

- 1 The Poiseuille equation relating the volume flow rate  $\frac{V}{t}$  of a fluid under laminar conditions through a horizontal tube of length  $L$  and internal radius  $r$  is

$$\frac{V}{t} = \frac{\pi p r^4}{8\eta L}$$

where  $p$  is the pressure difference between the two ends of the tube and  $\eta$  is the viscosity of the fluid.

- (a) Show that the SI base units for  $\eta$  is  $\text{kg m}^{-1} \text{s}^{-1}$ .

[2]

- (b) In an experiment to determine  $\eta$  for water, a student recorded the following measurements in SI units, as shown in Table 1.1.

**Table 1.1**

quantity	magnitude in SI units	percentage uncertainty / %
$\frac{V}{t}$	$1.0 \times 10^{-6}$	3
$p$	500	2
$L$	0.20	0.5

The internal diameter of the tube was measured and recorded as  $(0.200 \pm 0.002)$  cm.

- (i) Calculate the percentage uncertainty in the internal radius  $r$  of the tube.

percentage uncertainty = ..... % [1]

- (ii) Using the results in Table 1.1 and (b)(i), determine  $\eta$  with its associated uncertainty. Give your answer to an appropriate number of significant figures.

$$\eta = \dots \pm \dots \text{ kg m}^{-1} \text{ s}^{-1} [4]$$

- (iii) State and explain which measured quantity has the greatest contribution to the uncertainty of  $\eta$ .

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[1]

[Total: 8]

