

# On Trustworthy Rule-Based Models and Explanations

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## Explainability is Not a Game

When the decisions of ML models impact people, one should expect explanations to offer the strongest guarantees of rigor. However, the most popular XAI approaches offer none.

## Fairwashing: the risk of rationalization

Ulrich Aïvodji, Hiromi Arai, Olivier Fortineau, Sébastien Gambs, Satoshi Hara, Alain Tapp

Proceedings of the 36th International Conference on Machine Learning, PMLR 97:161-170, 2019.

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Home > Philosophy & Technology > Article

## Against Interpretability: a Critical Examination of the Interpretability Problem in Machine Learning

Research Article | Open access | Published: 13 August 2019

Volume 33, pages 487–502, (2020) Cite this article

Home > Explainable AI: Interpreting, Explaining and Visualizing Deep Learning > Chapter

## The (Un)reliability of Saliency Methods

Chapter | First Online: 10 September 2019

pp 267–280 | Cite this chapter

RESEARCH ARTICLE | OPEN ACCESS



## Fooling LIME and SHAP: Adversarial Attacks on Post hoc Explanation Methods

Authors: Dylan Slack, Sophie Hilgard, Emily Jia, Sameer Singh, Himabindu Lakkaraju | Authors  
[Info & Claims](#)

AIES '20: Proceedings of the AAAI/ACM Conference on AI, Ethics, and Society • Pages 180 - 186  
<https://doi.org/10.1145/3375627.3375830>

ARTICLE



## An empirical evaluation of the comprehensibility of decision table, tree and rule based predictive models

Authors: Johan Huysmans, Karel Dejaeger, Christophe Mues, Jan Vanthienen, Bart Baesens | Authors Info & Claims

Decision Support Systems, Volume 51, Issue 1 • Pages 141 - 154 • <https://doi.org/10.1016/j.dss.2010.12.003>

# Two Facets of Trust in Rule-based Models and Explanations

# SCIENTIFIC REPORTS



OPEN

## MediBoost: a Patient Stratification Tool for Interpretable Decision Making in the Era of Precision Medicine

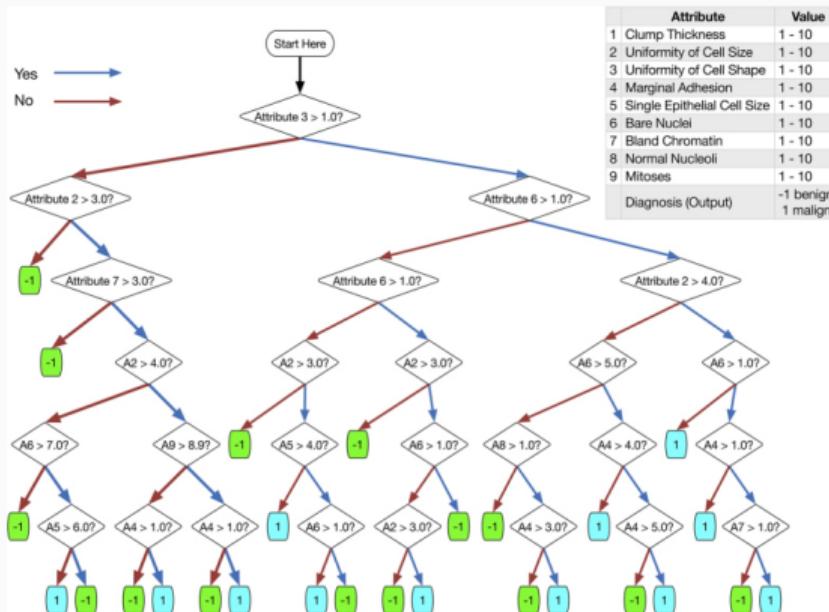
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Gilmer Valdes<sup>1,2</sup>, José Marcio Luna<sup>1</sup>, Eric Eaton<sup>3</sup>, Charles B. Simone II<sup>2</sup>, Lyle H. Ungar<sup>3</sup> & Timothy D. Solberg<sup>1,2</sup>

