

# 2008 Bulgarian IPhO Team Selection Test

## Short Exam 1

**Problem.** A solid ball of mass  $m$  and radius  $a$  (moment of inertia  $I = \frac{2}{5}ma^2$ ) starts rolling without slipping from the top of another fixed ball of radius  $b$ . Its initial velocity is negligible. The acceleration due to gravity is  $g$ .

- (a) Find the angle  $\theta = \theta_0$  at which the rolling ball will lose contact with the fixed ball. The angle  $\theta$  is measured between the upward direction and the segment connecting the centres of the balls.
- (b) Find the velocity of the centre of mass  $v$  of the rolling ball when it detaches.
- (c) What coefficient of friction  $k$  would make the upper ball start slipping at an angle  $\theta = \alpha < \theta_0$ ?

*The problem is worth 5 points.*

*Time: 60 minutes.*

## Theoretical Exam

**Problem 1.** A satellite of mass  $m$  moves in a circular orbit of radius  $r$  around a planet of mass  $M$ . Because of a drag force of the form  $F_{\text{dr}} = Av^n$ , the orbital radius decreases at a constant rate

$$\frac{dr}{dt} = D \ll \frac{r}{T},$$

where  $T$  is the orbital period. The gravitational constant is  $\gamma$ .

- (a) Find the number  $n$ .
- (b) Determine  $D = f(\gamma, M, m, A)$ .

**Problem 2.** An incompressible fluid of viscosity  $\eta$  flows along a cylindrical pipe of length  $L$  and radius  $R$ . The pressures at the two ends of the pipe are  $p_1$  and  $p_2$ , respectively. The flow is stationary.

- (a) Find the flow velocity  $v(r)$  in terms of the distance from the axis of the pipe  $r$ .
- (b) Find the volumetric flow rate through the pipe  $Q$ .

**Problem 3.** A ball of mass  $M$  has velocity  $v_0$ . It strikes a ball of mass  $m$  ( $M > m$ ) at rest. The collision is elastic. The angle between the velocity vectors of  $M$  before and after the collision is  $\alpha$ .

- (a) Find the maximum value of  $\alpha$ .
- (b) Find the velocities  $u_M$  and  $u_m$  of the two balls after the collision in the case where maximum  $\alpha$  is realised.

### Constants:

Acceleration due to gravity	$g$	$10.0 \text{ m/s}^2$
Boltzmann constant	$k$	$1.38 \times 10^{-23} \text{ J/K}$
Elementary charge	$e$	$1.6 \times 10^{-19} \text{ C}$

*Each problem is worth 3 points.  
Time: 5 hours.*

## Experimental Exam

### Problem 1. Diode and paperclip circuit.

#### *Equipment:*

Circuit consisting of two identical diodes and a paperclip (the diodes are connected in parallel and the paperclip is in series with one of the diodes), rectifier which can supply either constant voltage or constant current, two multimeters, [resistor substitution box](#) (current not to exceed 100 mA), wires, screwdriver, graph paper.

#### *Task 1. Finding the resistance of the paperclip $R$ .*

In this part of the problem you will measure the I-V curve of the circuit (without using the substitution box) for both positive and negative (i.e. with reversed polarity) voltages.

**Note:** Do not exceed a current of 2.5 A.

- (a) Sketch the circuit that you have assembled.
- (b) Write down the ranges that you use for the multimeters.
- (c) Describe how  $R$  can be calculated from your measurements.
- (d) How will you use the rectifier – to supply a constant voltage or a to supply a constant current?

**Note:** The characteristics of the diodes have a strong dependence on temperature.

- (e) **Quickly** measure the I-V curve of the circuit as the voltage/current is raised. After you have reached the maximum voltage/current, wait until the open diode reaches its equilibrium temperature (be careful not to burn yourself on one of the diodes). Then, **quickly** measure the I-V curve of the circuit as the voltage/current is lowered. Repeat this for voltages of the opposite polarity. Present your results in a table.
- (f) Write down whether a diode is open when a positive potential is applied on the terminal with the white band, or vice versa.
- (g) Decide on the dataset that you will use for determining  $R$ . Choose between the values taken when raising the current/voltage and those taken when lowering the current/voltage.
- (h) Plot a graph from which you can find  $R$ .
- (i) Find  $R$  from the graph.
- (j) Using the graph, find your error  $\Delta R$ .

#### *Task 2. Finding the reverse-bias saturation current of the diodes $I_S$ .*

The current  $I_S$  is the maximum current through a closed diode. The I-V curve of a diode can be modelled by the Shockley diode equation,

$$I = I_S \left( e^{\frac{eU}{nkT}} - 1 \right),$$

where  $e$  is the charge of the electron,  $k$  is the Boltzmann constant,  $T$  is the absolute temperature, and  $n$  is a number close to 1.

- (a) Find an approximation of the formula above which can be used when measuring the forward I-V curve for voltages on the order of a few hundred mV at room temperature.

- (b) Apply a voltage of such polarity that the diode with no paperclip attached to it is open. Measure an appropriate part of the I-V curve for currents under 100 mA. Use the resistor substitution box if necessary. Present your results in a table.
- (c) Plot your data in appropriate variables.
- (d) Using the plot, find  $I_S$  and  $n$ .

Call the examiner if you suspect that a multimeter's fuse has blown, or in case of any other technical difficulties.

*Each problem is worth 15 points.*  
*Time: 5 hours.*