

## Question 5: Photoelectric Effect and Atomic Physics

### (a) Linear Momentum of Photoelectrons

Maximum kinetic energy is  $K_{\max} = eV_s = (1.60 \times 10^{-19})(4.25) = 6.80 \times 10^{-19}$  J. The momentum is  $p = \sqrt{2m_e K_{\max}}$ .

$$p = \sqrt{2(9.11 \times 10^{-31})(6.80 \times 10^{-19})} \approx 1.114 \times 10^{-24} \text{ Ns}$$

### (b) Ratio of Emitted Electrons to Incident Photons ( $N_e/N_p$ )

Rate of photoelectron emission:

$$N_e = \frac{I_{\text{sat}}}{e} = \frac{21.7 \times 10^{-9}}{1.60 \times 10^{-19}} = 1.356 \times 10^{11} \text{ electrons/s}$$

Rate of photon incidence:

$$N_p = \frac{P_{\text{in}}}{E_p} = \frac{I \times A}{hc/\lambda} = \frac{(0.7)(10 \times 10^{-4})}{(6.63 \times 10^{-34})(3.00 \times 10^8)/(60 \times 10^{-9})} = 2.112 \times 10^{14} \text{ photons/s}$$

The ratio is:

$$\frac{N_e}{N_p} = \frac{1.356 \times 10^{11}}{2.112 \times 10^{14}} \approx 6.42 \times 10^{-4}$$

### (c) Collision with Hydrogen Atom

The electron's kinetic energy is  $K_{\max} = 4.25$  eV. The minimum energy to excite a hydrogen atom from its ground state ( $n = 1$ ) to the first excited state ( $n = 2$ ) is:

$$\Delta E = E_2 - E_1 = \left(-\frac{13.6}{2^2}\right) - \left(-\frac{13.6}{1^2}\right) = 10.2 \text{ eV}$$

Since the electron's energy (4.25 eV) is less than the required excitation energy (10.2 eV), the electron cannot excite the hydrogen atom. Therefore, no photons will be emitted.