#### CA4012

# DCU

#### Statistical Machine Translation

# Week 7: Phrase-based Translation n Model

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- What's the main deficiency of IBM Model 1?
- In terms of IBM Model 1, assuming the length of a so urce-side sentence is  $l_f$ , the length of a target-side sent ence is  $l_e$ , how many possible alignments between the m (ignoring the NULL word at the source side)?
- What's the main differences between higher IBM Mo dels and IBM Model 1?



- What's the main deficiency of IBM Model 1?
- It is weak at the reordering, because it regards all possible reorderings as equally likely.



- In terms of IBM Model 1, assuming the length of a so urce-side sentence is  $l_p$ , the length of a target-side sent ence is  $l_e$ , how many possible alignments between the m (ignoring the NULL word at the source side)?
- $(l_f)^{le}$



- What are the main differences between higher IBM Models and IBM Model 1?
  - IBM Model 1: lexical translation;
  - IBM Model 2: adds absolute alignment model;
  - IBM Model 3: adds fertility model;
  - IBM Model 4: adds relative alignment model;
  - IBM Model 5: fixes deficiency.

#### Exercise in Class

Given the following Chinese-English pairs:

S1	S2
yuan	hen yuan
far	far away

The source side is Chinese, and the target side is English. In this question, the *NULL* token is ignored.

#### Q1:

Assuming only one-to-one alignment is allowed, please list all the possible word alignments for the two sentence pairs.

### Exercise in Class

Given the following Chinese-English pairs:

S1	S2
yuan	hen yuan
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The source side is Chinese, and the target side is English. In this question, the *NULL* token is ignored.

#### Q1:

Assuming only one-to-one alignment is allowed, please list all the possible word alignments for the two sentence pairs.

a1: yuan – fara2: hen – far, yuan – awaya3: hen – away, yuan – far

#### Q2:

Considering all word alignments as above, state what the following translation probabilities will be after **two** iterations of the **Expectation Maximisation** algorithm and **show all the steps** followed to arrive at these values:

```
t(far|yuan)

t(way|yuan)

t(far|hen)

t(away|hen)
```



## Solution 1: Normal IBM 1

- Step 0: Initialisation
- Step 1: Expectation Alignment probability
  - Translation probability under the alignment:

Alignment probability for each alignment



### Solution 1: Normal IBM 1

- Step 0: Initialisation
- Step 1: Expectation Alignment probability
  - Translation probability under the alignment:

$$p(e, a|f) = \frac{\varepsilon}{(l_f + 1)^{l_e}} \prod_{j=1}^{l_e} t(e_j | f_{a(j)})$$

Alignment probability for each alignment

$$p(a|\mathbf{e},\mathbf{f}) = \frac{p(\mathbf{e},a|\mathbf{f})}{p(\mathbf{e}|\mathbf{f})} = \frac{p(\mathbf{e},a|\mathbf{f})}{\sum_{a} p(\mathbf{e},a|\mathbf{f})}$$



## Step 2: Maximisation

– Collecting fractional counts:

Estimate new lexical translation probability:

Iterate until convergence



# Step 2: Maximisation

– Collecting factional counts:

$$c(e|f; \boldsymbol{e}, \boldsymbol{f}) = \sum_{a} p(a|\boldsymbol{e}, \boldsymbol{f}) \sum_{j=1}^{l_e} \delta(e, e_j) \delta(f, f_{a(j)})$$

– Estimate new lexical translation probability:

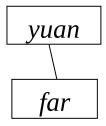
$$t(e|f; \boldsymbol{e}, \boldsymbol{f}) = \frac{\sum_{(\boldsymbol{e}, \boldsymbol{f})} c(e|f; \boldsymbol{e}, \boldsymbol{f})}{\sum_{e} \sum_{(\boldsymbol{e}, \boldsymbol{f})} c(e|f; \boldsymbol{e}, \boldsymbol{f})}$$

Iterate until convergence

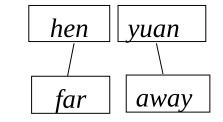




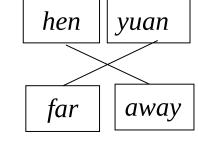




a2:



a3:



## Q2



#### Initialisation:

- Input words W1={hen, yuan}
- Output words W2={far, away}
- -t(far|yuan) = 1/2
- -t(away|yuan) = 1/2
- -t(far|hen) = 1/2
- -t(away|hen) = 1/2

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- Step 1 Expectation:
  - Compute the translation probability under each p ossible alignment:
    - p(e, a1|f) = t(far|yuan) = 1/2
    - p(e, a2|f) = t(far|hen)\*t(away|yuan) = 1/2 \* (1/2) = 1/4
    - p(e, a3|f) = t(away|hen)\*t(far|yuan) = 1/2 \* (1/2) = 1/4



- Step 1 Expectation:
  - Normalize the alignment probability:
    - p(a1|e,f) = (1/2)/(1/2) = 1
    - p(a2|e,f) = (1/4)/(1/4\*2) = 1/2
    - p(a3|e,f) = (1/4)/(1/4\*2) = 1/2



- Step 2 Maximisation:
  - Collect counts
    - c(far|yuan) = 1\*1+1/2\*1 = 3/2
    - c(away|yuan) = 1/2 \*1 = 1/2
    - c(far|hen) = 1/2\*1= 1/2
    - c(away|hen) = 1/2\*1= 1/2



- Step 2 Maximisation:
  - Normalize and estimate model parameters
    - t(far|yuan) = 3/2/(3/2+1/2) = 3/4
    - t(away|yuan) = 1/2/(3/2+1/2) = 1/4
    - t(far|hen) = 1/2/(1/2+1/2) = 1/2
    - t(away|hen) = 1/2/(1/2+1/2) = 1/2



- Step 1 Expectation:
  - Compute the translation probability under one ali gnment:
    - p(e, a1|f) = t(far|yuan) = 3/4
    - p(e, a2|f) = t(far|hen)\*t(away|yuan) = 1/2 \* (1/4) = 1/8
    - p(e, a3|f) = t(away|hen)\*t(far|yuan) = 1/2 \* (3/4) = 3/8



- Step 1 Expectation:
  - Compute the translation probability under one ali gnment:
    - p(e, a1|f) = t(far|yuan) = 3/4
    - p(e, a2|f) = t(far|hen)\*t(away|yuan) = 1/2 \* (1/4) = 1/8
    - p(e, a3|f) = t(away|hen)\*t(far|yuan) = 1/2 \* (3/4) = 3/8



- Step 1 Expectation:
  - Normalize the alignment probability:
    - p(a11|e,f) = (3/4)/(3/4) = 1
    - p(a22|e,f) = (1/8)/(4/8) = 1/4
    - p(a23|e,f) = (3/8)/(4/8) = 3/4



- Step 2 Maximisation:
  - Collect counts
    - c(far|yuan) = 1\*1+3/4\*1 = 7/4
    - c(away|yuan) = 1/4\*1 = 1/4
    - c(far|hen) = 1/4\*1+ = 1/4
    - c(away|hen) = 3/4\*1=3/4



- Step 2 Maximisation:
  - Normalize and estimate model parameters
    - t(far|yuan) = 7/4/(7/4+1/4)=7/8
    - t(away|yuan) = 1/4/(8/4)=1/8
    - t(far|hen) = 1/4/(1/4+3/4)=1/4
    - t(away|hen) = 3/4/(1/4+3/4)=3/4



### Results after two Iterations

- t(far|yuan) = 7/4/(7/4+1/4)=7/8
- t(away|yuan) = 1/4/(8/4)=1/8
- t(far|hen) = 1/4/(1/4+3/4)=1/4
- t(away|hen) = 3/4/(1/4+3/4)=3/4



# Solution 2: Simplified IBM 1

Step 1: Initialize model parameters p(e|f)

Step 2: Collect counts for word pair (*e*, *f*)

Step 3: Estimate new model parameters

Iterate untill convergence.



