

~~equal interval~~

Ch [2] in interpolation

equal interval ← در نسب الفتره على طول
ولا در نسب دالة كثيرة الحدود

a) Newton Forward → قریب من بداية الجدول

b) Newton back ward → قریب من نهاية الجدول

X	x_0	x_1	x_2	x_3	x_4
$y, f(x)$	y_0	y_1	y_2	y_3	y_4

لو نظرنا في منتصف الجدول نفسنا بـ (Backward or Forward)

$$\frac{\text{Back} + \text{For}}{2} \text{ في}$$

Difference Table

X	F(x)	Δ	Δ^2	Δ^3	Δ^4
x_0	y_0	$\frac{y_1 - y_0}{x_1 - x_0} = \Delta_0$	Forward		
x_1	y_1	$\frac{y_2 - y_1}{x_2 - x_1} = \Delta_1$			
x_2	y_2	$\frac{y_3 - y_2}{x_3 - x_2} = \Delta_2$	$\Delta_2 - \Delta_1 = \Delta_1^2$	$\Delta_2^2 - \Delta_1^2 = \Delta_1^3$	$\Delta_2^3 - \Delta_1^3 = \Delta_1^4$
x_3	y_3	$\frac{y_4 - y_3}{x_4 - x_3} = \Delta_3$	$\Delta_3 - \Delta_2 = \Delta_2^2$	$\Delta_3^2 - \Delta_2^2 = \Delta_2^3$	$\Delta_3^3 - \Delta_2^3 = \Delta_2^4$
x_4	y_4		Backward		

Newton Forward :-

$$y(x) = y_0 + s \Delta_0 + \frac{s(s-1)}{2!} \Delta_0^2 + \frac{s(s-1)(s-2)}{3!} \Delta_0^3 + \frac{s(s-1)(s-2)(s-3)}{4!} \Delta_0^4$$

$$s = \frac{x - x_0}{h}$$

$$s > 10$$

Back word

$$y(x) = y_4 + s \nabla_3 + \frac{s(s+1)}{2!} \nabla_2^2 + \frac{s(s+1)(s+2)}{3!} \nabla_1^3 + \frac{s(s+1)(s+2)(s+3)}{4!} \nabla_0^4$$

$$s = \frac{x - x_0}{h}$$

$$s \leq 0$$

الشروط

$$y(x) = y_n + \nabla_3 s + \frac{s(s+1)}{2!} \nabla_2^2 + \frac{s(s+1)(s+2)}{3!} \nabla_1^3 + \dots$$

أخرى من الخ الـ ٥

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لو طلبت دالة كثيرة حدود دفلي Newton Lagrange أو Lagrange

EX (6)

For the following data given

$$f(x) = \sin x \text{ estimate}$$

The value of $\sin(30.2^\circ)$

and $\sin(31.3^\circ)$

		30.2 Forward		31.3 Backward	
X		30	30.5	31	31.5
f(x)		0.5	0.50754	0.51504	0.5225

X	y	Δ	Δ^2	Δ^3
30	0.5		Forward	
30.5	0.50754	0.00754	-0.00064	
31	0.51504	0.0075	-0.00004	0
31.5	0.5225	0.00746		
			Backward	

$$h = 0.5$$

$$s = \frac{30.2 - 30}{0.5} = 0.4$$

$$y(30.2) = 0.5 + 0.4 \times 0.00754 + \frac{0.4(0.4-1)}{2!} (-0.00004)$$

$$+ \frac{0.4(0.4-1)(0.4-2)}{3!} (0)$$

$$y(30.2) = 0.50302$$

$$s = \frac{31.3 - 30}{0.5} = -0.4$$

$$y(31.3) = 0.5225 + (-0.4) \times 0.00746 + \frac{(-0.4)(-0.4+1)}{2!} (-0.00004)$$

to

$$y(31.3) = \checkmark$$

Interpolation with spline Functions

x	x_0	x_1	x_2	x_3
$f(x)$	y_0	y_1	y_2	y_3

$\underbrace{\hspace{1.5cm}}_{s_0(x)} \quad \underbrace{\hspace{1.5cm}}_{s_1(x)} \quad \underbrace{\hspace{1.5cm}}_{s_2(x)}$

