QUANTUM ELECTRONICS AND ATOMIC PHYSICS

BASIC INSTRUCTIONS OF THE COURSE

- Instructor: Kihwan Kim 金奇奂,
 MMW-S423, <u>kimkihwan@mail.tsinghua.edu.cn</u>
- Teaching Assistant: Mu Qiao 乔木,
 MMW-S427, <u>qiao-m17@mails.tsinghua.edu.cn</u>
 Class hours: Fri. from 9:50 am to 12:15 pm
- Class Room: 6B112
- Office time: On every Wed. from 1 pm to 2 pm

TEXT BOOKS & REFERENCES

- Quantum Electronics for Atomic Physics
- by Warren Nagounary (Oxford Press 2010)
- Atomic Physics

by Foot, C. J. (Oxford University Press, 2005)

Fundamentals of Photonics

by Saleh, B. E. A. and Teich, M. C. (2nd Ed., Wiley-Interscience, 2007)

Lasers

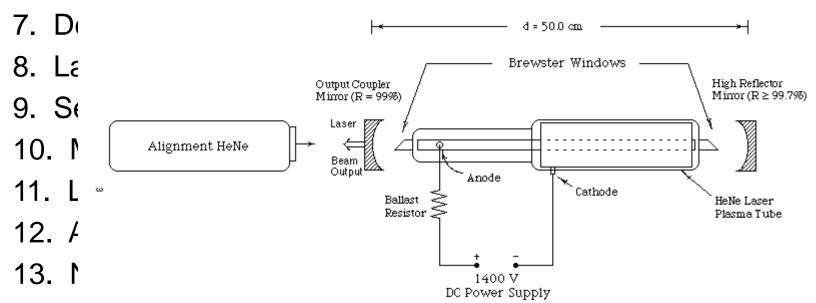
by Siegman, A. E. (University Science Books, 1986)

TOPICS

- 1. Gaussian beams
- 2. Optical resonators geometrical properties
- 3. Energy relations in optical cavities
- 4. Optical cavity as frequency discriminator
- 5. Laser gain and some of its consequences
- 6. Laser oscillation and pumping mechanisms
- 7. Descriptions of specific CW laser systems
- 8. Laser gain in a semiconductor
- 9. Semiconductor diode lasers
- 10. Mode-locked lasers and frequency metrology
- 11. Laser frequency stabilization and control systems
- 12. Atomic and molecular discriminants
- 13. Nonlinear optics
- 14. Frequency and amplitude modulation

TOPICS

- 1. Gaussian beams
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14. Frequency and amplitude modulation

GRADING

• Midterm 20%

• Final 20%

• Homework 50%

• Attendance 10%

- Homework:
 - How often? every week
 - When to submit? in two weeks after the assignment
 - Where to submit? Online
 - Problem solving? In the end of the class after the submission
- Extra Points for "Good Questions" or "Good Answers" in class
 - Broad questions that the instructor cannot answer in the same class generally qualifies!
 - Answers that the instructor cannot provide in the class
 - Equivalent to the point of one week of homework

1. GAUSSIAN BEAM

1.2 PARAXIAL WAVE EQUATION

Wave equation

$$\nabla^2 u - \frac{1}{c^2} \frac{\partial^2 u}{\partial t^2} = 0,$$

• With a time dependency by $e^{i\omega t}$

$$\nabla^2 u + k^2 u = 0,$$

 With paraxial assumption that requires that the normals to the wavefronts make a small angle

$$u(x, y, z) = \psi(x, y, z)e^{-ikz}$$

The Paraxial Wave Equation

$$\nabla_t^2 \psi - 2ik \frac{\partial \psi}{\partial z} = 0,$$

where
$$\nabla_t^2 \ (= \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2}).$$

1.3 GAUSSIAN BEAM FUNCTIONS AND THE COMPLEX BEAM PARAMETER

A simple solution of the paraxial wave equation

$$\nabla_t^2 \psi - 2ik \frac{\partial \psi}{\partial z} = 0,$$

A trial solution,

$$\psi(x, y, z) = \exp\left\{-i\left(P(z) + \frac{k}{2q(z)}r^2\right)\right\}, \quad r^2 = x^2 + y^2,$$
$$\frac{dq(z)}{dz} = 1 \quad \text{and} \quad \frac{dP(z)}{dz} = -\frac{i}{q(z)}$$