# Solution 2: Simplified IBM 1

Step 1: Initialize model parameters p(e|f)

Step 2: Collect counts for word pair (e, f)

$$c(e|f; \boldsymbol{e}, \boldsymbol{f}) = \frac{t(e|f)}{\sum_{i=0}^{l_f} t(e|f_i)} \sum_{j=1}^{l_e} \delta(e, e_j) \sum_{i=0}^{l_f} \delta(f, f_i)$$

Step 3: Estimate new model parameters

$$t(e|f; \boldsymbol{e}, \boldsymbol{f}) = \frac{\sum_{(\boldsymbol{e}, \boldsymbol{f})} c(e|f; \boldsymbol{e}, \boldsymbol{f})}{\sum_{e} \sum_{(\boldsymbol{e}, \boldsymbol{f})} c(e|f; \boldsymbol{e}, \boldsymbol{f})}$$

Iterate untill convergence.

## Q2



- Initialisation:
  - Input words W1={hen, yuan}
  - Output words W2={far, away}
    - t(far|yuan) = 1/2
    - t(away|yuan) = 1/2
    - t(far|hen) = 1/2
    - t(away|hen) = 1/2



- Collect counts for word pairs sentence by sentence
  - S1: yuan far
    - c(far|yuan) =  $\frac{1/2}{1/2} * 1 = 1$
  - S2: hen yuan far away
    - c(far|yuan) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} * 1 = \frac{1}{2}$
    - c(away|yuan) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} * 1 = \frac{1}{2}$
    - c(far|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} * 1 = \frac{1}{2}$
    - c(away|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} * 1 = \frac{1}{2}$



- Using Simplified IBM Model 1 to estimate new word translation probabilities
  - t(far|yuan) =  $\frac{1+1/2}{\frac{1}{2}+\frac{1}{2}+1} = \frac{3}{4}$
  - t(away|yuan) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2} + 1} = \frac{1}{4}$
  - t(far|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} = \frac{1}{2}$
  - t(away|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{2}} = \frac{1}{2}$



- Collect counts for word pairs sentence by sentence
  - S1: yuan far
    - c(far|yuan) =  $\frac{3/4}{3/4} * 1 = 1$
  - S2: hen yuan far away
    - c(far|yuan) =  $\frac{3/4}{\frac{3}{4} + \frac{1}{2}} * 1 = \frac{3}{5}$
    - c(away|yuan) =  $\frac{1/4}{\frac{1}{4} + \frac{1}{2}} * 1 = \frac{1}{3}$
    - c(far|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{3}{4}} * 1 = \frac{2}{5}$
    - c(away|hen) =  $\frac{1/2}{\frac{1}{2} + \frac{1}{4}} * 1 = \frac{2}{3}$



- Using Simplified IBM Model 1 to estimate new word translation probabilities
  - t(far|yuan) =  $\frac{1+3/5}{\frac{3}{5}+\frac{1}{3}+1} = \frac{24}{29}$
  - t(away|yuan) =  $\frac{1/3}{\frac{3}{5} + \frac{1}{3} + 1} = \frac{5}{29}$
  - t(far|hen) =  $\frac{2/5}{\frac{2}{5} + \frac{2}{3}} = \frac{3}{8}$
  - t(away|hen) =  $\frac{2/3}{\frac{2}{5} + \frac{2}{3}} = \frac{5}{8}$



#### Results from two solutions

- t(far|yuan) = 7/4/(7/4+1/4)=7/8
- t(away|yuan) = 1/4/(8/4) = 1/8
- t(far|hen) = 1/4/(1/4+3/4)=1/4
- t(away|hen) = 3/4/(1/4+3/4)=3/4

• 
$$t(far|yuan) = \frac{1+3/5}{\frac{3}{5} + \frac{1}{3} + 1} = \frac{24}{29}$$

• 
$$t(away|yuan) = \frac{1/3}{\frac{3}{5} + \frac{1}{3} + 1} = \frac{5}{29}$$

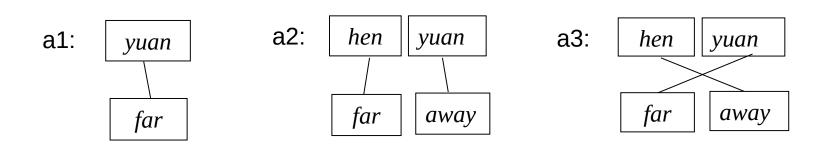
• 
$$t(far|hen) = \frac{2/5}{\frac{2}{5} + \frac{2}{3}} = \frac{3}{8}$$

• 
$$t(away|hen) = \frac{2/3}{\frac{2}{5} + \frac{2}{3}} = \frac{5}{8}$$

## Why different?











#### Content

#### **Phrase-based Translation Model**

Learning a Phrase Translation Table

**Bidirectional Word Alignment** 

Phrase Pair Extraction

Phrase Translation Probability

**Exercises** 



#### Phrase-based Translation Model

Word-based models translate words as atomic units.



#### Phrase-based Translation Model

- Word-based models translate words as atomic units.
- Phrase-based models translate phrases as atomic unit
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- Word-based models translate words as atomic units.
- Phrase-based models translate phrases as atomic unit
   s.
- A phrase is a contiguous sequence of words in a sente nce.



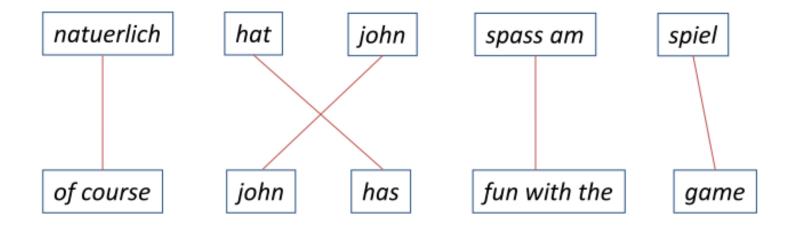
- Word-based models translate words as atomic units.
- Phrase-based models translate phrases as atomic unit
   s.
- A phrase is a contiguous sequence of words in a sente nce.
  - He likes reading

Phrase-based models are the "standard" model in statistical machine translation.

Short: PBSMT, PB-SMT



## Example



- Source sentence is segmented into phrases.
- Each phrase is translated into target language.
- Phrases are re-ordered.



- A monolingual phrase:
  - A phrase can be any contiguous sequence of words in a sentence

e.g. of course, fun with the



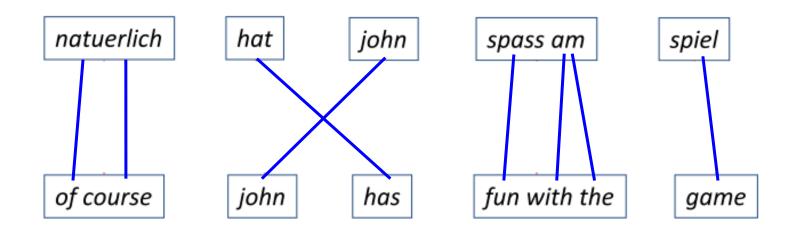
- A monolingual phrase:
  - A phrase is not necessarily syntactic well-formed
     e.g. fun with the



- A monolingual phrase:
  - A phrase is not necessarily semantically meaningful
     e.g. with the

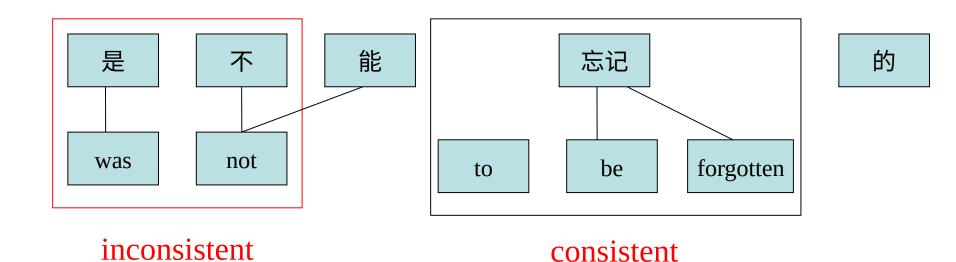


• A bilingual phrase pair should be consistent with word alignment.





