
$b' \leftarrow \mathcal{B}^{\text{KEY}, \text{ENC}}(\tilde{K})$	$\sigma_i \leftarrow \varepsilon$	$C_1 \leftarrow_{\$} \{0, 1\}^{ C_0 }$
<b>return</b> $(b = b')$	<b>return</b> $\varepsilon$	<b>return</b> $C_b$

$\mathcal{B}$  with  $\tilde{K}$  must distinguish between random  $C_1$  and  $C_0$  that the subverted  $\tilde{\mathcal{E}}$  returns.

## Another SURV definition [this work]

Game $\text{SURV}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle $\text{KEY}(i)$	Oracle $\text{ENC}(M, A, i)$
$b \leftarrow_{\$} \{0, 1\}$	<b>if</b> $(K_i = \perp)$ <b>then</b>	<b>if</b> $(K_i = \perp)$ <b>then return</b> $\perp$
$\tilde{K} \leftarrow_{\$} \tilde{\mathcal{K}}$	$K_i \leftarrow_{\$} \mathcal{K}$	$(C_0, \sigma_i) \leftarrow_{\$} \tilde{\mathcal{E}}(\tilde{K}, K_i, M, A, \sigma_i, i)$
$b' \leftarrow \mathcal{B}^{\text{KEY}, \text{ENC}}(\tilde{K})$	$\sigma_i \leftarrow \varepsilon$	$C_1 \leftarrow_{\$} \{0, 1\}^{ C_0 }$
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$\mathcal{B}$  with  $\tilde{K}$  must distinguish between random  $C_1$  and  $C_0$  that the subverted  $\tilde{\mathcal{E}}$  returns.

We prove that  $\text{SURV}_{\$} \xleftrightarrow{\text{IND\$-CPA}} \text{SURV}$ .

## Indistinguishability in presence of leakage for key exfiltration [BKR16]

Game $\text{LIND}_{\Pi}^{\mathcal{B}}$	Oracle $\text{ENC}(M_0, M_1)$
$(\text{Lk}, \sigma) \leftarrow \mathcal{B}^{\text{RO}}$	$C \leftarrow \mathcal{E}^{\text{RO}}(\mathbf{K}, M_b)$
$\mathbf{K} \leftarrow \{0, 1\}^k$	<b>return</b> $C$
$L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$	
$b \leftarrow \{0, 1\}$	
$b' \leftarrow \mathcal{B}^{\text{ENC}, \text{RO}}(L, \sigma)$	
<b>return</b> $(b = b')$	

Classic left-or-right IND-CPA game, taking leakage  $L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$  into account.

## Another LIND definition [this work]

Game $\text{LIND}_{\Pi}^{\mathcal{B}}$	Oracle $\text{ENC}(M)$
$(Lk, \sigma) \leftarrow \mathcal{B}^{\text{RO}}$	$C_0 \leftarrow \mathcal{E}^{\text{RO}}(\mathbf{K}, M)$
$\mathbf{K} \leftarrow \$ \{0, 1\}^k$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$
$L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$	<b>return</b> $C_b$
$b \leftarrow \$ \{0, 1\}$	
$b' \leftarrow \mathcal{B}^{\text{ENC}, \text{RO}}(L, \sigma)$	
<b>return</b> $(b = b')$	

Classic IND\$-CPA game, taking leakage  $L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$  into account.

## Another LIND definition [this work]

Game $\text{LIND\$}_{\Pi}^{\mathcal{B}}$	Oracle $\text{ENC}(M)$
$(\text{Lk}, \sigma) \leftarrow \mathcal{B}^{\text{RO}}$	$C_0 \leftarrow \$ \mathcal{E}^{\text{RO}}(\mathbf{K}, M)$
$\mathbf{K} \leftarrow \$ \{0, 1\}^k$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$
$L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$	<b>return</b> $C_b$
$b \leftarrow \$ \{0, 1\}$	
$b' \leftarrow \mathcal{B}^{\text{ENC}, \text{RO}}(L, \sigma)$	
<b>return</b> $(b = b')$	

Classic IND\$-CPA game, taking leakage  $L \leftarrow \text{Lk}^{\text{RO}}(\mathbf{K})$  into account.

We show that  $\text{LIND\$} \implies \text{LIND}$ .



## Security model for simultaneous ASAs and KE

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# Security model for simultaneous ASAs and key exfiltration [this work]

Game SURV-LIND $_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$

$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$

$(\text{Lk}, \sigma) \leftarrow \mathcal{B}^{\text{RO}}(\tilde{K})$

$b \leftarrow \$ \{0, 1\}$

$b' \leftarrow \mathcal{B}^{\text{LEAK, ENC, RO}}(\tilde{K}, \sigma)$

**return**  $(b = b')$

Oracle ENC( $M, A, i$ )

**if**  $(K_i = \perp)$  **then return**  $\perp$

$(C_0, \sigma_i) \leftarrow \$ \tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$

$C_1 \leftarrow \$ \{0, 1\}^{|C_0|}$

**return**  $C_b$

Oracle LEAK( $i$ )

**if**  $(K_i = \perp)$  **then**

$K_i \leftarrow \$ \{0, 1\}^k$

$\sigma_i \leftarrow \varepsilon$

$L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$

**return**  $L$

**return**  $\perp$

# Security model for simultaneous ASAs and key exfiltration [this work]

Game SURV-LIND $_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle ENC( $M, A, i$ )	Oracle LEAK( $i$ )
$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$	<b>if</b> ( $K_i = \perp$ ) <b>then return</b> $\perp$	<b>if</b> ( $K_i = \perp$ ) <b>then</b>
$(Lk, \sigma) \leftarrow \mathcal{B}^{\text{RO}}(\tilde{K})$	$(C_0, \sigma_i) \leftarrow \$ \tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$	$K_i \leftarrow \$ \{0, 1\}^k$
$b \leftarrow \$ \{0, 1\}$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$	$\sigma_i \leftarrow \varepsilon$
$b' \leftarrow \mathcal{B}^{\text{LEAK, ENC, RO}}(\tilde{K}, \sigma)$	<b>return</b> $C_b$	$L \leftarrow \$ Lk^{\text{RO}}(K_i)$
<b>return</b> ( $b = b'$ )		<b>return</b> $L$
		<b>return</b> $\perp$

As in SURV\$ (equiv. to SURV) distinguish between random  $C_1$  and  $C_0$  from  $\tilde{\mathcal{E}}$ , with leakage  $L \leftarrow \$ Lk^{\text{RO}}(K)$  as in LIND\$ (equiv. to LIND) through LEAK oracle.