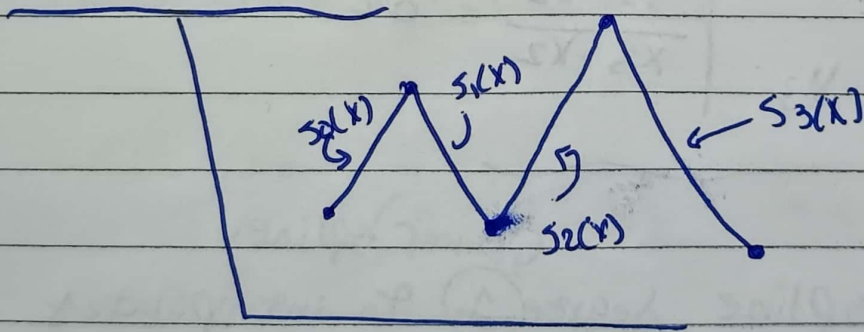
دقوم بزرگوں (۶) : کہند کہ نقطہ

$S_i(x)$ ← عدد الشرائح

تسوق النقطة الى عابرها موجودة في كل اى مشروع وارو اعوض فيها

Linear spline :-

(1) st degree spline



كل ما أعلى أو degree كلما ~~الدراسة~~ الدراسة الدور كثيره الدور

عدد الشرائح = عدد القراءات - 2

~~$$f_i(x) = y_i + y_i + 1 - y_i$$~~

بیشتر از ۱۱ برابر و ۱۱ برابر از ۱۱

$$S_i(x) = y_i + \frac{y_{i+1} - y_i}{x_{i+1} - x_i} (x - x_i)$$

$$= y_i + \delta_i (x - x_i)$$

x	y	δ
x_0	y_0	
x_1	y_1	$\frac{y_1 - y_0}{x_1 - x_0} = \delta_0$
x_2	y_2	$\frac{y_2 - y_1}{x_2 - x_1} = \delta_1$
x_3	y_3	$\frac{y_3 - y_2}{x_3 - x_2} = \delta_2$

EX

Linear spline

Find spline degree 2 to interpolate data

$$F(2-2) = 2$$

 $S_i(x)$ Linear

x	1	1.5	2	2.5	3
$S(x)$	1	3	7	10	15
	$S_0(x)$	$S_1(x)$	$S_2(x)$	$S_3(x)$	



x	y	δ
1	1	4
1.5	3	8
2	7	6
2.5	10	10
3	15	

$j = 0, 1, 2, 3$

~~$s_2(x) = y_2 + \delta_2 (x - x_2)$~~

~~$s_2(x) = 7 + 6(2.2 - 2) = 14.2$~~

$i = 0$
 ~~$s_0(x) = 1 + 4(\frac{x}{2} - 1)$~~

$$i=0$$

$$s_0(x) = 1 + 4(x-1) = 4x-3$$

$$i=1$$

$$s_1(x) = 3 + 8(x-1.5) = 8x-9$$

$$i=2$$

$$s_2(x) = 7 + 6(x-2) = 6x-5$$

$$i=3$$

$$s_3(x) = 10 + 10(x-2.5) = 10x-15$$

$$s_i(x) \begin{cases} \rightarrow 4x-3 & | 1 \leq x < 1.5 \\ \rightarrow 8x-9 & | 1.5 \leq x < 2 \\ \rightarrow 6x-5 & | 2 \leq x < 2.5 \\ \rightarrow 10x-15 & | 2.5 \leq x \leq 3 \end{cases}$$

$$f(2.2) = 6x - 5 = 6 \times 2.2 - 5 = 8.2$$

$$7 \leq 8.2 \leq 10$$

Home work

$$f(x) = x^3 + 2$$

$$\text{at } x = 0, 0.2, 0.4, 0.6, 0.8, 1.0$$

Linear spline

$$\text{to find at } x = 0.1, 0.3, 0.5$$

$$0.7, 0.9$$

$$s_i(x) = ??$$