# Redundancy

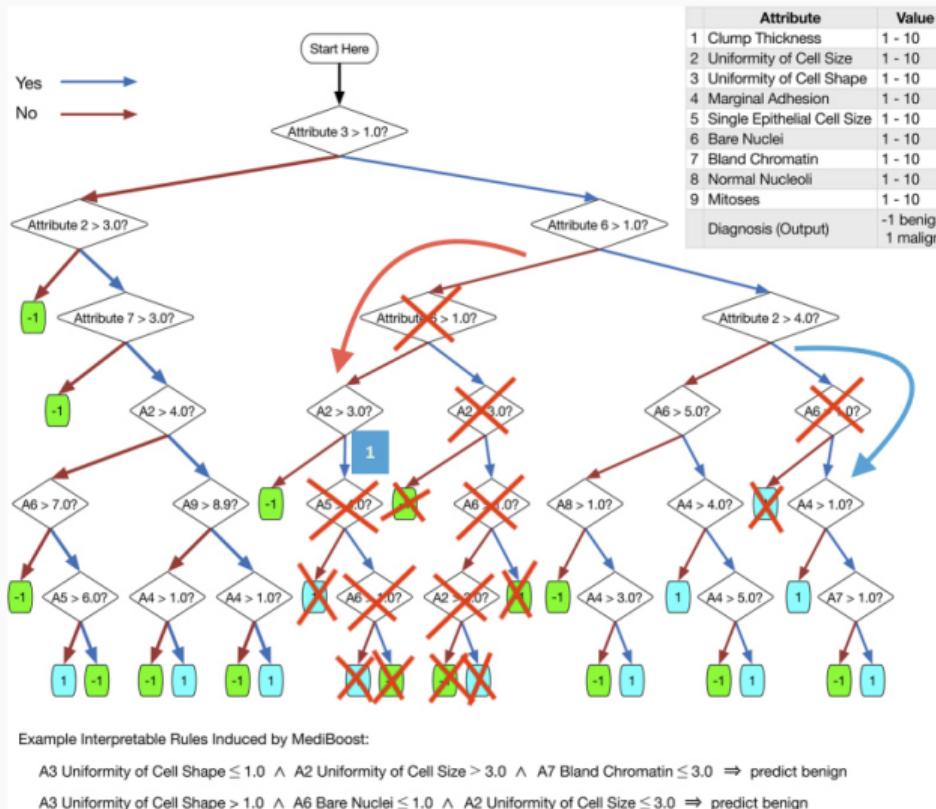


Example Interpretable Rules Induced by MediBoost:

A3 Uniformity of Cell Shape  $\leq 1.0$   $\wedge$  A2 Uniformity of Cell Size  $> 3.0$   $\wedge$  A7 Bland Chromatin  $\leq 3.0 \Rightarrow$  predict benign

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- **Illustrative examples of Anchor explanations**, produced by a neural network trained on the Adult dataset:
  - $\text{Age} \leq 28 \wedge \text{Occupation} = \text{Other} \wedge \text{CapitalGain} = 0 \wedge \text{CapitalLoss} = 0 \wedge \text{Workclass} = \text{Private} \implies 0$
  - $\text{MaritalStatus} = \text{Married-civ-spouse} \wedge \text{Education} = \text{Masters} \implies 1$

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- In such cases, the resulting explanations may lack reliability and cannot be considered fully trustworthy.

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- Can we identify and characterize negative overlaps between rules or explanations in the feature space, subject to background constraints?
- How can these ideas be effectively implemented in practice?
- Do well-known tools suffer from redundancy and overlap, and to what extent?

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- There are very efficient tools that can be used to check if  $F_1 \models F_2$ . They are called SAT (Boolean Satisfiability Solvers).