# Security model for simultaneous ASAs and key exfiltration [this work]

Game SURV-LIND $_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle ENC( $M, A, i$ )	Oracle LEAK( $i$ )
$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$	<b>if</b> ( $K_i = \perp$ ) <b>then return</b> $\perp$	<b>if</b> ( $K_i = \perp$ ) <b>then</b>
$(\text{Lk}, \sigma) \leftarrow \mathcal{B}^{\text{RO}}(\tilde{K})$	$(C_0, \sigma_i) \leftarrow \$ \tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$	$K_i \leftarrow \$ \{0, 1\}^k$
$b \leftarrow \$ \{0, 1\}$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$	$\sigma_i \leftarrow \varepsilon$
$b' \leftarrow \mathcal{B}^{\text{LEAK}, \text{ENC}, \text{RO}}(\tilde{K}, \sigma)$	<b>return</b> $C_b$	$L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$
<b>return</b> ( $b = b'$ )		<b>return</b> $L$
		<b>return</b> $\perp$

As in SURV\$ (equiv. to SURV) distinguish between random  $C_1$  and  $C_0$  from  $\tilde{\mathcal{E}}$ ,  
**with leakage**  $L \leftarrow \$ \text{Lk}^{\text{RO}}(K)$  **as in LIND\$ (equiv. to LIND) through Leak oracle.**

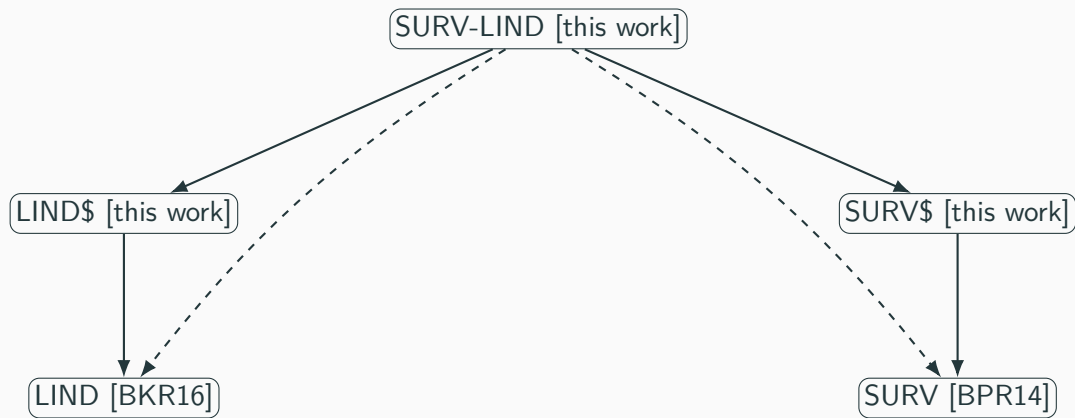
# Security model for simultaneous ASAs and key exfiltration [this work]

Game SURV-LIND $_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle ENC( $M, A, i$ )	Oracle LEAK( $i$ )
$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$	<b>if</b> ( $K_i = \perp$ ) <b>then return</b> $\perp$	<b>if</b> ( $K_i = \perp$ ) <b>then</b>
$(Lk, \sigma) \leftarrow \mathcal{B}^{\text{RO}}(\tilde{K})$	$(C_0, \sigma_i) \leftarrow \$ \tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$	$K_i \leftarrow \$ \{0, 1\}^k$
$b \leftarrow \$ \{0, 1\}$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$	$\sigma_i \leftarrow \varepsilon$
$b' \leftarrow \mathcal{B}^{\text{LEAK, ENC, RO}}(\tilde{K}, \sigma)$	<b>return</b> $C_b$	$L \leftarrow \$ Lk^{\text{RO}}(K_i)$
<b>return</b> ( $b = b'$ )		<b>return</b> $L$
		<b>return</b> $\perp$

As in SURV\$ (equiv. to SURV) distinguish between random  $C_1$  and  $C_0$  from  $\tilde{\mathcal{E}}$ , with leakage  $L \leftarrow \$ Lk^{\text{RO}}(K)$  as in LIND\$ (equiv. to LIND) through LEAK oracle.

We show that SURV-LIND  $\Rightarrow$  LIND\$ and SURV-LIND  $\Rightarrow$  SURV\$.

## Summary of security notions



Solid: proved.      Dashed: by transitivity.

**Impossibility: generic attack**

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## Generic attack: leakage function

Algorithm  $\text{Lk}_{i,\tilde{K},M}^{\text{RO}}(K_i)$

// state management

$r \leftarrow \text{RO}(\langle i, \tilde{K}, 0 \rangle, |r|)$

$(C, \sigma') \leftarrow \mathcal{E}^{\text{RO}}(K_i, M, \varepsilon, \sigma; r)$

**return**  $\text{RO}(\langle C \rangle, \ell)$

Returns the  $\ell$ -bits “hash” of the ciphertext from the encryption of  $M$  with coins  $r$ .



## Generic attack: subversion

<p>Algorithm <math>\tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, \mathbf{K}_i, M, A, \sigma, i)</math></p> <hr/> <p>// state management where <math>\sigma</math> parses as <math>\tilde{\sigma}, \bar{\sigma}</math></p> <p><math>r \leftarrow \text{RO}(\langle i, \tilde{K}, \tilde{\sigma} \rangle,  r )</math></p> <p><math>(C, \bar{\sigma}) \leftarrow \mathcal{E}^{\text{RO}}(\mathbf{K}_i, M, A, \sigma; r)</math></p> <p><b>return</b> <math>C, \langle \tilde{\sigma}, \bar{\sigma} \rangle</math></p>
--

Returns the ciphertext of  $M$  under the same coins  $r$  used by the leakage function.