Homework #1: derive the above equations

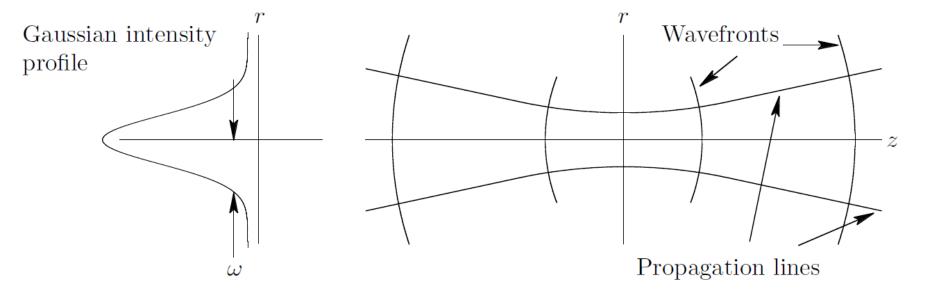
$$\begin{split} \psi(x,y,z) &= \exp\left\{-i\left(P(z) + \frac{k}{2q(z)}r^2\right)\right\}, \quad r^2 = x^2 + y^2, \\ \frac{dq(z)}{dz} &= 1 \quad \text{and} \quad \frac{dP(z)}{dz} = -\frac{i}{q(z)} \\ q(z_2) &= q(z_1) + (z_2 - z_1) \\ \frac{1}{q} &= \frac{1}{R} - i\frac{\lambda}{n\pi\omega^2} \quad \text{, complex beam parameter } q \end{split}$$

Since,
$$u(x, y, z) = \psi(x, y, z)e^{-ikz}$$

$$u(x, y, z) = \exp\left\{-i\left(P(z) + kz + k\frac{r^2}{2R}\right) - \frac{r^2}{\omega^2}\right\}$$

The radius of the beam is ω .

The wave-front would be $z + \frac{r^2}{2R} = const.$



$$\frac{1}{q} = \frac{1}{R} - i\frac{\lambda}{n\pi\omega^2} \qquad u(x, y, z) = \exp\left\{-i\left(P(z) + kz + k\frac{r^2}{2R}\right) - \frac{r^2}{\omega^2}\right\}$$

The wave-front would be

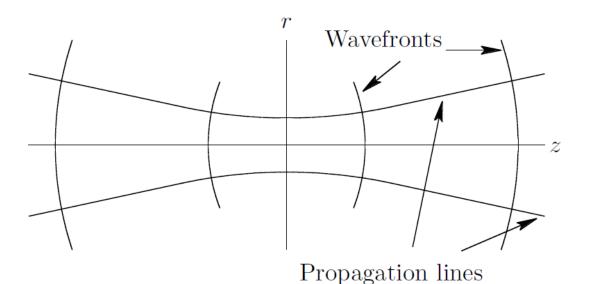
$$z + \frac{r^2}{2R} = const.$$

The radius of the beam is ω .

When $r \ll R$, the paraxial approximation, R can be considered as the radius of a wave-front sphere

1.4 SOME GAUSSIAN BEAM PROPERTIES

Gaussian intensity profile

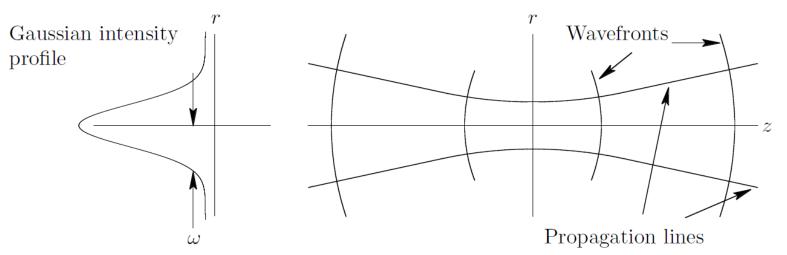


At waist:
$$q \equiv q_0 = i \frac{n\pi\omega_0^2}{\lambda}$$
 $\frac{1}{q} = \frac{1}{R} - i \frac{\lambda}{n\pi\omega^2}$

$$q(z) = q_0 + z = i\frac{n\pi\omega_0^2}{\lambda} + z$$
 $q(z_2) = q(z_1) + (z_2 - z_1)$

$$\frac{1}{q} = \frac{1}{R} - i \frac{\lambda}{n\pi\omega^2}$$

$$q(z_2) = q(z_1) + (z_2 - z_1)$$



$$q(z) = q_0 + z = i\frac{n\pi\omega_0^2}{\lambda} + z$$

$$\frac{1}{q} = \frac{1}{R} - i\frac{\lambda}{n\pi\omega^2}$$

Distance to waist $=-Re\{q(z)\}$ and,

Radius of waist $=\sqrt{\frac{\lambda}{n\pi}}Im\{q(z)\}.$

$$\omega(z) = \omega_0 \left[1 + \left(\frac{\lambda z}{n\pi\omega_0^2} \right)^2 \right]^{1/2}$$

$$R(z) = z \left[1 + \left(\frac{n\pi\omega_0^2}{\lambda z} \right)^2 \right].$$

Homework #2: derive the above equations and draw the functions