# Background

## Rule-Based Models

- We consider models that can be represented as a set of (unordered) rules together with background constraints  $\mathcal{B}$
- Examples include decision trees, decision diagrams, random forests, boosted trees, decision sets, among others
- We use  $\mathcal{M}$  to denote a model
- A literal is a unary relation on a feature. For instance  $(\text{size} > 20)$  is a literal.
- A rule  $R$  is denoted by  $L \implies o$ , where  $L$  is a conjunction of literals and  $o$  is a prediction outcome

## Example

### Background constraints $\mathcal{B}$

- $(\text{salary} > 0) \leftrightarrow (\text{age} \geq 18)$
- $(\text{size} = 140) \rightarrow (\text{size} > 120)$
- $(\text{weight} > 90) \rightarrow (\text{weight} \geq 85)$
- $(\text{weight} \geq 85) \rightarrow (\text{weight} > 80)$

### The Model

- $R_1 = (\text{salary} > 0) \wedge (\text{size} \neq 140) \wedge (\text{age} > 10) \wedge (\text{color} = \text{blue}) \wedge (\text{weight} > 80) \implies 1$
- $R_2 = (\text{salary} > 0) \wedge (\text{size} = 140) \implies 1$
- $R_3 = (\text{salary} > 0) \wedge (\text{weight} > 90) \implies 1$
- $R_4 = (\text{size} > 120) \wedge (\text{weight} < 85) \implies 0$

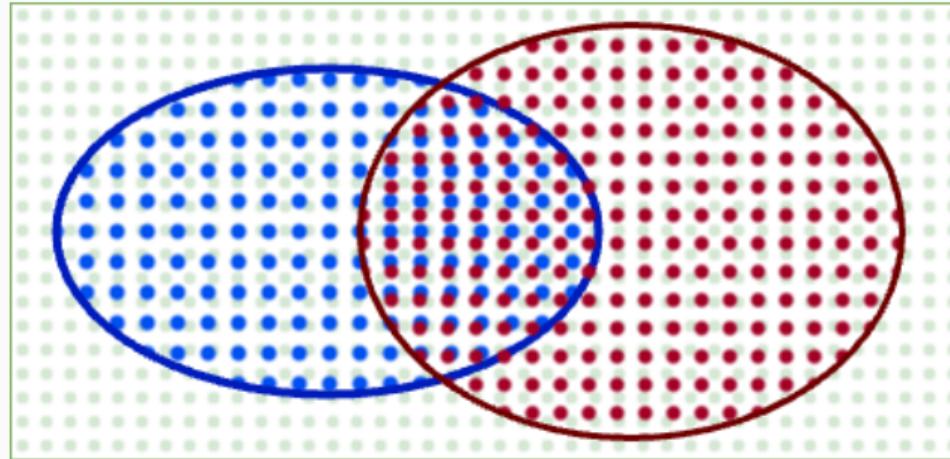
# Theoretical Contributions On Overlap and Redundancy

## Overlap

- Given two rules  $R_1$  and  $R_2$ , do  $R_1$  and  $R_2$  overlap?
- Can we find all negative overlaps?

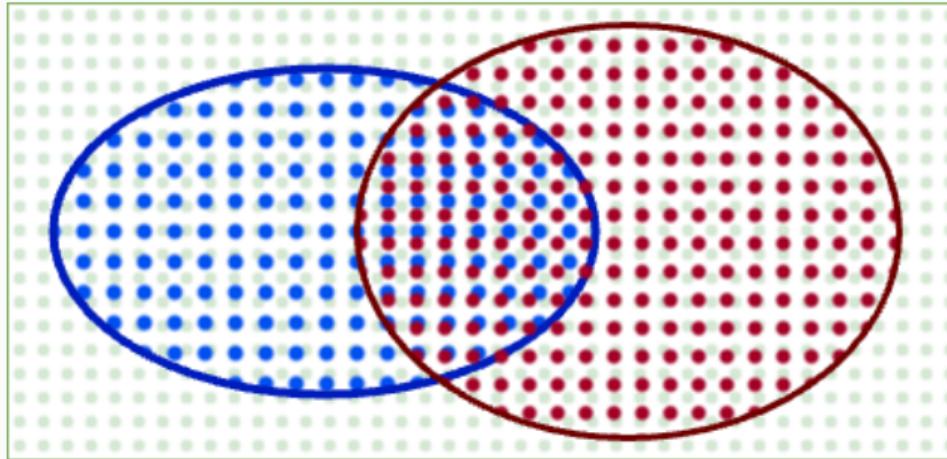
## Overlap

**Figure 1:** Illustration of overlap between two rules  $R_1$  and  $R_2$ . Points are inputs in feature space that satisfy  $\mathcal{B}$ . Blue: fire  $R_1$ ; Red: fire  $R_2$ .



