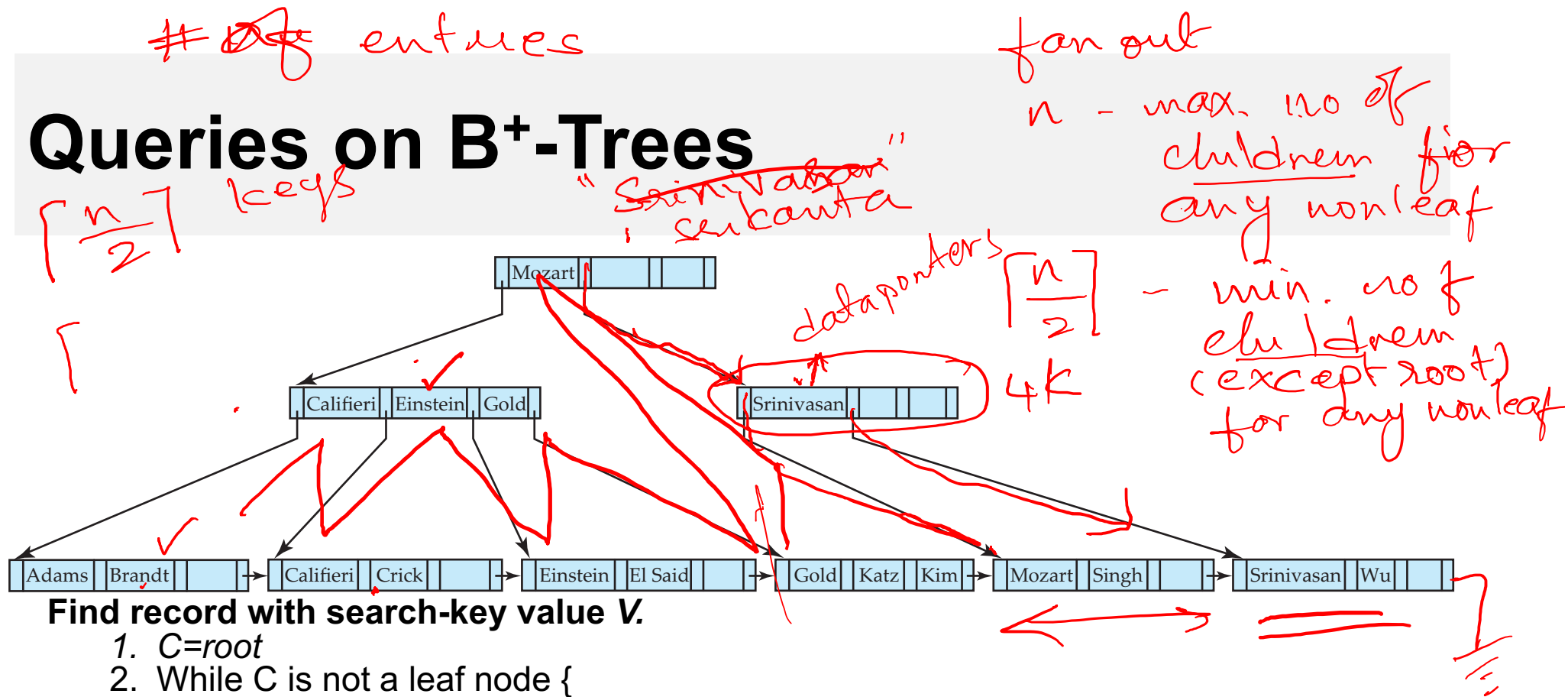


COL 362 & COL 632

Indexing

03 Mar 2023

Queries on B⁺-Trees



Find record with search-key value V.

1. $C = \text{root}$
2. While C is not a leaf node {
 1. Let i be least value s.t. $V \leq K_i$.
 2. If no such exists, set $C = \text{last non-null pointer in } C$
 3. Else { if ($V = K_i$) Set $C = P_{i+1}$ else set $C = P_i$ }
3. Let i be least value s.t. $K_i = V$
4. If there is such a value i , follow pointer P_i to the desired record.
5. Else no record with search-key value V exists.

Analysis of B⁺-trees

- No. of search keys: 1,000,000
- Block size: 4K ✓
- Size of an index entry: 40B
- Max. no. of search keys per block:
- Max. height of the tree:
- No. of block accesses per query:

Key + Pointer

100

4

$\left(\begin{matrix} 4 \\ 4 \end{matrix} + 1 \right)$

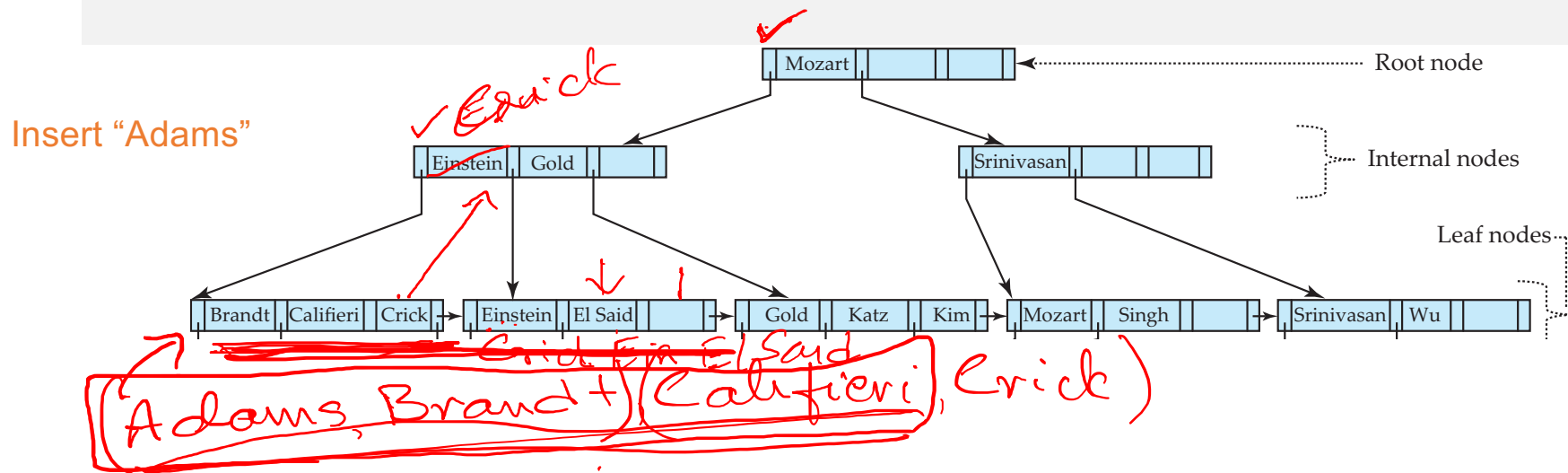
$$n = \frac{4K}{40B} \approx 100$$

$$\log_{50} 1 \times 10^6 = 4$$

$$\log_2 1 \times 10^6$$

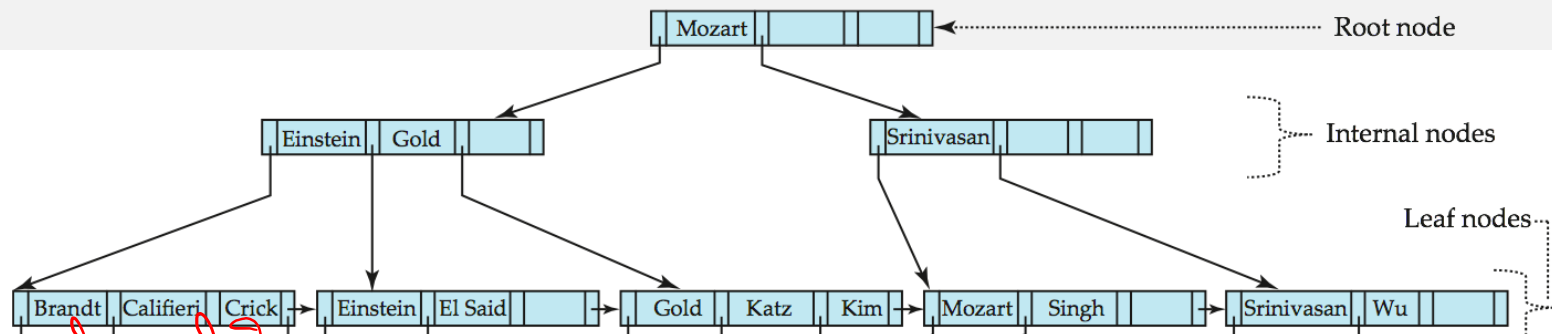
B+-trees – insertion

B⁺-Tree Insertion

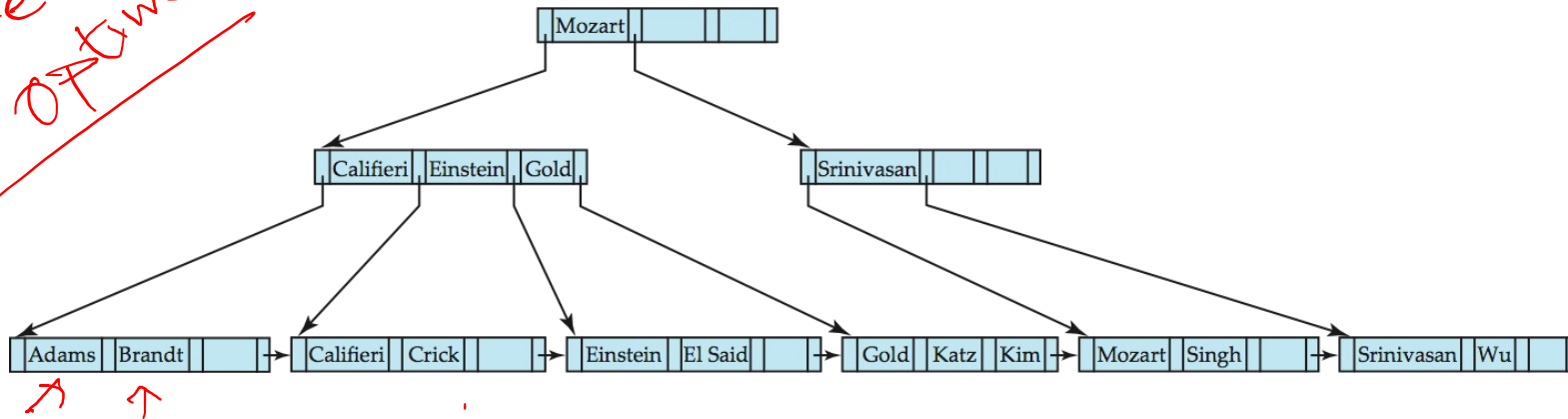


B⁺-Tree Insertion

n/2



Correct and optimal?



B⁺-Tree before and after insertion of "Adams"