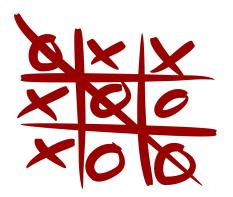
Topic 0: Course Introduction



What is Game Theory?

- ► Mathematical framework that models interactions between selfish (strategic) agents.
- Distributed Artificial Intelligence (AI): Multiple agents with potentially non-identical rationalities and motives perform autonomous actions.
- ► The final outcome depends on all the agents' actions.

Game theory focuses on analyzing the final outcome.

On the other hand, mechanism design focuses on designing systems where selfish agents converge to a desired outcome.

Charles Waldegrave presents a minimax mixed strategy solution to a twoperson version of the card

1838 Antoine Augustin Cournot presents a solution flater known as Nash equilibrium) to a market duopoly.

1913 Ernest Zermelo proved that the ontimal chess strategy is strictly determined.

1928 Birth of Game Theory: John Von Neumann publishes a paper titled On the Theory of Games of Strategy for continuous strategy spaces.

1938 Emile Borel proved a person zero-sum matrix games, when the payoff matrix is symmetric.

John Von Neumann and Oskar Morgenstern coauthors a seminal book titled Theory of Games and Francmic Rehavior

The second edition of Theory of Games and Economic Behavior was published, which

1950-51 John Nash proposes a new

solution (later known as Nash equilibrium for nperson games, Merrill Flood and Melvin Dresher investigates Prisoner's Dilemma in RAND Corp.

1950s Lloyd Shapley studies the value of n-person games, investigates stochastic games. Later, in early

game le Her.















A Brief History of Game Theory





1960s

Thomas Schelling studies bargaining and introduces the notion of conflict. John C. Harsanvi studies Bayesian games. Reinhard Selten introduced the concept of subgame perfect equilibrium.

1970s

Robert I. Aumann studies repeated games, and defines correlated equilibrium, John Maynard Smith introduces evolutionary stable strategies. Leonid Hurwicz studies incentive compatibility in mechanism design.

1980s

Robert Axelrod wrote computer programs for tit-for-tat game tournaments. Eric Maskin studied incentives and dynamic markets. Roger Myerson discovered the connection between ontimal allocations and

truthful revelation.



1994

John Nash, Reinhard Selten and John Harsanvi won the Nobel Prize.

1990s

Noam Nisan and Amir Ronen have studied algorithmic mechanism design. Elias Koutsoupias and Christos H. Papadimitriou introduced the concept of price of anarchy and studied selfish behavior amonost

Internet users.

2000s

Constantinos Daskalakis and Christos H. Papadimitriou studied the computational complexity of finding Nash equilibrium Tim Roughgarden and Eva Tardos studies price of anarchy and Braess' paradox in selfish routing



2007 Leonid Hurwicz, Eric Maskin and Roger Myerson won the Nobel prize.



Koutsoupias, Christos

Papadimitriou, Noam

Nisan, Amir Ronen, Tim

Roughgarden and Eva

Tardos won the Godel

Prize.

2012

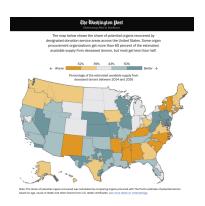
2018 Constantinos Daskalakis won the Rolf Nevanlinna Prize

Application 1: Economics and Finance





Application 2: Government & Policy Making



Source: Washington Post1

EVERYTHING YOU NEED TO KNOW ABOUT TRUMPONOMICS

The upper right-hand corner is traditional Republican territory, but what Trump proposes borrows from a number of political camps.



Source: Fortune²

¹ https://www.washingtonpost.com/graphics/2018/national/organ-transplant-shortages/?noredirect=on

² https://fortune.com/2016/08/11/trumponomics-chart/ Sid Nadendla (CS 5001: Game Theory for Computing)

Application 3: Transportation



Application 4: E-Commerce

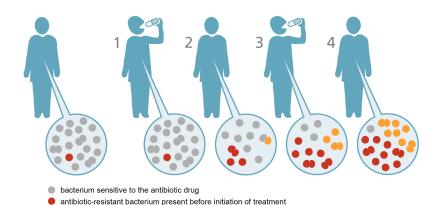


Application 5: Personalization & Targeted Ads





Application 6: Population Dynamics and Evolutionary Biology



antibiotic-resistant bacterium appearing during treatment (by mutation)

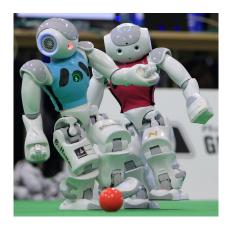
Sid Nadendla (CS 5001: Game Theory for Computing)

Application 7: Airport Security



and many more...

In this course, we will focus³ on...