## Generic attack

Algorithm  $\mathcal{B}_{\text{drnd}}(\tilde{K}, \tau)$

**if**  $(\tau = \perp)$  **then**

$M \leftarrow \$ \{0, 1\}^\nu$

**return**  $(\text{Lk}_{i, \tilde{K}, M}, M)$

**else**

$M \leftarrow \tau$

$i \leftarrow \$ \mathcal{I}; A \leftarrow \varepsilon$

$L \leftarrow \text{LEAK}(i)$

$C \leftarrow \text{ENC}(M, A, i)$

$b' \leftarrow (L \neq \text{RO}(\langle C \rangle, \ell))$

**return**  $b'$

Algorithm  $\tilde{\mathcal{E}}^{\text{RO}}(\tilde{K}, \mathbf{K}_i, M, A, \sigma, i)$

// state management where  $\sigma$  parses as  $\tilde{\sigma}, \bar{\sigma}$

$r \leftarrow \text{RO}(\langle i, \tilde{K}, \tilde{\sigma} \rangle, |r|)$

$(C, \bar{\sigma}) \leftarrow \mathcal{E}^{\text{RO}}(\mathbf{K}_i, M, A, \sigma; r)$

**return**  $C, \langle \tilde{\sigma}, \bar{\sigma} \rangle$

Algorithm  $\text{Lk}_{i, \tilde{K}, M}^{\text{RO}}(\mathbf{K}_i)$

// state management

$r \leftarrow \text{RO}(\langle i, \tilde{K}, 0 \rangle, |r|)$

$(C, \sigma') \leftarrow \mathcal{E}^{\text{RO}}(\mathbf{K}_i, M, \varepsilon, \sigma; r)$

**return**  $\text{RO}(\langle C \rangle, \ell)$

Adversary  $\mathcal{B}$  gets  $\ell$ -bit “hash”  $L$ , queries  $\text{ENC}$  to get  $C$  and checks  $(L \neq \text{RO}(\langle C \rangle, \ell))$ .

## Generic attack: informal summary

The subversion's control of random coins lets the leakage precompute the ciphertext.

**Possibility: big-key encryption with sessions**

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**Problem:** ASA  $\implies$  force usage of predefined coins  
KE  $\implies$  leakage can precompute ciphertext.  
 $\implies$  complete control.

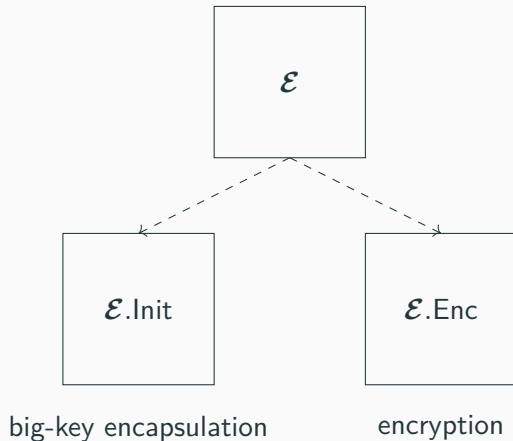
**Problem:** ASA  $\implies$  force usage of predefined coins  
KE  $\implies$  leakage can precompute ciphertext.  
 $\implies$  complete control.

**Solution:** Secure randomness generation.

## Big-key symmetric encryption with sessions

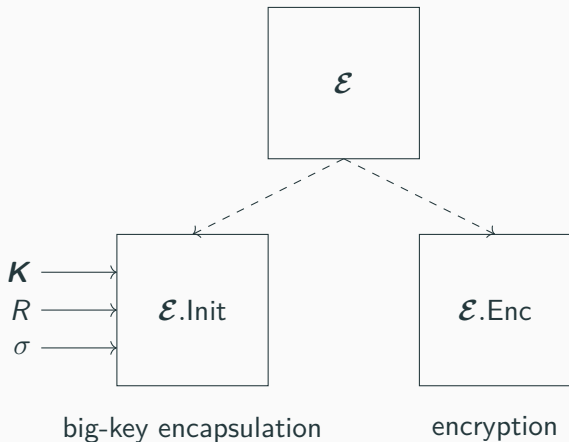


## Big-key symmetric encryption with sessions

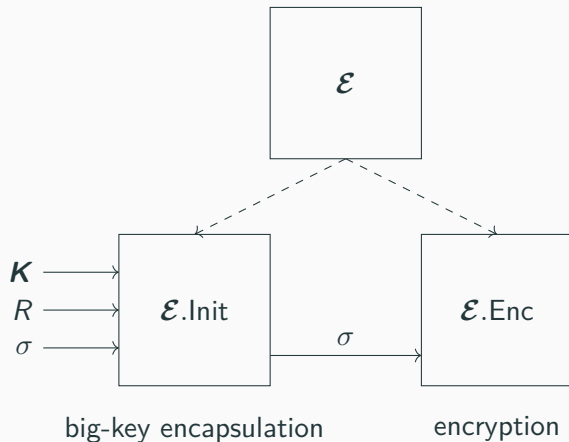




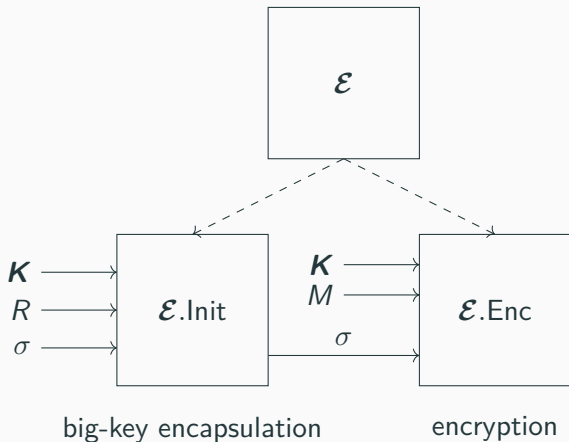
## Big-key symmetric encryption with sessions



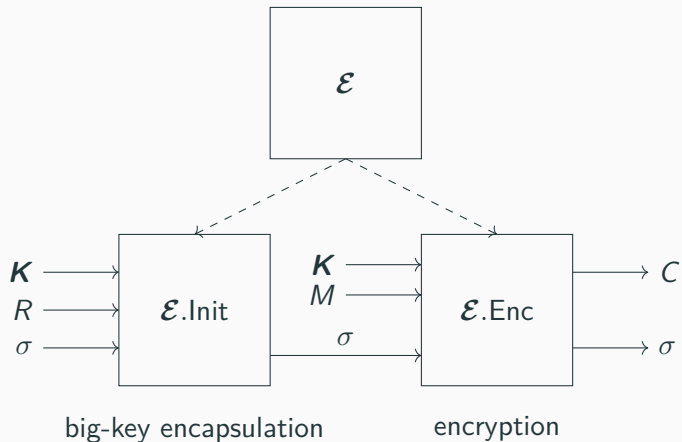
## Big-key symmetric encryption with sessions