### Bilingual Phrase Pairs: Consistency





#### Advantages:

many-to-many translation can handle non-compositional phrases or idioms

e.g. real estate, face value, kick the bucket, shooting the breeze



- Advantages:
  - use of local context in translation

e.g. the boy in a red shirt | 穿红衬衣的男孩



#### Advantages:

the more data, the longer phrases can be learnede.g. phrase-based SMT is the state-of-the-artNice to meet you, can I have the bill please?



- Advantages:
  - the model is conceptually much simpler.
- e.g. no need the fertility, insertion and deletion in the word-based models.



### Phrase Translation Table

- Main knowledge source:
  - table with phrase translations and their probabilities
- Example: phrase translations for natuerlich

Translation	Probability		
of course	0.5		
naturally	0.3		
of course,	0.15		
, of course ,	0.05		



#### Phrase Translation Table

 Real example taken from Europarl for the German phrase den Vorschlag

English	Probability		English	Probability	
the proposal	0.6277		the suggestions	0.0114	
's proposal	0.1068		the proposed	0.0114	
a proposal	0.0341		the motion	0.0091	
the idea	0.025		the idea of	0.0091	
this proposal	0.0227		the proposal,	0.0068	
proposal	0.0205		its proposal	0.0068	
of the proposals	0.0159		it	0.0068	
the proposals	0.0159		•••••		



### Phrase Translation Table

English	Probability	English	Probability
the proposal	0.6277	the suggestions	0.0114
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proposal	0.0205	its proposal	0.0068
of the proposals	0.0159	it	0.0068
the proposals	0.0159	•••••	

- ✓ lexical variation (proposal vs suggestions)
- ✓ morphological variation (proposal vs proposals)
- ✓ included function words (the, a, ...)
- ✓ noise (it)



#### Content

Phrase-based Translation Model

**Learning a Phrase Translation Table** 

**Bidirectional Word Alignment** 

Phrase Pair Extraction

Phrase Translation Probability

**Exercises** 



Task: learn the model from a parallel corpus



Task: learn the model from a parallel corpus

Three stages:



Task: learn the model from a parallel corpus Three stages:

1. word alignment: using IBM models or other method



Task: learn the model from a parallel corpus Three stages:

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Task: learn the model from a parallel corpus Three stages:

- 1. word alignment: using IBM models or other method
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- 3. scoring phrase pairs



### Content

Phrase-based Translation Model

Learning a Phrase Translation Table

**Bidirectional Word Alignment** 

Phrase Pair Extraction

Phrase Translation Probability

**Exercises** 





• Each target word can be aligned to at most one source word. Therefore, it's not possible to end up with an alignment of one target word to many source words

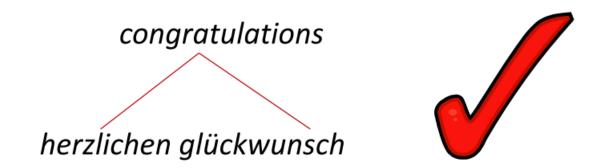
herzlichen glückwunsch congratulations





### How to fix this?

Compute word alignments in both directions!



 In this way, we can get many-to-one alignments as well as one-to-many alignments.



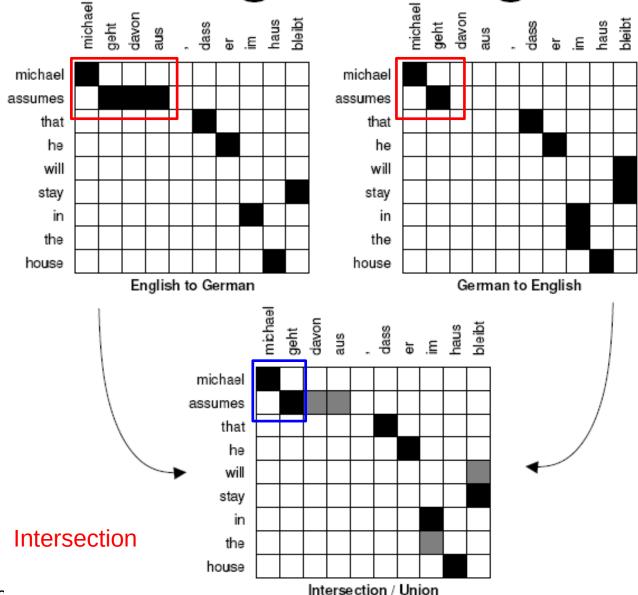
# Bidirectional Word Alignment

#### Algorithm of Bidirectional word alignment:

- 1. Using IBM Models to do word alignment in one direction.
- 2. Using IBM Models to do word alignment in the other direction.
- 3. Merge the above two alignments.

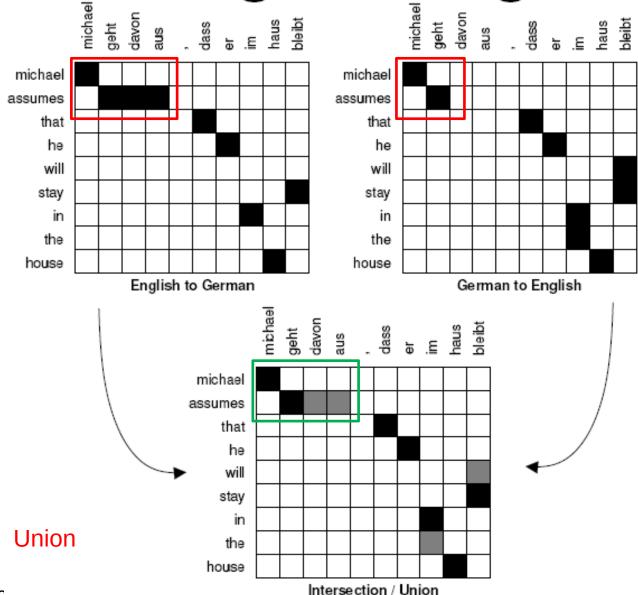
## Symmetrizing Word Alignments





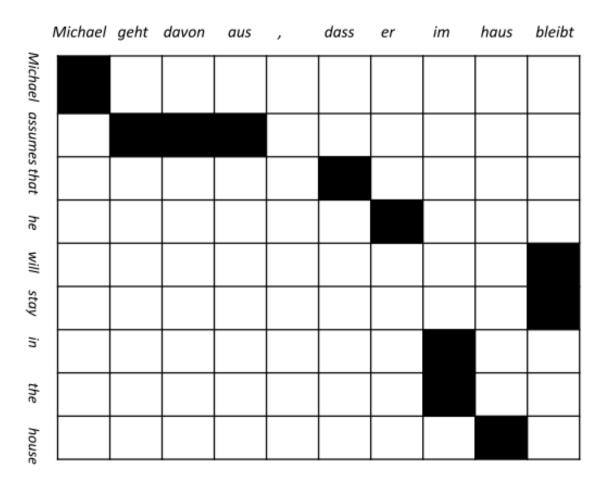
## Symmetrizing\_Word Alignments

















- Add alignment points from union based on heuristics:
  - directly/diagonally neighboring points
  - finally, add alignments that connect unaligned words in source and/or target
- Popular method: grow-diag-final-and