# Overlap

**Figure 1:** Illustration of overlap between two rules  $R_1$  and  $R_2$ . Points are inputs in feature space that satisfy  $\mathcal{B}$ . Blue: fire  $R_1$ ; Red: fire  $R_2$ .



## Lemma (Overlap Check)

Two rules  $R_1$  and  $R_2$  overlap iff  $\mathcal{B} \wedge L_1 \wedge L_2$  is satisfiable.

# Redundancy

- Rule redundancy
- Literal redundancy
  - Local redundancy
  - Global redundancy

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## Notations

- $\Delta(o)$ : set of rules with outcome  $o$
- Suppose that  $\Delta(o) = \{R_1, \dots, R_z\} \cup \{R\}$
- Denote by  $Rest = L_1 \vee \dots \vee L_z$

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## Proposition (Rule Redundancy Check)

A rule  $R$  is redundant in  $\mathcal{M}$  iff  $\mathcal{B} \wedge L \models Rest$

# Literal Redundancy

## Notation

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## Definition (Literal Redundancy)

A literal  $l$  is redundant in  $L$  iff  $l \in L$  and  $\mathcal{M}_l$  is equivalent to  $\mathcal{M}$ .

## Example

- $R_1 = (\text{salary} > 0) \wedge (\text{size} \neq 140) \wedge (\text{age} > 10) \wedge (\text{color} = \text{blue}) \wedge (\text{weight} > 80) \implies 1$
- $(\text{age} > 10)$  is locally redundant in  $R_1$ .

# Local Redundancy

## Example

- $R_1 = (\text{salary} > 0) \wedge (\text{size} \neq 140) \wedge (\text{age} > 10) \wedge (\text{color} = \text{blue}) \wedge (\text{weight} > 80) \implies 1$
- $(\text{age} > 10)$  is locally redundant in  $R_1$ .

## Lemma (Local Redundancy)

If  $I \in L$  and  $\mathcal{B} \wedge L \setminus \{I\} \models I$  then  $I$  is redundant in  $L$ .

## Global Redundancy: Example

- $R_1 = (\text{salary} > 0) \wedge (\text{size} \neq 140) \wedge (\text{age} > 10) \wedge (\text{color} = \text{blue}) \wedge (\text{weight} > 80) \implies 1$
- $R_2 = (\text{salary} > 0) \wedge (\text{size} = 140) \implies 1$
- ...

$(\text{size} \neq 140)$  is globally redundant in  $R_1$ :

- $\text{Flip}_{(\text{size} \neq 140)} = (\text{salary} > 0) \wedge (\text{size} = 140) \wedge (\text{age} > 10) \wedge (\text{color} = \text{blue}) \wedge (\text{weight} > 80)$
- $\mathcal{B} \wedge \text{Flip}_{(\text{size} \neq 140)} \models (\text{salary} > 0) \wedge (\text{size} = 140)$

# Global Redundancy

## Notation

- $\text{Flip}_I = L \cup \{\neg I\} \setminus \{I\}$

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- $\text{Flip}_I = L \cup \{\neg I\} \setminus \{I\}$

## Lemma (Global Redundancy)

*If  $I$  is not locally redundant in  $L$  and  $\mathcal{B} \wedge \text{Flip}_I \models \text{Rest}$ , then  $I$  is redundant in  $L$*

