

Solutions to Homework 5

Instructor: Sid Nadendla

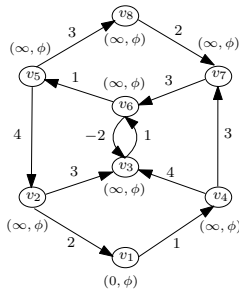
Due: May 7, 2023

Solution to Problem 1: Bellman-Ford Algorithm

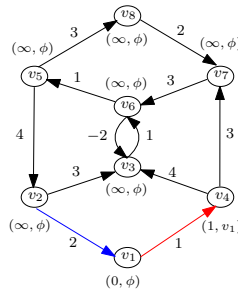
Edge relaxation order: $(v_1, v_4), (v_2, v_1), (v_2, v_3), (v_3, v_6), (v_4, v_3), (v_4, v_7), (v_5, v_2), (v_5, v_8), (v_6, v_3), (v_6, v_5), (v_7, v_6), (v_8, v_7)$

Node Attributes: $(distance_estimate, parent)$

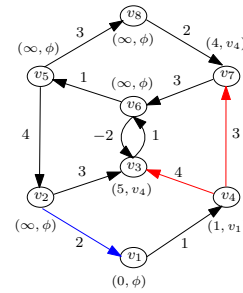
Successful edge relaxations in RED, failed edge relaxations in BLUE.



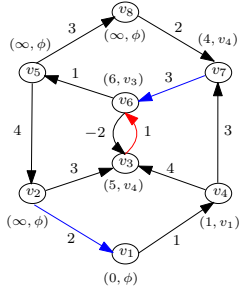
Initialization



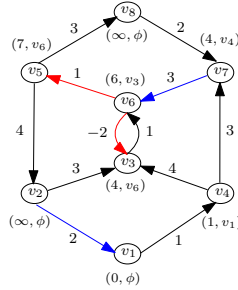
Iteration 1



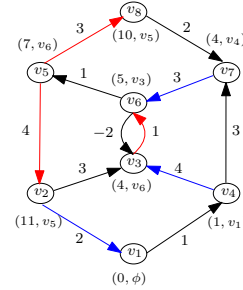
Iteration 2



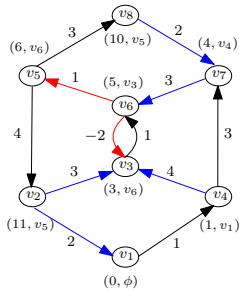
Iteration 3



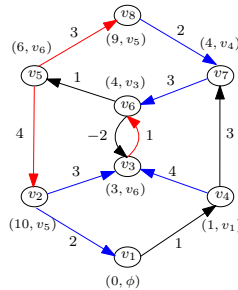
Iteration 4



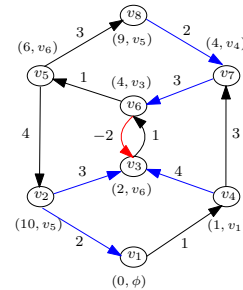
Iteration 5



Iteration 6



Iteration 7



Iteration 8

In the iteration $|V| = 8$, we observe an update of distance estimate due to edge relaxation.

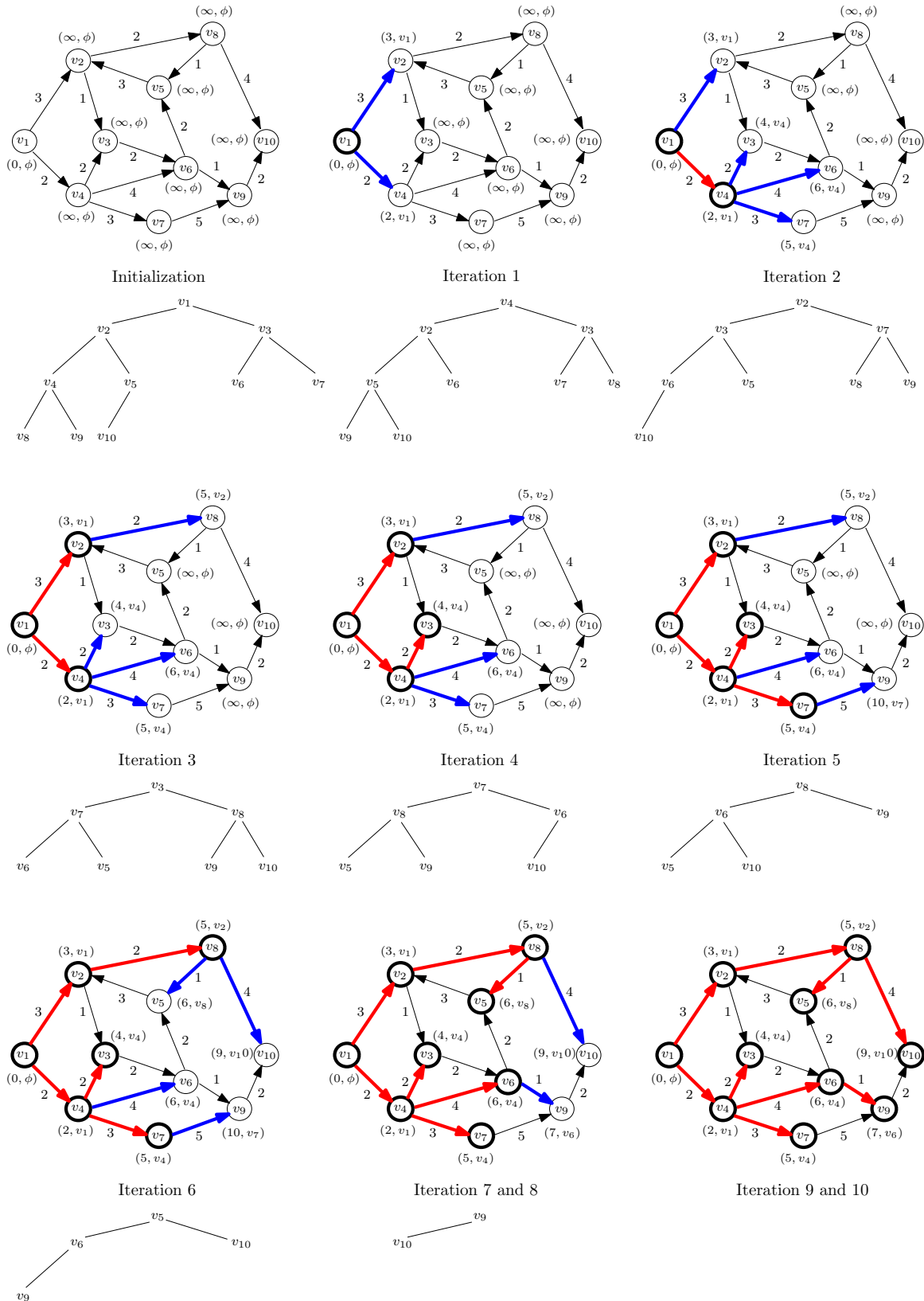
In other words, we have a negative weight cycle.

Solution to Problem 2: Dijkstra's Algorithm

50 points

Data Structure: Min. Priority Queue implemented using min-heaps

Node Attributes: (*distance_estimate*, *parent*)



Bonus Problem (10 points): Implement Dijkstra's algorithm on graphs represented as adjacency lists in Python, and validate your code on the example graph given in Problem 2.

Solution: Code is not included in this solution set.