#### Content

Phrase-based Translation Model

Learning a Phrase Translation Table

**Bidirectional Word Alignment** 

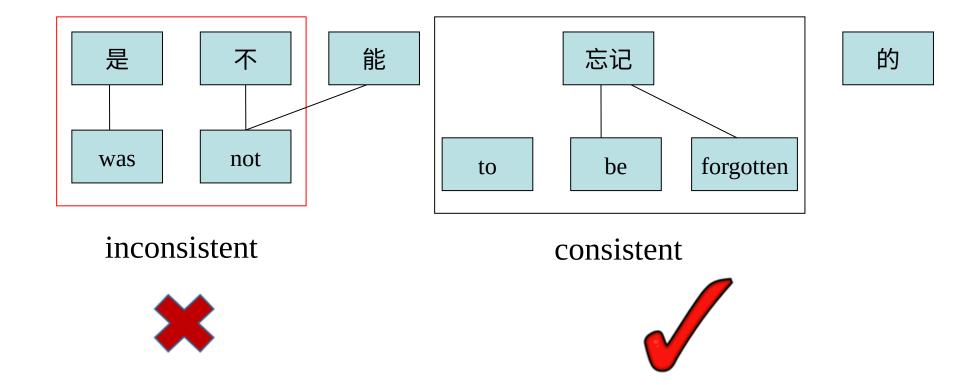
**Phrase Pair Extraction** 

Phrase Translation Probability

**Exercises** 

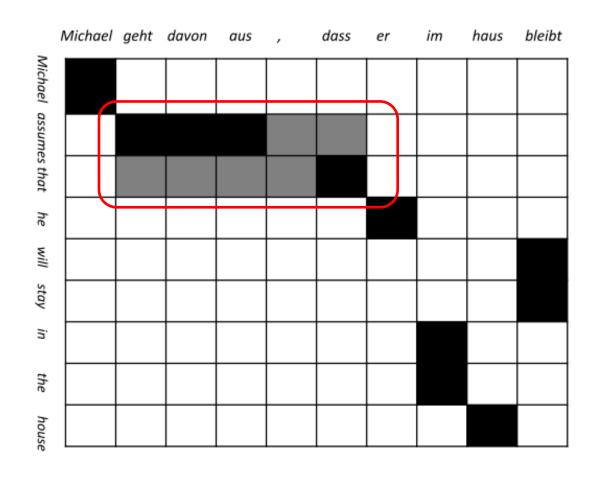


# Recall: Bilingual Phrase Pairs





## Extracting Phrase Pairs



extract phrase pair consistent with word alignment:

assumes that / geht davon aus, dass

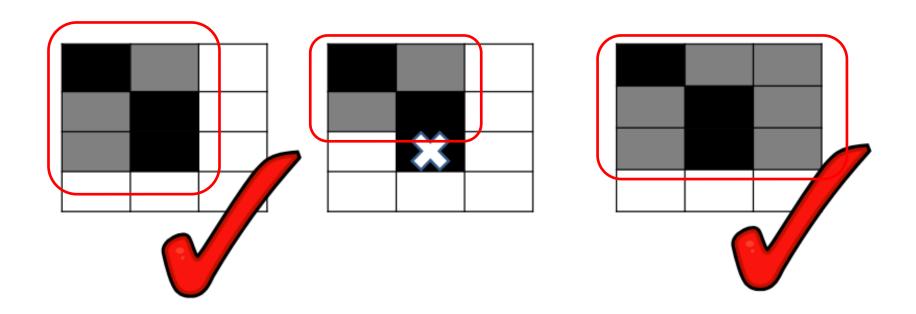


#### **Consistent Conditions**

- A phrase pair (e, f) is consistent with a bidirectional word alignment A if and only if
  - For all words  $e_i$  in e, if  $e_i$  is aligned to a word  $f_j$  in A, then  $f_j$  is in f.
  - For all words  $f_j$  in f, if  $f_j$  is aligned to a word  $e_i$  in A, then  $e_i$  is in e.
  - There exists  $e_i$  in e,  $f_j$  in f:  $(e_i, f_j)$  in A