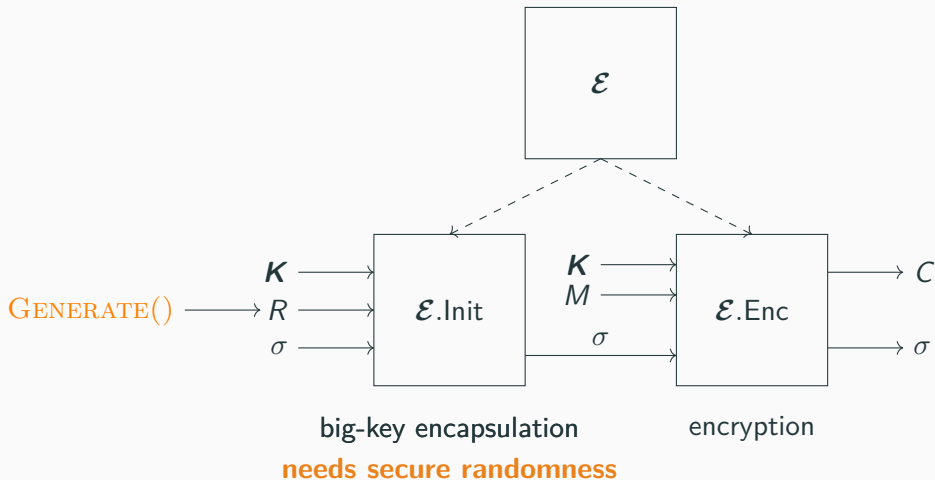
## Big-key symmetric encryption with sessions



## Big-key symmetric encryption with sessions



# Big-key symmetric encryption with sessions



# Security notion: RESIST

Game $\text{RESIST}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle $\text{ENC}(M, A, i)$	Proc. $\text{GENERATE}()$
$\vec{K}_{i, \sigma_i} \leftarrow \perp$ everywhere	<b>if</b> $(\sigma_i = \perp)$ <b>then return</b> $\perp$	$R \leftarrow \$ \mathcal{R}$
$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$	$C_0, \sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Enc}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$	<b>return</b> $R$
$(\text{Lk}, \tau) \leftarrow \$ \mathcal{B}^{\text{RO}}(\tilde{K})$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$	
$b \leftarrow \$ \{0, 1\}$	<b>return</b> $C_b$	
$b' \leftarrow \$ \mathcal{B}^{\text{LEAK, INIT, ENC, RO}}(\tilde{K}, \tau)$	Oracle $\text{INIT}(i)$	
<b>return</b> $(b = b')$	<b>if</b> $(K_i = \perp)$ <b>then return</b> $\perp$	
Oracle $\text{LEAK}(i)$	$R \leftarrow \$ \text{GENERATE}()$	
<b>if</b> $(K_i \neq \perp)$ <b>then return</b> $\perp$	<b>if</b> $R = \perp$ <b>then abort</b>	
$K_i \leftarrow \$ \mathcal{K}; L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$	$\sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Init}^{\text{RO}}(\tilde{K}, K_i, R, \sigma_i, i)$	
<b>return</b> $L$	<b>return</b> $R$	

# Security notion: RESIST

Game $\text{RESIST}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$	Oracle $\text{ENC}(M, A, i)$	Proc. $\text{GENERATE}()$
$\vec{K}_i, \sigma_i \leftarrow \perp$ everywhere	<b>if</b> $(\sigma_i = \perp)$ <b>then return</b> $\perp$	$R \leftarrow \$ \mathcal{R}$
$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$	$C_0, \sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Enc}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$	<b>return</b> $R$
$(\text{Lk}, \tau) \leftarrow \$ \mathcal{B}^{\text{RO}}(\tilde{K})$	$C_1 \leftarrow \$ \{0, 1\}^{ C_0 }$	
$b \leftarrow \$ \{0, 1\}$	<b>return</b> $C_b$	
$b' \leftarrow \$ \mathcal{B}^{\text{LEAK, INIT, ENC, RO}}(\tilde{K}, \tau)$	Oracle $\text{INIT}(i)$	
<b>return</b> $(b = b')$	<b>if</b> $(K_i = \perp)$ <b>then return</b> $\perp$	
Oracle $\text{LEAK}(i)$	$R \leftarrow \$ \text{GENERATE}()$	
<b>if</b> $(K_i \neq \perp)$ <b>then return</b> $\perp$	<b>if</b> $R = \perp$ <b>then abort</b>	
$K_i \leftarrow \$ \mathcal{K}; L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$	$\sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Init}^{\text{RO}}(\tilde{K}, K_i, R, \sigma_i, i)$	
<b>return</b> $L$	<b>return</b> $R$	

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Game  $\text{RESIST}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$

$\vec{K}_i, \sigma_i \leftarrow \perp$  everywhere

$\tilde{K} \leftarrow \$ \tilde{\mathcal{K}}$

$(\text{Lk}, \tau) \leftarrow \$ \mathcal{B}^{\text{RO}}(\tilde{K})$

$b \leftarrow \$ \{0, 1\}$

$b' \leftarrow \$ \mathcal{B}^{\text{LEAK, INIT, ENC, RO}}(\tilde{K}, \tau)$

**return**  $(b = b')$

Oracle  $\text{LEAK}(i)$

**if**  $(K_i \neq \perp)$  **then return**  $\perp$

$K_i \leftarrow \$ \mathcal{K}; L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$

**return**  $L$

Oracle  $\text{ENC}(M, A, i)$

**if**  $(\sigma_i = \perp)$  **then return**  $\perp$

$C_0, \sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Enc}^{\text{RO}}(\tilde{K}, K_i, M, A, \sigma_i, i)$  **return**  $R$

$C_1 \leftarrow \$ \{0, 1\}^{|C_0|}$

**return**  $C_b$

Oracle  $\text{INIT}(i)$

**if**  $(K_i = \perp)$  **then return**  $\perp$

$R \leftarrow \$ \text{GENERATE}()$

**if**  $R = \perp$  **then abort**

$\sigma_i \leftarrow \$ \tilde{\mathcal{E}}.\text{Init}^{\text{RO}}(\tilde{K}, K_i, R, \sigma_i, i)$

**return**  $R$

Proc.  $\text{GENERATE}()$

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Game  $\text{RESIST}_{\Pi, \tilde{\Pi}}^{\mathcal{B}}$

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$b' \leftarrow \$ \mathcal{B}^{\text{LEAK, INIT, ENC, RO}}(\tilde{K}, \tau)$

**return**  $(b = b')$

Oracle  $\text{LEAK}(i)$

**if**  $(K_i \neq \perp)$  **then return**  $\perp$

$K_i \leftarrow \$ \mathcal{K}; L \leftarrow \$ \text{Lk}^{\text{RO}}(K_i)$

**return**  $L$

Oracle  $\text{ENC}(M, A, i)$

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$C_0, \sigma_i \leftarrow \$ \tilde{\mathcal{E}}^{\text{Enc}^{\text{RO}}}(\tilde{K}, K_i, M, A, \sigma_i, i)$

$C_1 \leftarrow \$ \{0, 1\}^{|C_0|}$

**return**  $C_b$

Oracle  $\text{INIT}(i)$

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$R \leftarrow \$ \text{GENERATE}()$

