

- 7 A submarine uses cables to recover a submerged wooden chest as shown in Fig. 7.1.

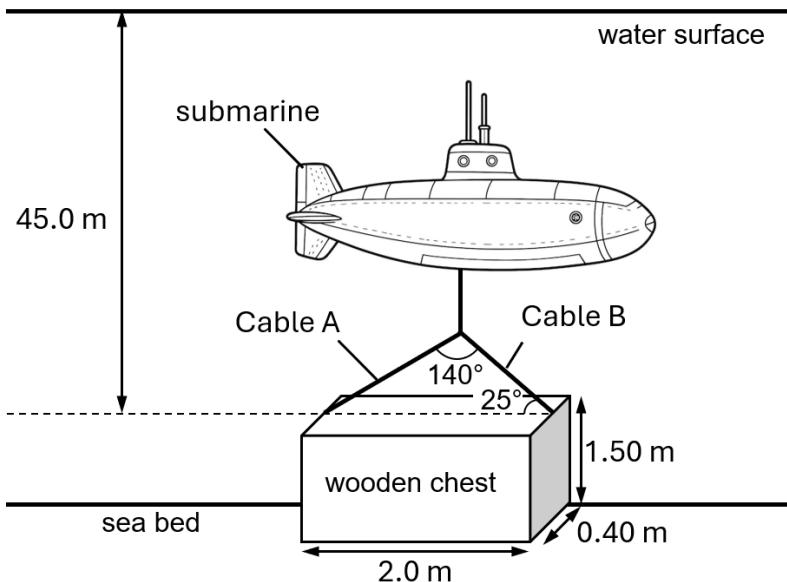


Fig. 7.1 (not to scale)

The submarine has a mass of 3600 kg. The density of seawater is 1030 kg m^{-3} and the average density of the chest is 1800 kg m^{-3} .

- (a) Show that the hydrostatic pressure p of a fluid at a depth h and density ρ is given by the expression

$$p = \rho gh.$$

[2]

(b) The box is held in equilibrium slightly above the sea bed.

(i) Explain why the seawater exerts an upthrust on the chest.

.....
.....
.....

[2]

(ii) Calculate the upthrust of the wooden chest when it is raised above the sea bed.

$$\text{upthrust} = \dots\dots\dots\dots\dots N [2]$$

(iii) Calculate the weight of the wooden chest.

$$\text{weight} = \dots\dots\dots\dots\dots N [1]$$

(iv) Determine the tension in cable A and cable B.

$$\text{tension in cable A} = \dots\dots\dots\dots\dots N$$

$$\text{tension in cable B} = \dots\dots\dots\dots\dots N$$

[4]

[Turn over

- (c) The submarine is propelled forward at a constant velocity of 4.5 m s^{-1} by a 0.50 MW motor connected to a propeller. The drag force F_d acting on the submarine and the chest is given by

$$F_d = kv^2,$$

where $k = 3.5 \times 10^3 \text{ N s}^2 \text{ m}^{-2}$.

- (i) Calculate the thrust provided by the propeller.

thrust = N [2]

- (ii) Calculate the efficiency of the motor when the submarine is cruising at a speed of 4.5 m s^{-1} .

efficiency = % [2]

- (d) The total mass of the submarine is suddenly decreased by 200 kg by pumping water out of the submarine horizontally in a negligible time. The volume of the submarine remains unchanged.

- (i) Calculate the initial upward acceleration of the submarine.

acceleration = m s^{-2} [3]

- (ii) Explain why the acceleration of the submarine eventually decreases to zero as the submarine ascends.

[2]