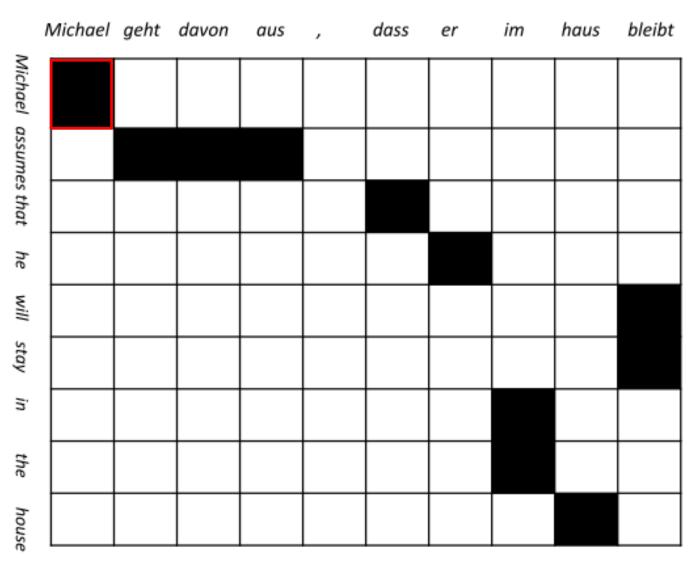


## Consistent with Word Alignment



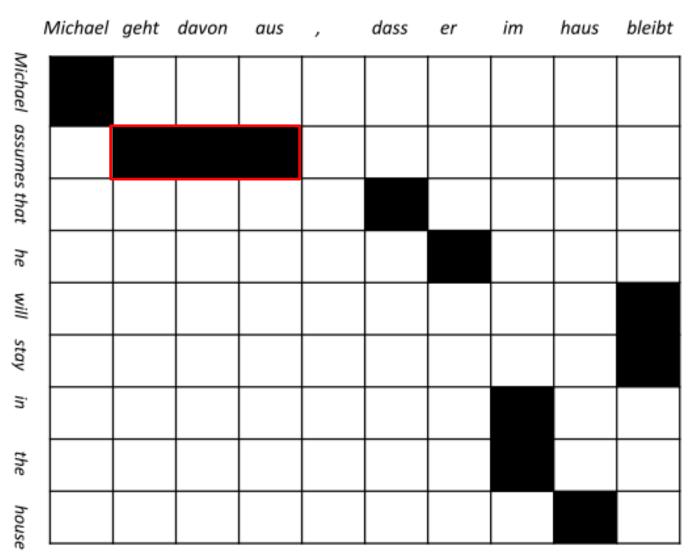


### Phrase Pair Extraction

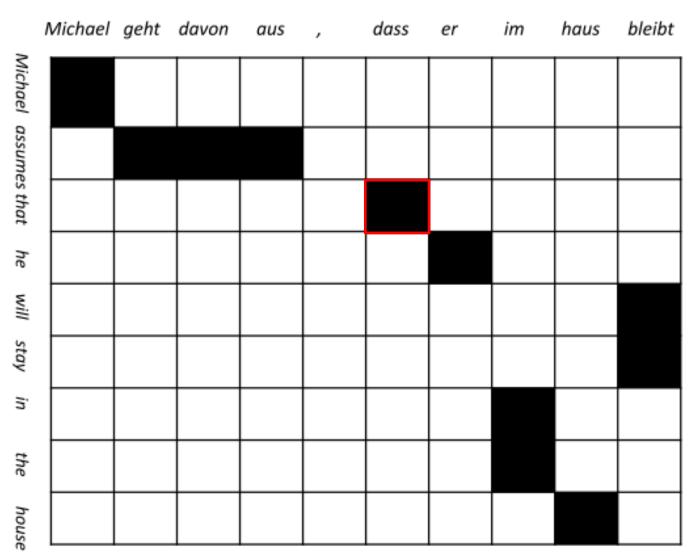




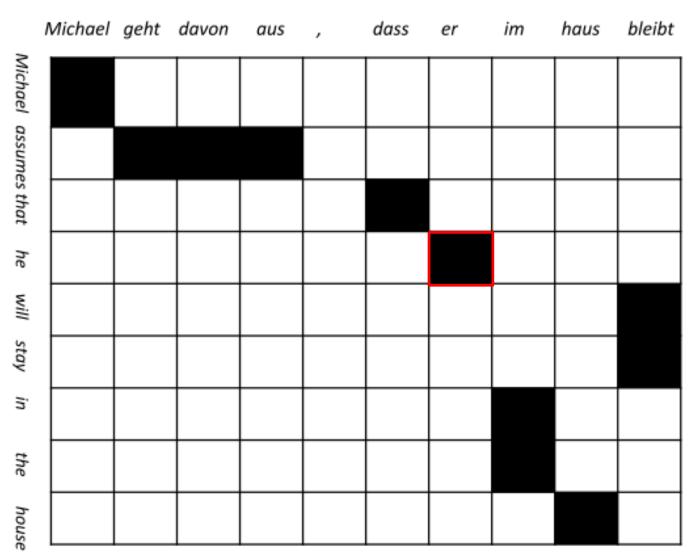
### Phrase Pair Extraction



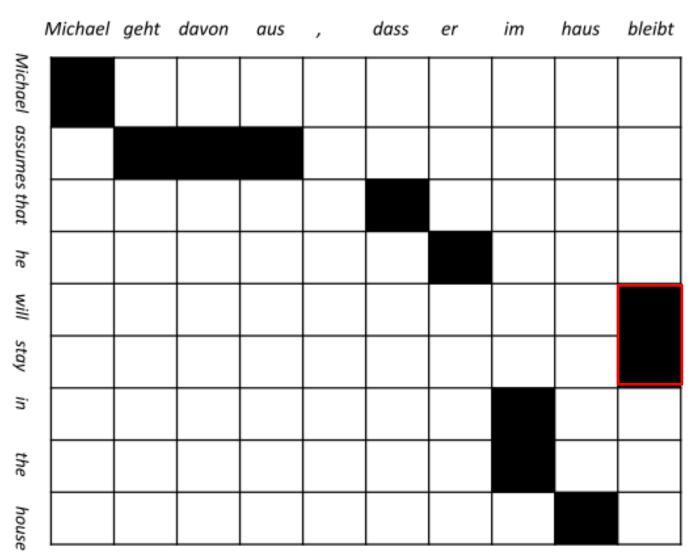




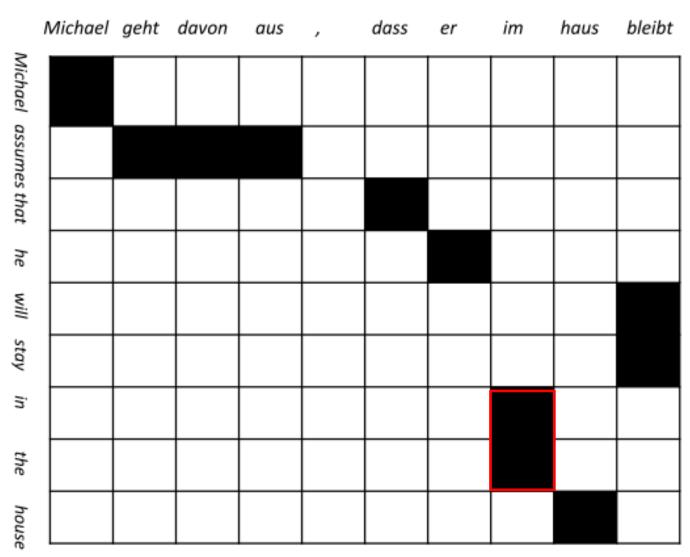




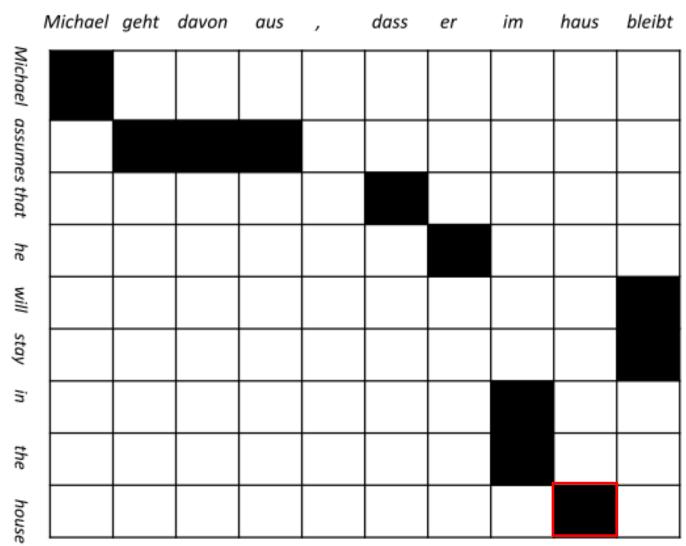








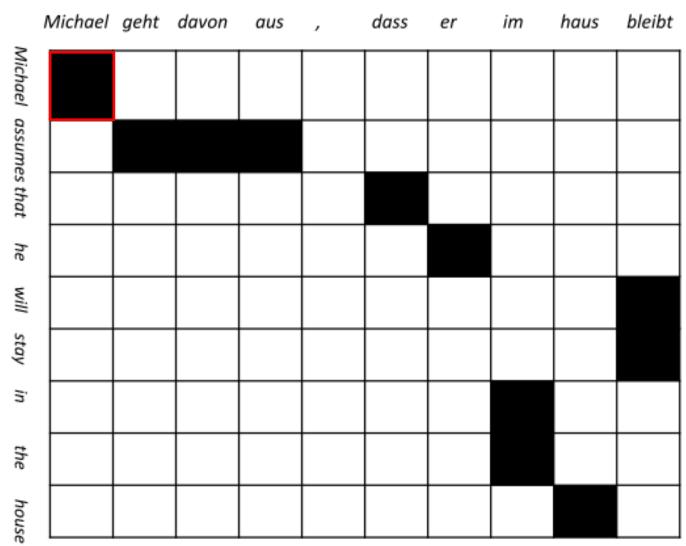




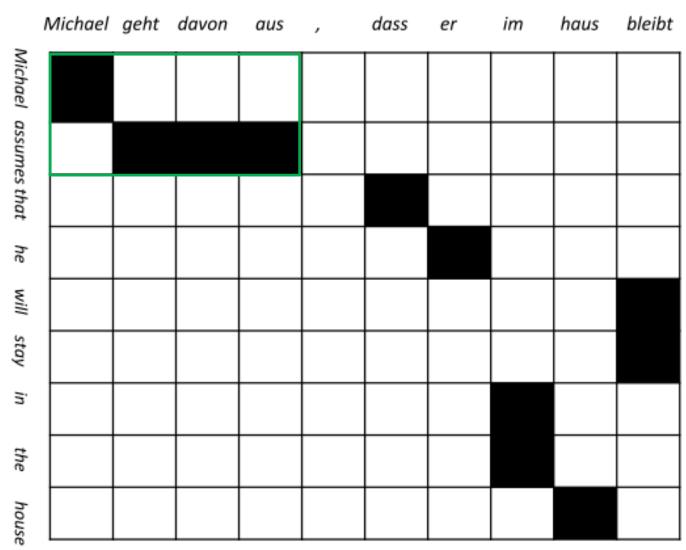


```
michael | michael
assumes | geht davon aus / geht davon aus ,
that | dass / , dass
he | er
will stay | bleibt
in the | im
house | haus
```