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$\sigma_i \leftarrow \$ \tilde{\mathcal{E}}^{\text{Init}^{\text{RO}}}(\tilde{K}, K_i, R, \sigma_i, i)$

**return**  $R$

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$R \leftarrow \$ \mathcal{R}$

**return**  $R$

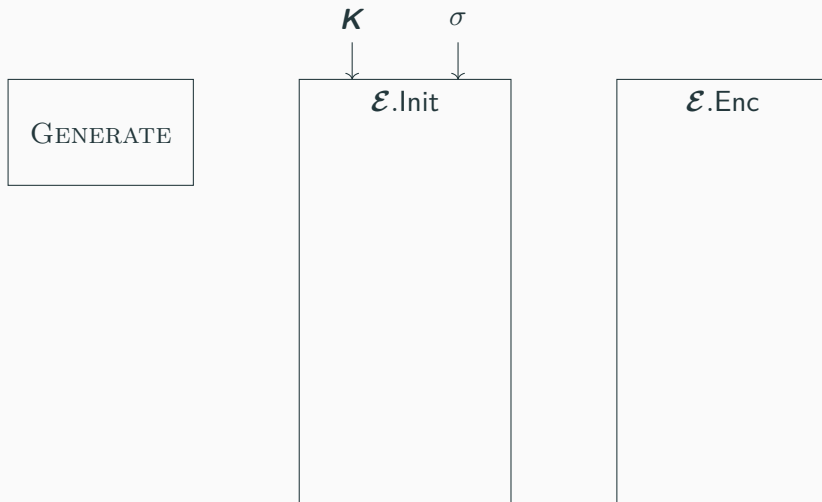
## Construction $\text{SES}[\Pi, k, P]$ : encryption

GENERATE

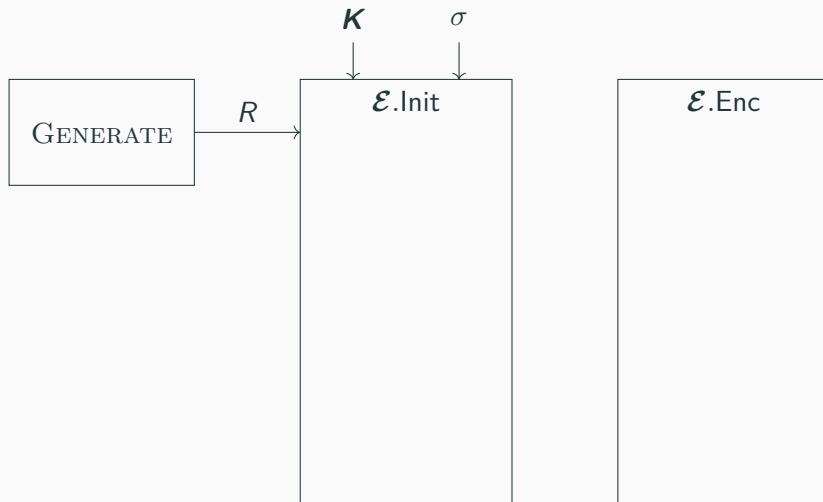
$\mathcal{E}.\text{Init}$

$\mathcal{E}.\text{Enc}$

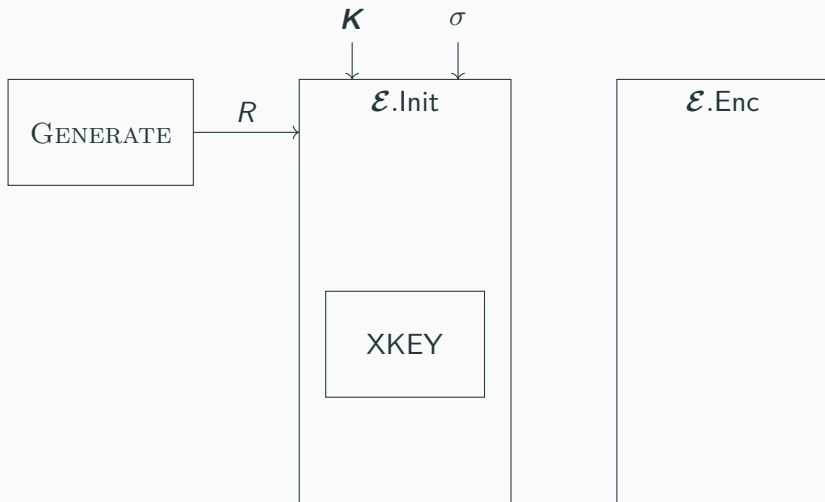
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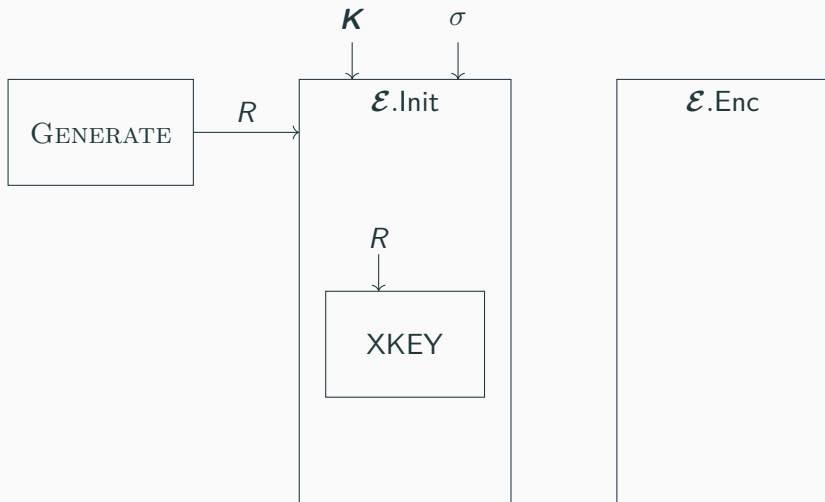


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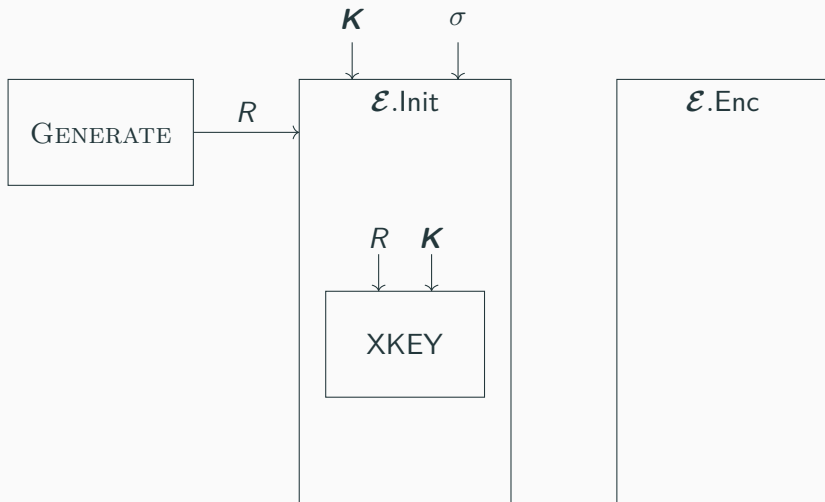
XKEY is the big-key encapsulation scheme from [BKR16].