How do emotionless geniuses play games?

— Colin F. Camerer

³This course is not about designing video games!

However, in the real world...

Most practical agents (including people) have limitations, emotions and biases. Such players are known as *boundedly rational* agents. The study of game theory in the presence of boundedly rational agents is called *behavioral game theory*, which is out of the scope of this course.



Prerequisites

- ► Linear Algebra
 - Matrices to organize choice information at competing agents.
 - Matrix operations/reductions (e.g. simplex algorithm) to make informed decisions.
- ► Probability Theory and Statistics
 - ► Account for randomized actions at competing agents.
 - Compute the average outcome of the interaction.
- ► Algorithms
 - ► Implement AI-based agents
 - ► Compute the final outcome (solution) algorithmically.
- Calculus
 - ► Game ⇒ Minimax (saddle-point) solutions.
 - ► Optimization theory??? (no need for this course, but a very powerful tool!)

Textbook Information

This course has **no** single textbook.

Instead, we will follow multiple reference books, some being listed below:

- ▶ Roger B. Myerson, "Game Theory: Analysis of Conflict," Harvard University Press, 1991.
- ▶ Drew Fudenberg, Jean Tirole, "Game Theory," MIT Press, 1991.
- ► Tamer Başar and Geert Jan Olsder, "Dynamic Noncooperative Game Theory," SIAM, 2nd Ed., 1999.
- ▶ Martin J. Osborne, "An Introduction to Game Theory," Oxford University Press, 2003.
- Noam Nisan et al. (Editors), "Algorithmic Game Theory," Cambridge University Press, 2007.
- John von Neumann and Oskar Morgenstern, "Theory of Games and Economic Behavior," 60th Anniversary Commemorative Edition, Princeton University Press, 2007.
- Yoav Shoham, Kevin Leyton-Brown, "Multiagent Systems: Algorithmic, Game-Theoretic, and Logical Foundations," Cambridge University Press, 2008.
- Herbert Gintis, "Game Theory Evolving: A Problem-Centered Introduction to Modeling Strategic Interaction," Princeton University Press, 2nd Ed., 2009.
- David Easley and Jon Kleinberg, "Networks, Crowds and Markets: Reasoning about a Highly Connected World," Cambridge University Press, 2010.

Resources Available for Free...

S&T Digital Library:

- ► Roger B. Myerson, "Game Theory: Analysis of Conflict," Harvard University Press, 1991.
- Samson Lasaulce and Hamidou Tembine, "Game Theory and Learning for Wireless Networks," Academic Press, 2011.
- ► Harold W. Kuhn, "Lectures on the Theory of Games," Annals of Mathematics Studies (Book 166), Princeton University Press, 2003.

Publishers:

- Noam Nisan et al. (Editors), "Algorithmic Game Theory," Cambridge University Press, 2007.
- Yoav Shoham, Kevin Leyton-Brown, "Multiagent Systems: Algorithmic, Game-Theoretic, and Logical Foundations," Cambridge University Press, 2008.
- David Easley and Jon Kleinberg, "Networks, Crowds and Markets: Reasoning about a Highly Connected World," Cambridge University Press, 2010.

Links to free digital copies of these books can be found on the course website for personal use!

Topics

This course is broadly divided into 6 topics:

- ► **Topic 0**: *Introduction* (1 lecture)
- ► **Topic 1**: *Decision Theory* (3 lectures)
- ► Topic 2: Basic Models (6 lectures)
- ► Topic 3: Dynamic Games (5 lectures)
- ► **Topic 4:** *Mechanism Design* (4 lectures)
- ► **Topic 5**: *Coalitional Games* (3 lectures)
- ► Topic 6: Advanced Solution Concepts (3 lectures)

Tentative Plan

- ► Submit assignments in two weeks on GitLab⁴.
- ► Programming language: Python
- ► In-class quizzes on CANVAS.
- ► In-class midterm exams⁵.
- ▶ Project-update presentation at the end of Topic 5.
- Project presentations during the last week of classes, and a report due by last day of classes.
- ► Grades calculated based on

Туре	Grade
Assignments (Top-4 of HWs 1-5 + HW 6)	40% of total grade
Midterm Exams (2)	30% of total grade
Quizzes (Top-4 of Quizzess 1-5 + Quiz 6)	10% of total grade
Project (1)	20% of total grade
Final Grade for Undergrad Students	[85 $-$ 100]: A, [75 $-$ 85): B, [60 $-$ 75): C, [50 $-$ 60): D, $<$ 50: F
Final Grade for Grad Students	[85 $-$ 100]: A, [75 $-$ 85): B, [60 $-$ 75): C, $<$ 60: F

⁴Detailed instructions regarding GitLab are provided on instructor's website

⁵Take home if in-person classes are suspended