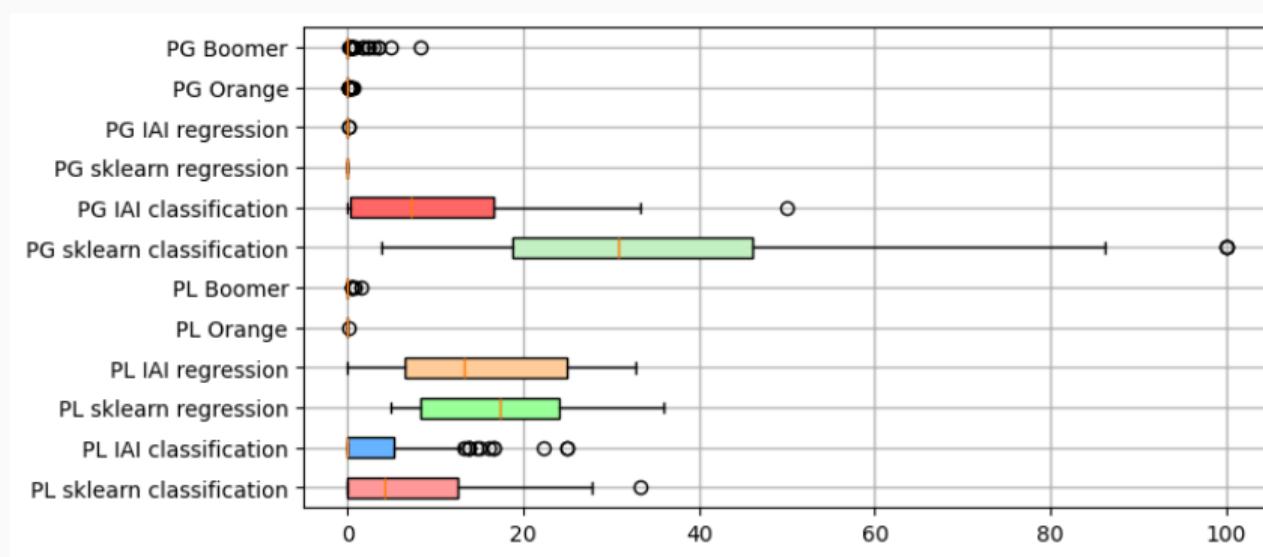
## Experimental Results: Redundancy

## Experimental Setting

- Scikit-learn and Interpretable AI for learning classification and regression decision trees
- Boomer to learn ensembles of boosted rules
- Orange v3 to learn decision sets for classification
- Diverse datasets from UCI ML repository with diverse characteristics
- Background constraints  $\mathcal{B}$  that enforce domain coherence between the features.
- SAT calls with PySAT
- One-hour time limit.
- All experiments ran on Apple M1 Pro (32 GB)

## Frequency of Redundancies

**Figure 2:** Frequency of Literal Redundancy. PL (respectively PG) is the percentage of locally (respectively globally) redundant literals



## Experimental Results: Overlaps

# Overlapping Anchor Explanations

Learner	Dataset	Train	Test	# Explanations	# Overlap
xgboost randomforest logistic nn	recidivism	92.39	74.33	333	87
	recidivism	93.52	75.46	321	65
	recidivism	62.59	60.00	196	735
	recidivism	87.47	71.49	341	150
xgboost randomforest logistic nn	lending	90.10	82.89	260	384
	lending	91.25	83.60	278	207
	lending	82.56	83.51	50	54
	lending	88.00	82.54	159	66
xgboost randomforest logistic nn	adult	90.35	84.26	565	3195
	adult	93.52	85.60	558	2534
	adult	83.00	82.98	378	2788
	adult	92.47	83.62	597	3212

# Conclusions

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## Contributions

1. Introduce a new approach to identifying and removing redundant information in rule based models under background constraints
2. Establish a dichotomy in the nature of redundancy
3. Propose novel algorithms for mining overlapping rules and explanations
4. Provide empirical insights:
  - Redundancy is widespread in commonly used tools
  - Overlapping rules occur frequently
  - Anchor explanations often lack trustworthiness

## What I didn't have time to cover

- How to generate the background constraints
- The impact of the background constraints
- The computational overhead
- The quality of Overlap
- The correlation between redundancy and prediction quality
- The relationship with formal explainability (abductive explanations)

# Conclusions

## Future Research

- Develop stronger benchmarks for background (user-defined) constraints. If you know examples, please share with us!
- Incorporate distance metrics into regression tasks
- Why do Boomer and tree ensembles leverage overlap more effectively than Orange?