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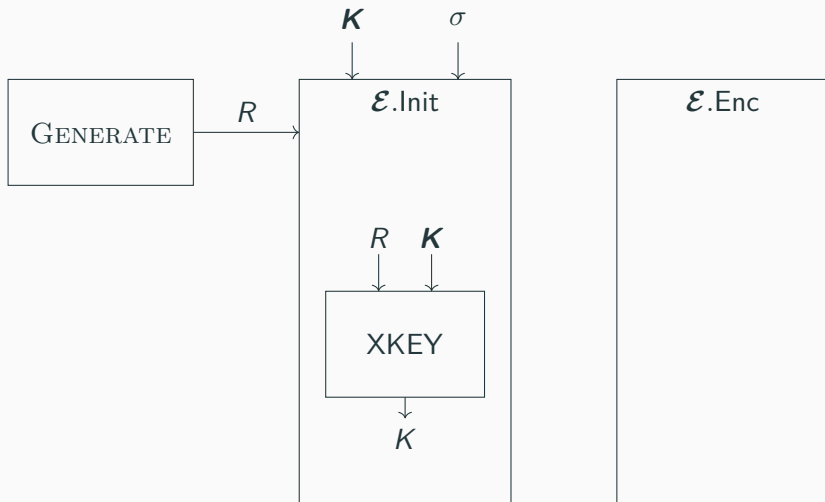
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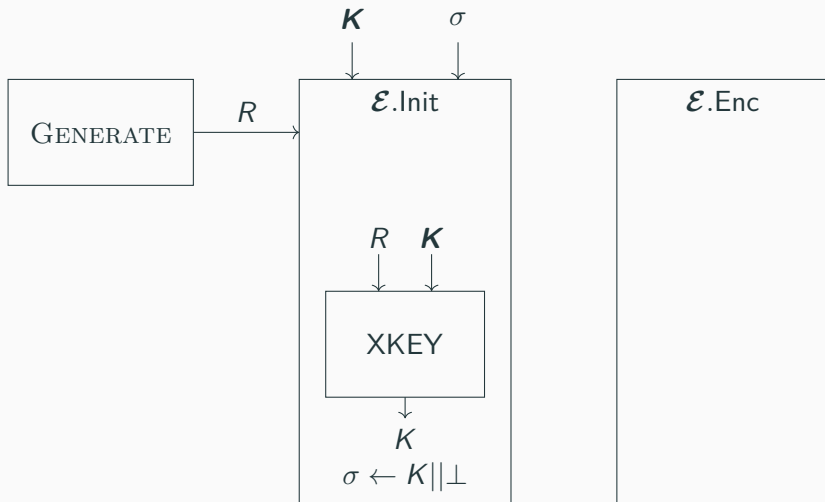