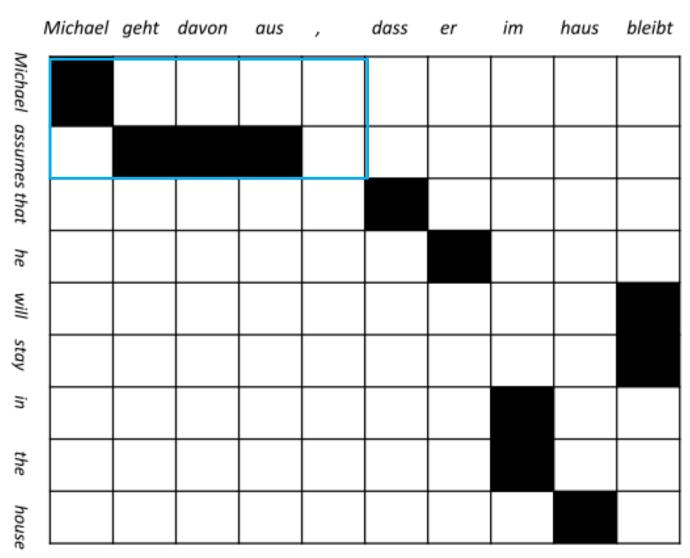




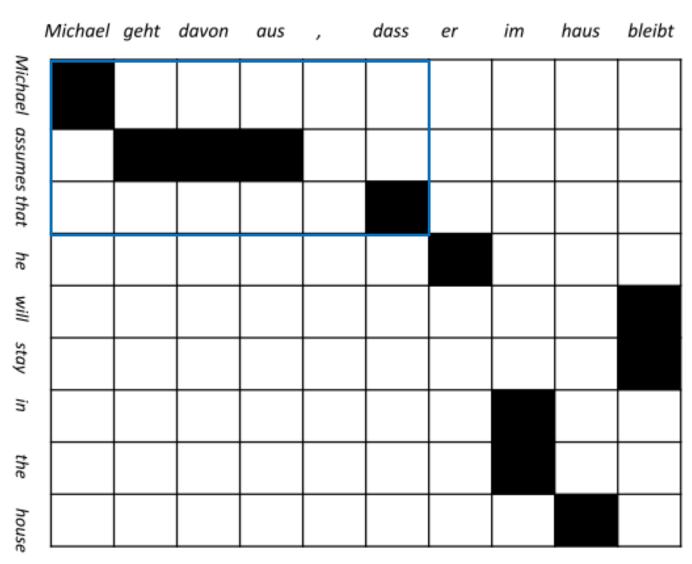




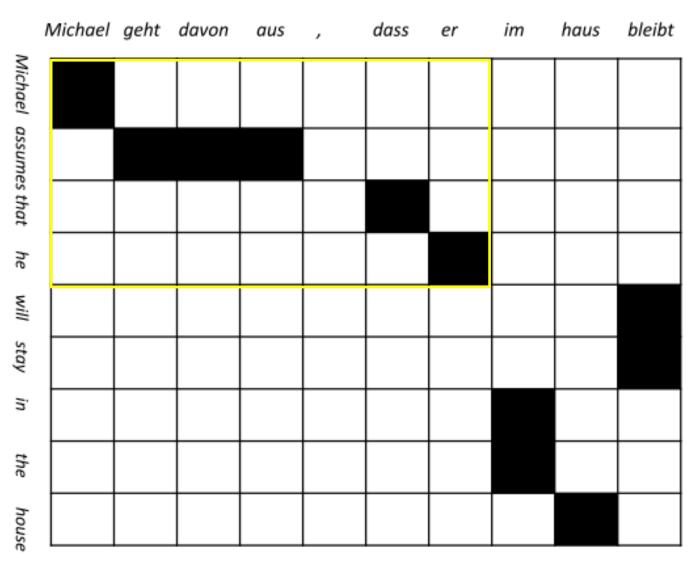




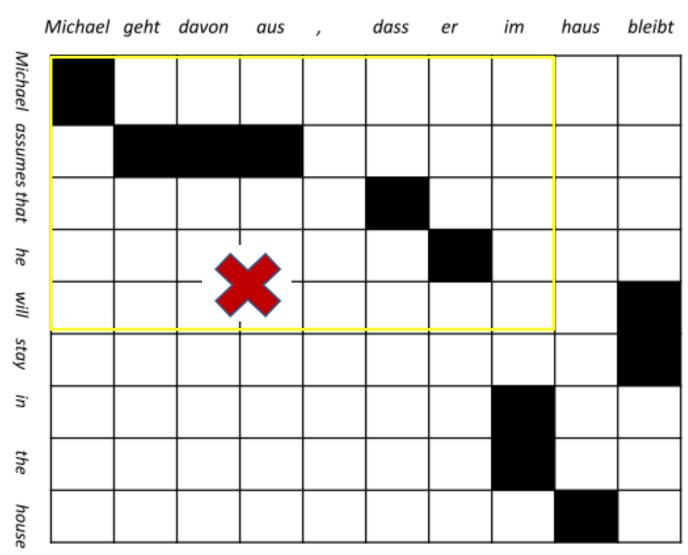




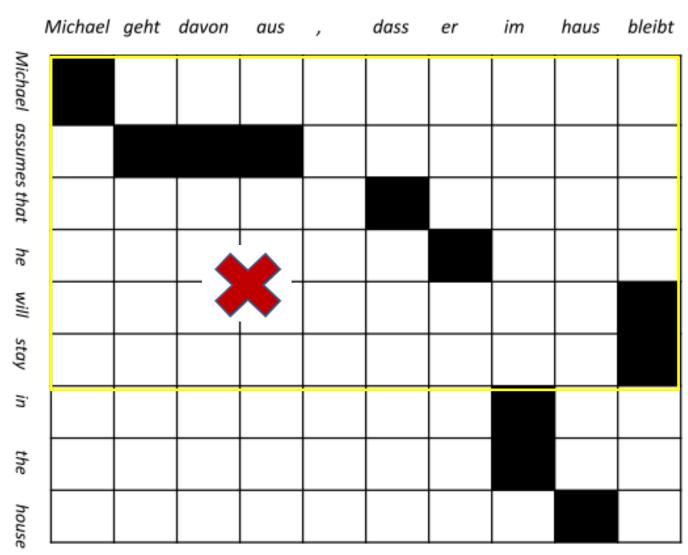




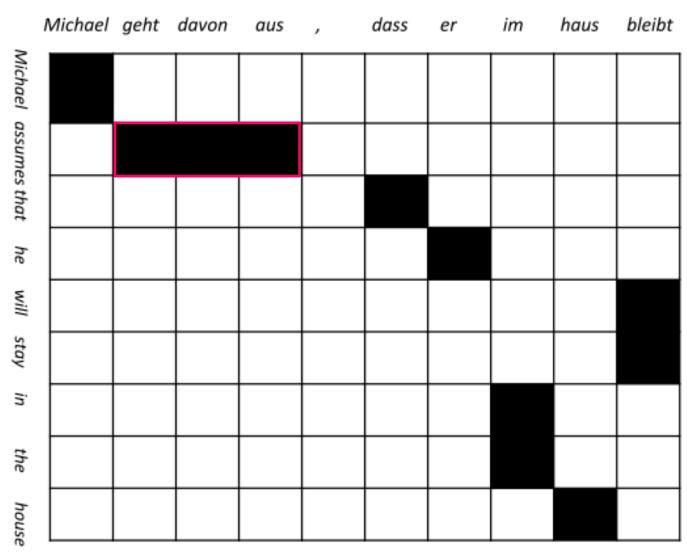




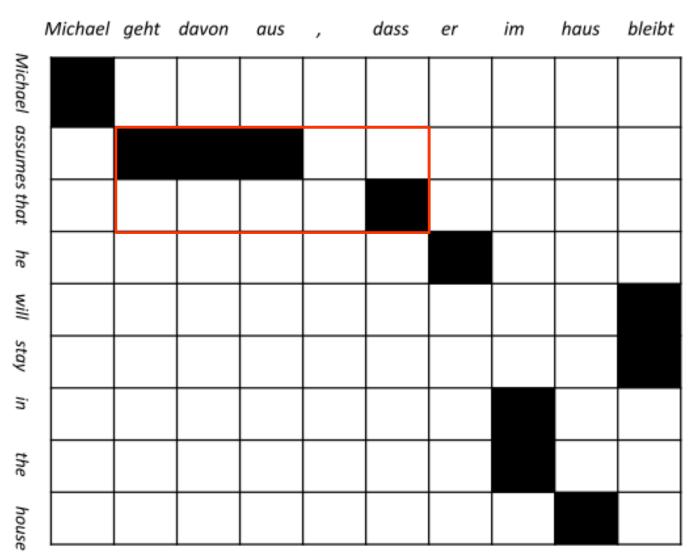




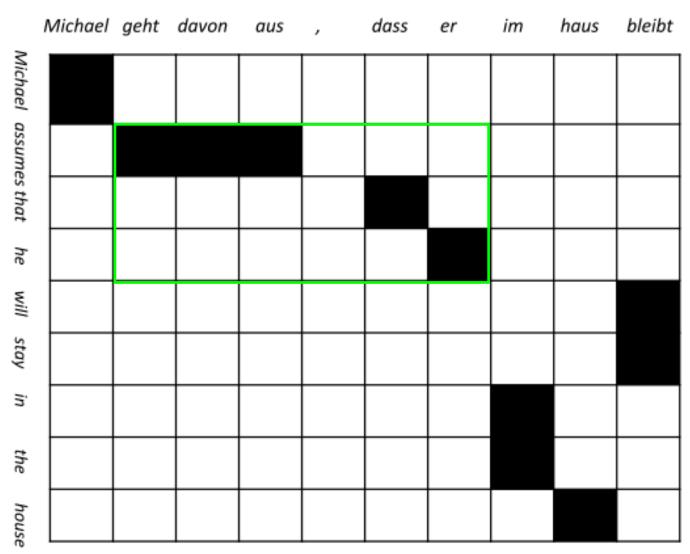




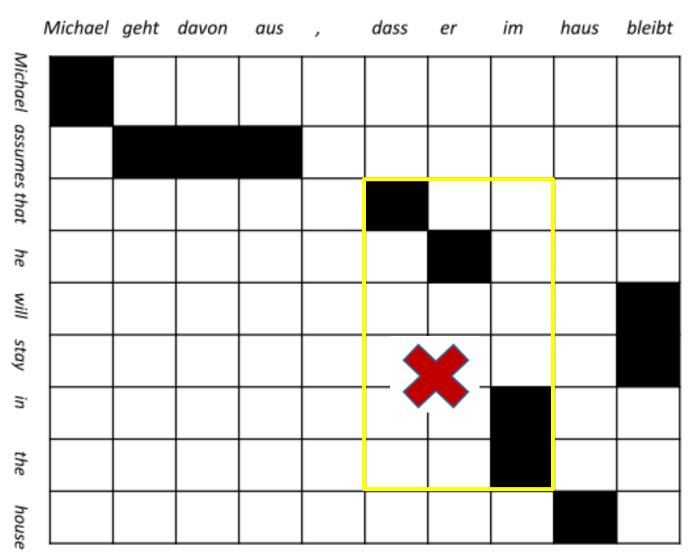




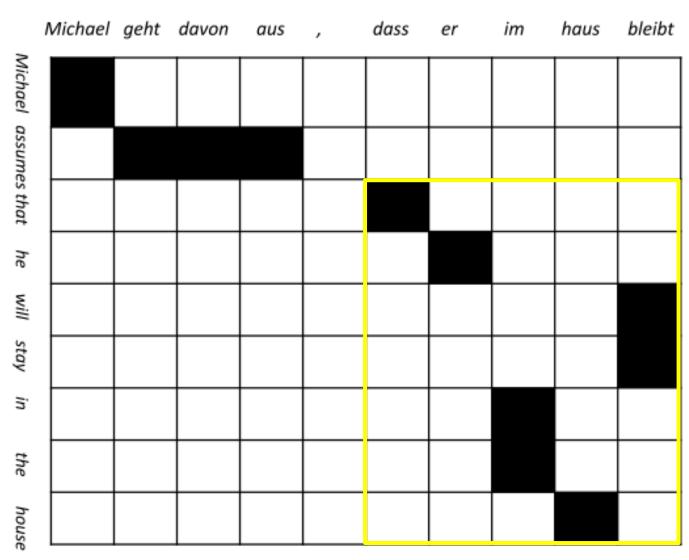




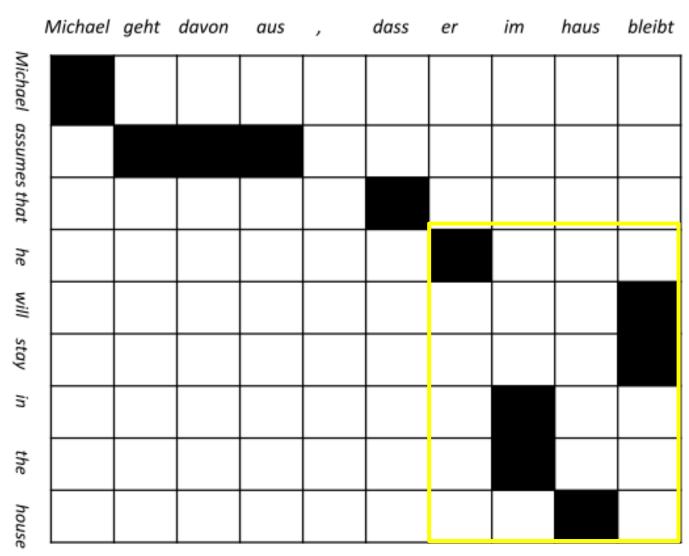




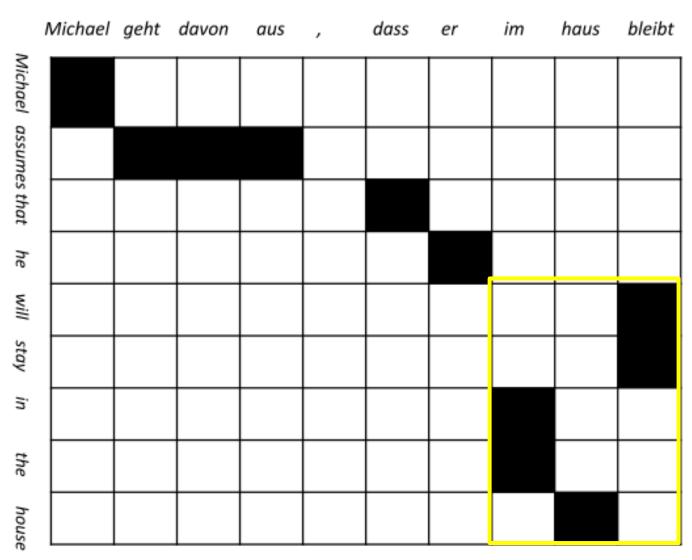




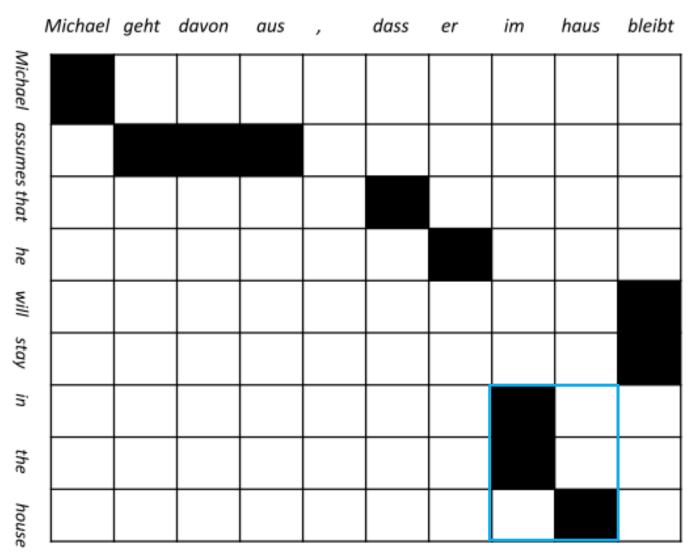














# Phrase Pair Extraction (More)

- michael assumes | michael geht davon aus / michael geht davon aus ,
- assumes that | geht davon aus , dass
- assumes that he | geht davon aus , dass er
- that he | dass er / , dass er
- in the house | im haus
- michael assumes that | michael geht davon aus , dass
- michael assumes that he | michael geht davon aus , dass er
- michael assumes that he will stay in the house | michael geht davon aus , dass er im h
  aus bleibt
- assumes that he will stay in the house | geht davon aus , dass er im haus bleibt
- that he will stay in the house | dass er im haus bleibt / dass er im haus bleibt ,
- he will stay in the house | er im haus bleibt
- will stay in the house | im haus bleibt



#### Exercise

Source: a b c d

Target: w x y z

Extract all bilingual phrase pairs consistent with the

following word alignment.

	a	b	С	d
<b>\{</b>				
×				
<b>&lt;</b>				
Z				





w | a wxyz|abc wxyz|abcd  $X \mid C$  $x \mid c d$ x y z | b cx y z | b c dy z | b

	a	b	С	d
<b>\</b>				
×				
Y				
Z				



#### Content

Phrase-based Translation Model

Learning a Phrase Translation Table

Bidirectional Word Alignment

