

Homework 4: Graph Algorithms: Part I

Instructor: Sid Nadendla

Due: April 22, 2022

In this homework, we will focus our attention to searching on graphs and finding minimum spanning trees.

Problem 1: Graph Traversal

50 points

1. Demonstrate both breadth-first search (BFS) and depth-first search (DFS) algorithms (with v_5 as the start node) on the graph shown in Figure 1. Clearly show how each node-attribute (including frontier) changes in each iteration in both the algorithms. (20 points)
2. Implement both BFS and DFS algorithms in Python using adjacency list representation for the graph, and demonstrate it on the example graph shown in Figure 1. (30 points)

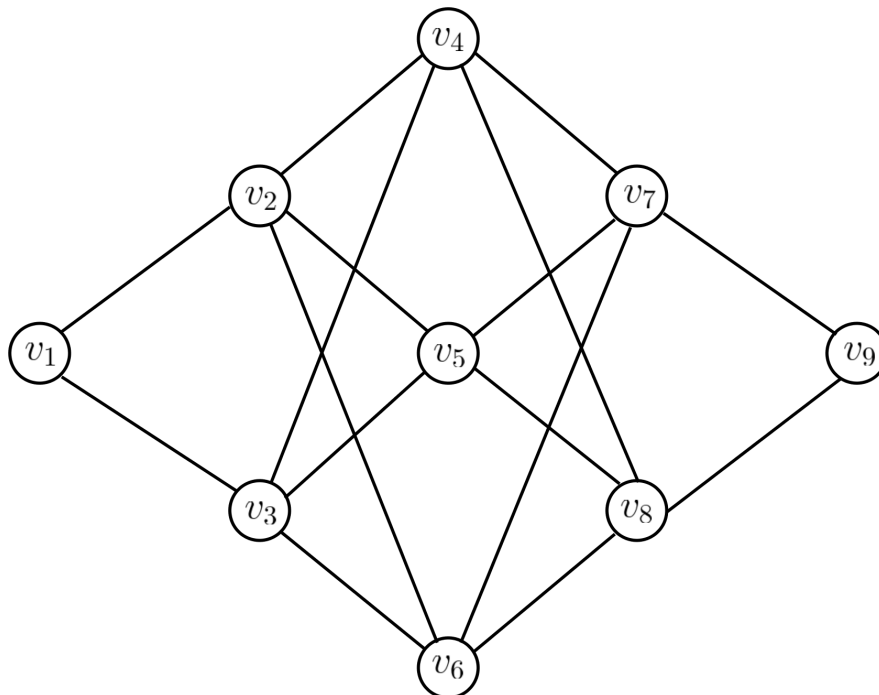


Figure 1: Example Graph for Search Algorithms

Problem 2: Minimum Spanning Trees**50 points**

1. Demonstrate both Kruskal's and Prim's algorithm (with vertex v_1 as the start node) for the Petersen graph shown in Figure 2. (20 points)
2. Implement Prim's algorithm in Python using adjacency matrix representation of a graph, and demonstrate it on the Petersen graph shown in Figure 2. (15 points)

Bonus Problem (10 points):

- Implement Kruskal's algorithm in Python with the disjoint set data structure using adjacency list representation, and demonstrate it on the graph in Figure 2.

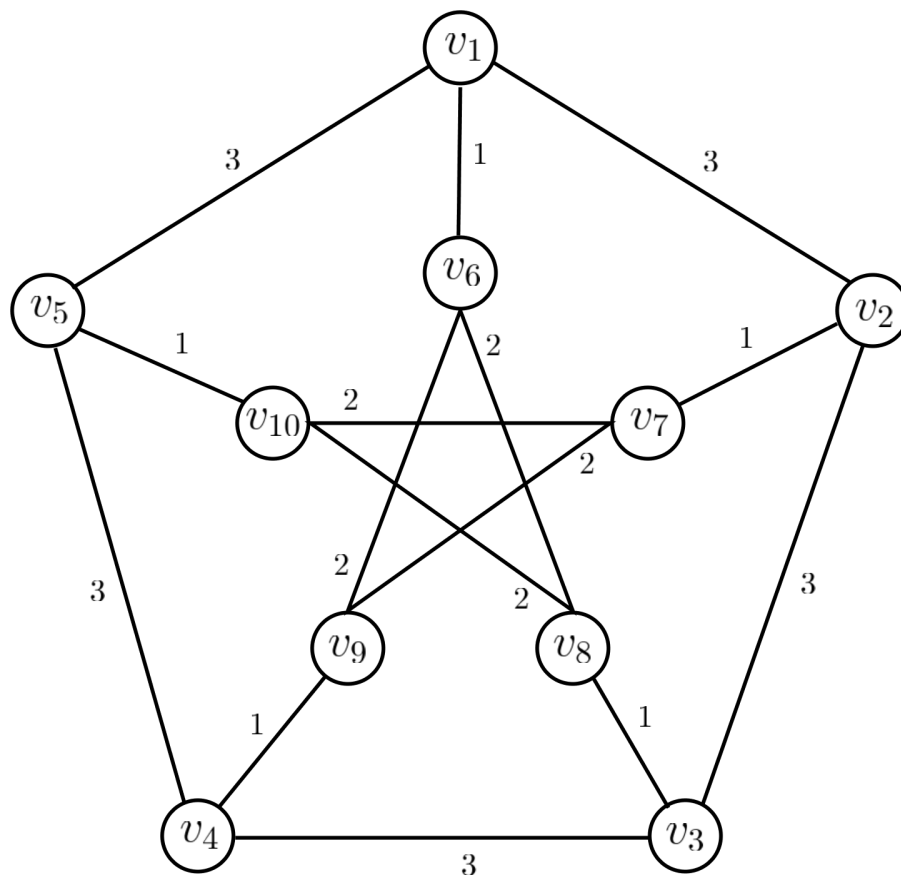


Figure 2: Petersen Graph