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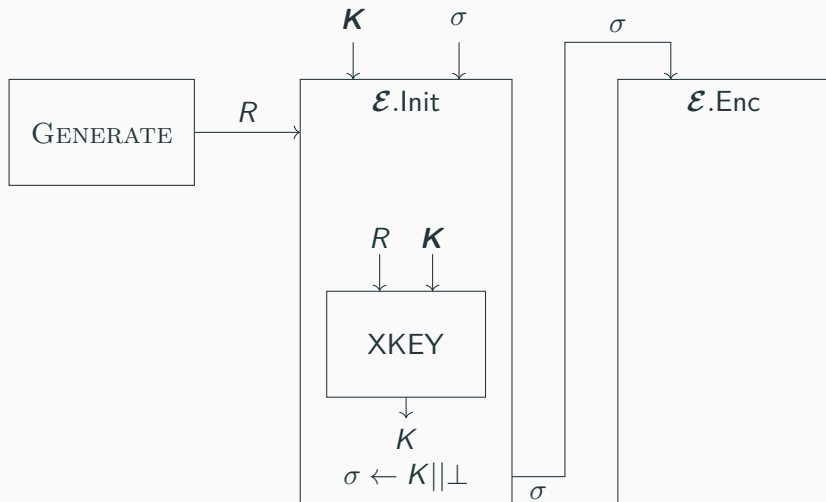
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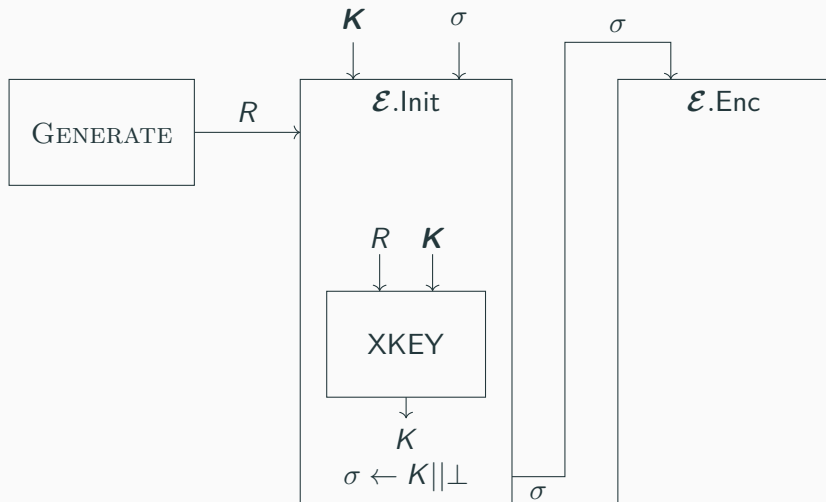
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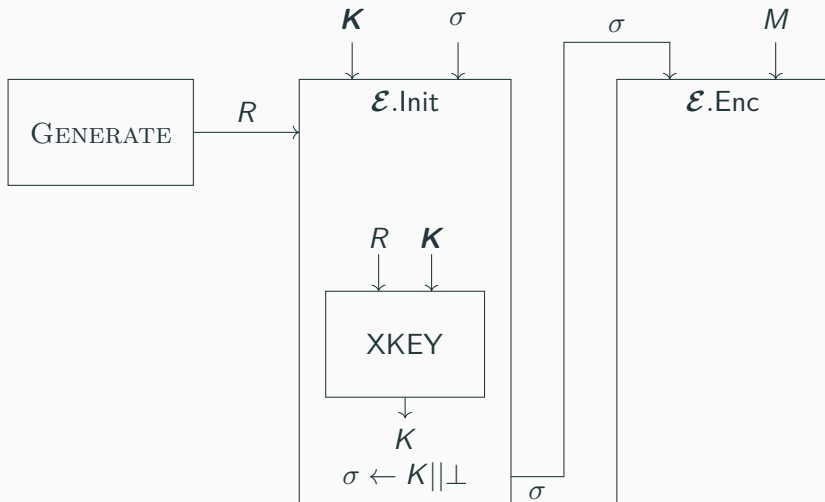
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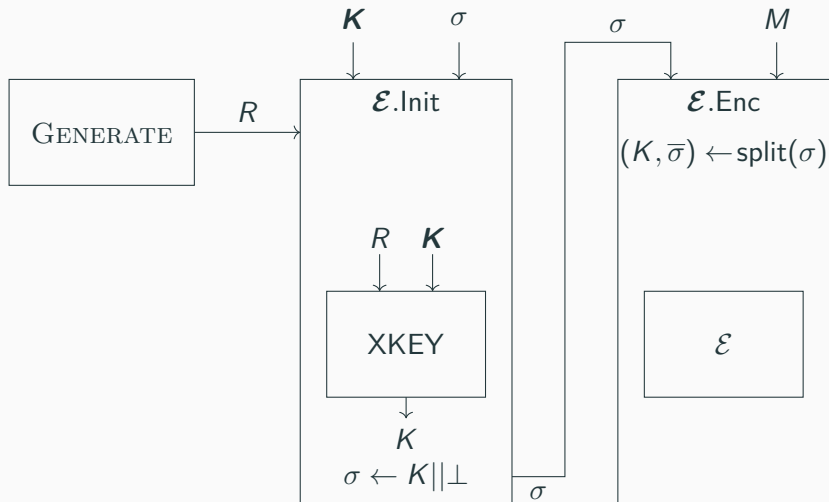
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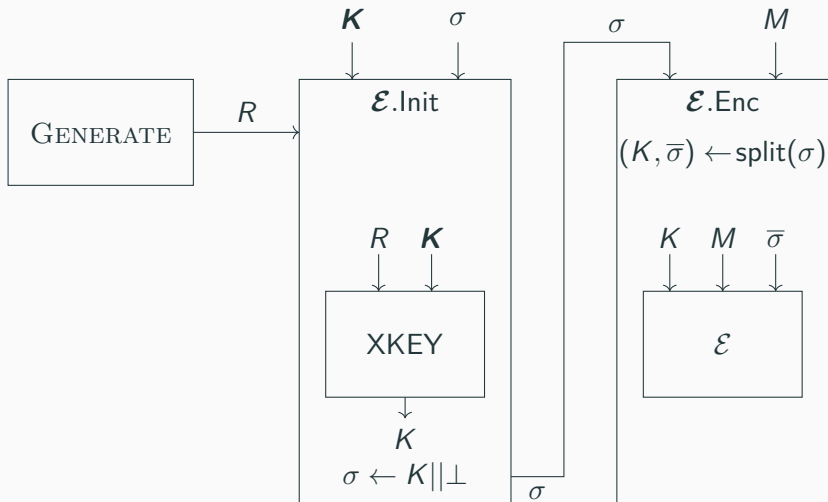
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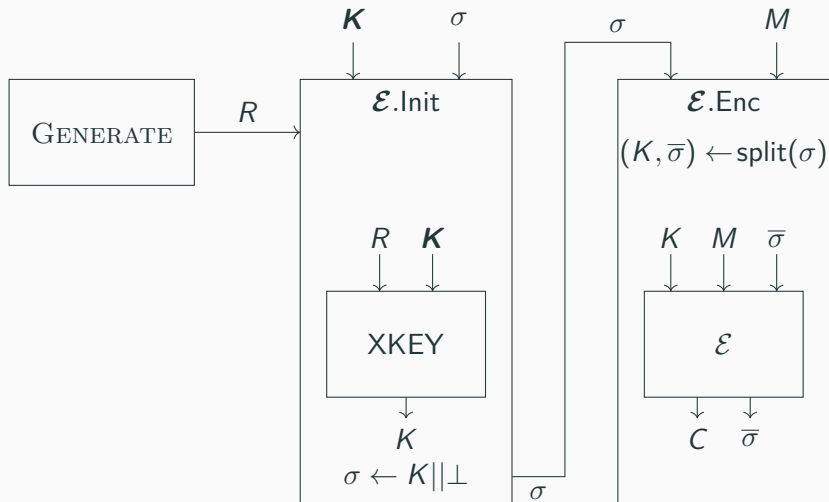
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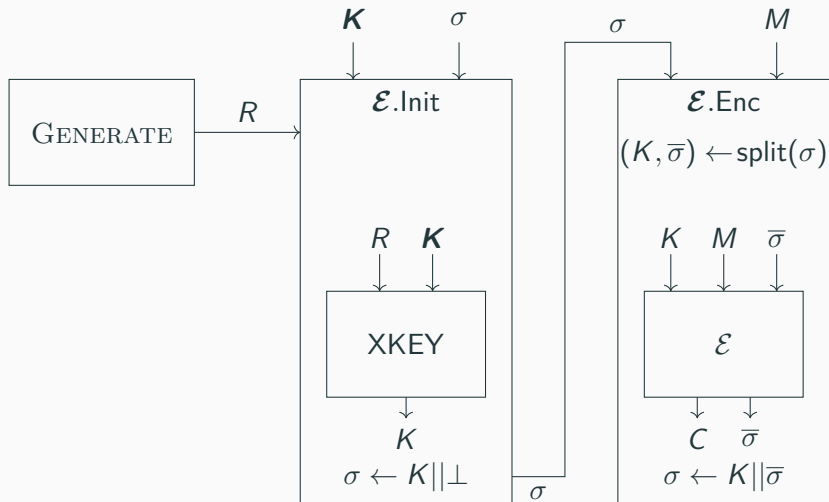
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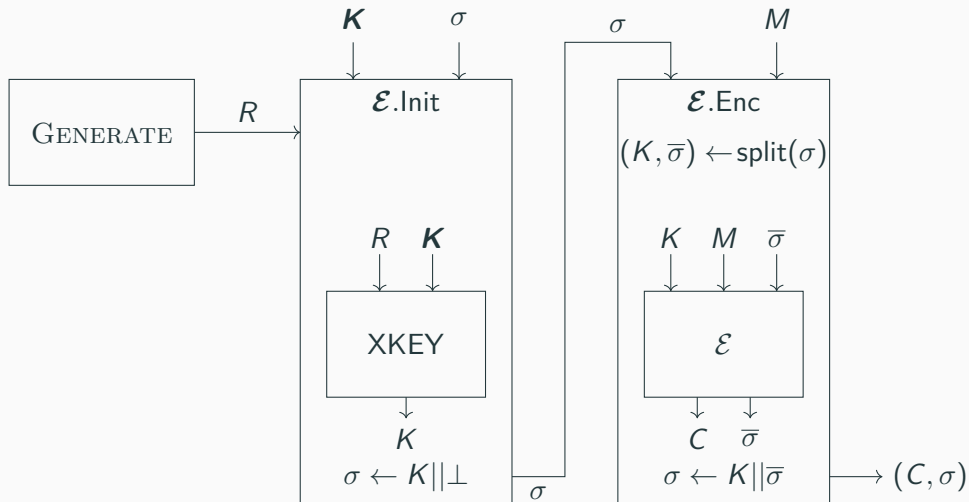