Phrase Pair Extraction

**Phrase Translation Probability** 

**Exercises** 



# Scoring Phrase Translations

- Phrase pair extraction: collect all phrase pairs from the data
- Phrase pair scoring: assign probabilities to phrase translations
- Score by relative frequency (MLE):

$$\phi(\bar{f}|\bar{e}) = \frac{count(\bar{e},\bar{f})}{\sum_{\bar{f}_i} count(\bar{e}',\bar{f}_i')}$$



# Scoring Phrase Translations

Score by relative frequency (MLE) (the other direction):

$$\phi(\bar{e}|\bar{f}) = \frac{count(\bar{e},\bar{f})}{\sum_{\bar{e}_i} count(\bar{f},\bar{e}_i)}$$



# Example

• Phrase translations for natuerlich, calculate the phrase translation probability.

Translation	Counts
of course	50
naturally	30
of course,	15
, of course ,	10



# Scoring Phrase Translations

$$\phi(\bar{e}|\bar{f}) = \frac{count(\bar{e},\bar{f})}{\sum_{\bar{e}_i} count(\bar{f},\bar{e}_i)}$$

$$\phi(\bar{e}|\bar{f}) = \phi(of\ course|natuerlich) = \frac{50}{50 + 30 + 15 + 10} = 0.5$$

$$\phi(\bar{e}|\bar{f}) = \phi(naturally|natuerlich) = \frac{30}{50 + 30 + 15 + 10} = 0.3$$

$$\phi(\bar{e}|\bar{f}) = \phi(of\ course\ , |natuerlich) = \frac{15}{50+30+15+10} = 0.15$$

$$\phi(\bar{e}|\bar{f}) = \phi(\text{, of course , |natuerlich}) = \frac{5}{50 + 30 + 15 + 10} = 0.05$$



#### Example: a Real Phrase Table

Source side: French

Target side: English

```
de l' immigration , ||| of immigration , ||| 0.5 0.0792945 1 0.0953929 |||
de l' immigration ||| immigration ||| 0.0769231 0.0872234 0.5 0.402069 |||
de l' immigration ||| of immigration ||| 0.5 0.10012 0.5 0.115455 ||| 0-0
de l' immobilier amé ricain ||| us housing ||| 0.5 0.00182555 1 0.0649596
de l' immobilier pour ||| of housing in ||| 1 0.000297943 1 0.00156694 |||
