Trustworthy Machine Learning Through the Lens of Combinatorial Optimisation and Operations Research

Keywords: Fairness, Interpretability, Explainability, Privacy

Context

- Machine learning now permeates daily life and high-stakes decisions, making **trustworthiness** more critical than ever.
- Trust spans multiple dimensions: **philosophy**, **bias mitigation**, and **technical safety**.
- Advances in **combinatorial optimisation** and **operations research** open new paths to address trust-related challenges.

Figure 1: Four Facets of Trust Explored in This Work

Contributions

- Fair rule lists using backtracking search and mixed integer linear programming [1, 2]
- Optimal decision trees and diagrams using boolean satisfiability, backtracking search, and dynamic programming [3, 4]
- Dataset reconstruction from interpretable models [5]
- Trustworthy explanations using Boolean satisfiability [6]
- Generalising statistical fairness to unseen data using sample-robust optimisation [1]
- Sensitive attribute reconstruction using constraint programming [7]

Example of Interpretable Models

- A *rule list* model provides interpretable predictions by applying an ordered sequence of if–then rules to the input data.
- *Default of Credit Card* dataset: each individual is represented by demographic information, credit data, and payment history. The goal is to predict whether a person will default on their credit card payment.

1. If `Delay` $= 2$ months and `Age` > 60, then **predict Default**.
2. Else if `Education` $=$ University and `Sex` $=$ Male, then **predict No Default**.
3. Else if `Marriage` $=$ Single and `Sex` $=$ Female, then **predict Default**.
4. Else **predict No Default**.

Figure 4: Example of a rule list for the *Default of Credit Card* dataset.

Example: Learning Fair Rule Lists

- There exist multiple fairness measures. For a statistical measure $\mathcal{M}$, we aim to ensure that for two protected groups $\mathcal{A}, \mathcal{B}$ (e.g., male and female),

$$|\mathcal{M}(\mathcal{A}) - \mathcal{M}(\mathcal{B})| < \epsilon.$$

- Let X be the training data and Y their true labels. For a given fairness measure $\mathcal{M}$, the fair rule list problem seeks a rule list that minimises prediction error subject to fairness constraints. Let $\mathcal{R}$ be the set of all possible rules:

$$r^* = \arg\min_{r \in \mathcal{R}} \texttt{error}(r, X, Y)$$
$$\text{s.t.} \quad \texttt{fairness}(r, X, Y) \leq \epsilon.$$

- We solve this problem using a backtracking search. At each node, an integer linear program (ILP) ensures that the joint misclassification–fairness constraint remains feasible.

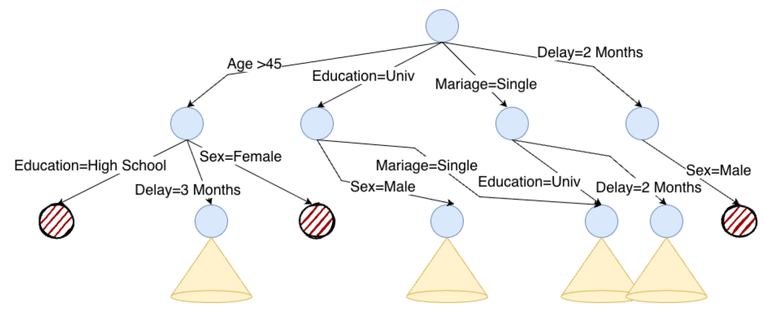

Figure 2: Pruning the search space with ILP. Each node represents a set of candidate models; dashed nodes are pruned by the ILP model.

- We also address the challenging problem of *generalising fairness*, using mixed-integer programming within a sample-robust optimisation framework to guarantee fairness under uncertainty.
- `FairCORELS` is a **multi-objective tool** designed to learn fair rule lists.

Figure 3: Example trade-offs produced by `FairCORELS` for the Statistical Parity fairness metric on the *Default of Credit Card* dataset.

References

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