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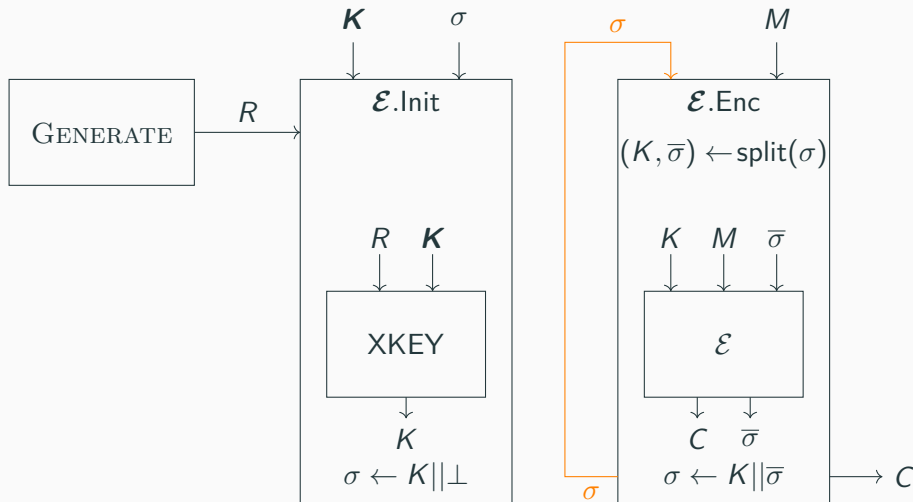
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# Big Brother is defeated

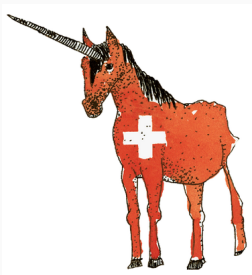
## Theorem

Let  $\Pi = (\mathcal{K}, \mathcal{E}, \mathcal{D})$  be an encryption scheme with unique ciphertexts and  $\mathcal{K} = \{0, 1\}^\kappa$ . Let  $k, P, h$  be positive integers. Let  $\mathbf{\Pi} = \text{SES}[\Pi, k, P]$  and let  $\tilde{\mathbf{\Pi}} = (\tilde{\mathcal{K}}, \tilde{\mathcal{E}}, \tilde{\mathcal{D}})$  be a subversion of  $\mathbf{\Pi}$  that meets the decryptability condition. Let  $\mathcal{B}$  be an adversary. Then

$$\mathbf{Adv}_{\mathbf{\Pi}, \tilde{\mathbf{\Pi}}, h, p, \ell}^{\text{resist}}(\mathcal{B}) \leq \Delta_1 + \Delta_2 + \Delta_3,$$

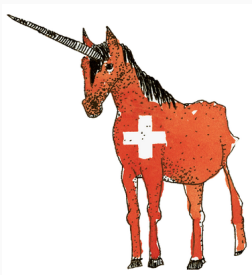
with  $\Delta_1 = 0$ ,  $\Delta_2 = 2 \cdot q_K \cdot \mathbf{Adv}_{\text{XKEY}}^{\text{ukey}}(\mathcal{A})$ ,  $\Delta_3 = 2 \cdot q_I \cdot \mathbf{Adv}_{\Pi}^{\text{ind\$}}(\mathcal{A}')$ .

# How to get secure randomness



We show how to instantiate `GENERATE` with the unicorn protocol [LW17]:

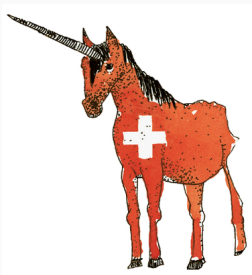
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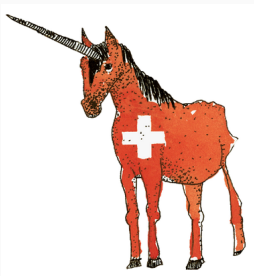
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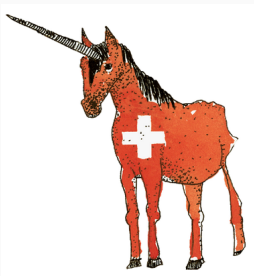


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We prove security of our construction with unicorn, by bounding  $\text{Adv}_{\text{XKEY}}^{\text{ukey}}$ .

## Conclusion and future work

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Coordinated ASAs and key exfiltration attacks break standalone symmetric encryption:  
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### **Future work:**

- more realistic leakage models;
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- faster sources of secure randomness (VDF-based or distributed random beacons);
- consider advantages of secure randomness more generally.



-  Mihir Bellare, Daniel Kane, and Phillip Rogaway.  
**Big-key symmetric encryption: Resisting key exfiltration.**  
In Matthew Robshaw and Jonathan Katz, editors, *CRYPTO 2016, Part I*, volume 9814 of *LNCS*, pages 373–402. Springer, Berlin, Heidelberg, August 2016.
-  Mihir Bellare, Kenneth G. Paterson, and Phillip Rogaway.  
**Security of symmetric encryption against mass surveillance.**  
In Juan A. Garay and Rosario Gennaro, editors, *CRYPTO 2014, Part I*, volume 8616 of *LNCS*, pages 1–19. Springer, Berlin, Heidelberg, August 2014.
-  Arjen K. Lenstra and Benjamin Wesolowski.  
**Trustworthy public randomness with sloth, unicorn, and trx.**  
*Int. J. Appl. Cryptogr.*, 3(4):330–343, 2017.