de l' immobilier ||| housing ||| 0.0769231 0.0173907 0.25 0.16069 ||| 1-0
de l' immobilier ||| of housing ||| 0.5 0.0199621 0.25 0.0461423 ||| 0-0 1
de l' immobilier ||| real estate ||| 0.333333 0.0447481 0.25 0.0201379 |||
de l' immobilier ||| remain ||| 0.05 0.000692525 0.25 0.04 ||| 2-0 ||| 20
```



#### Content

Phrase-based Translation Model

Learning a Phrase Translation Table

**Bidirectional Word Alignment** 

Phrase Pair Extraction

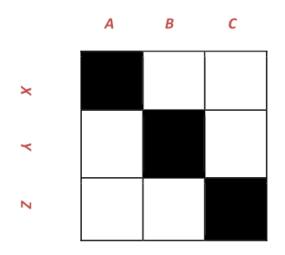
Phrase Translation Probability

**Exercises** 



#### Exercise 1

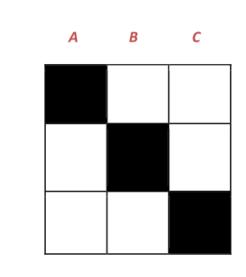
• List all phrase pairs that are consistent with the following word alignment:







$X \mid A$
$XY \mid AB$
XYZ ABC
$Y \mid B$
YZ BC
$Z \mid C$

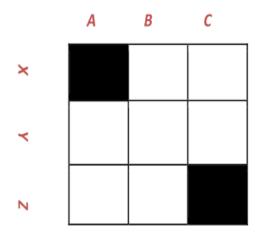


×



#### Exercise 2

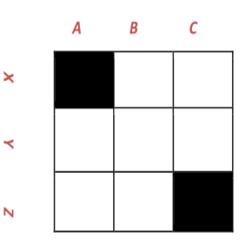
• List all phrase pairs that are consistent with the following word alignment:







 $X \mid A$  $X \mid A B$  $XY \mid A$  $XY \mid AB$ XYZ|ABC $Z \mid C$  $YZ \mid C$  $YZ \mid BC$ 





#### Exercise 3

• Given the following statistics of extracted bilingual p hrases in terms of Chinese phrase "xihuan paobu", pl ease calculate the translation probabilities for each ph rase pair.

Translation	Counts
likes running	1500
like running	800
likes jogging	700
love running	100



### Solution 3

$\phi(likes\ running xihuan\ paobu) =$	$=\frac{1500}{1500+300+300}=0.484$	ŀ
	800	
$\phi(like\ running xihuan\ paobu) =$	$\frac{1500 + 800 + 700 + 100}{1500 + 800 + 700 + 100} = 0.258$	0.258
$\phi(likes\ running xihuan\ paobu)$ =	== = 0.220	6
	100	
$\phi(likes\ running xihuan\ paobu)$ :	$=\frac{100}{1500 + 800 + 700 + 100} = 0.03$	2

Translation	Counts
likes running	1500
like running	800
likes jogging	700
love running	100



# Discussion