Department of Computer Science CS 2500: Algorithms

Sample Questions for Exam 2

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This handout presents a few review questions for Midterm 2 on April 28, 2022. Midterm 2 will be 1.5-hour long in-class exam with about 2-3 questions.

Section 1: Dynamic Programming

1. Consider a 0-1 Knapsack problem with n indivisible items, where v_i and w_i are the value and weight of the i^{th} item respectively. If the size of the Knapsack is W, show that the Bellman equation is

$$V[i,j] = \min_{x_i \in \{0,1\}} v_i x_i + V[i-1,j-x_i w_i], \text{ for all } i = 1, \dots, n \text{ and } j = 0, 1, \dots, W,$$

and write the pseudocode for the dynamic programming solution to 0-1 Knapsack problem.

2. Consider a matrix chain multiplication $A_1 \cdot A_2 \cdots A_n$, where A_i is a $p_{i-1} \times p_i$ matrix. IF the cost of computing the product of $k \times \ell$ and $\ell \times m$ matrices is $k\ell m$, show that the Bellman equation is

$$m[i,j] = \begin{cases} m[i,k] + m[k+1,j] + p_{i-1}p_kp_j, & \text{if } i > j \\ 0, & \text{otherwise.} \end{cases}$$

Using the above Bellman equation, write a pseudocode for the dynamic programming algorithm for matrix-chain multiplication problem.

Section 2: Greedy Algorithms

- 1. When can a greedy algorithm produce an optimal solution?
- 2. Demonstrate on the following example, how to find an optimal solution to the Fractional Knapsack problem using a greedy algorithm?

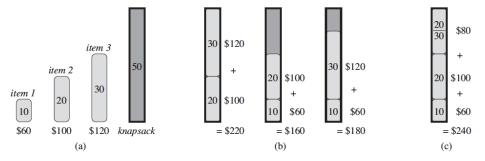


Figure 1: Fractional Knapsack

Section 3: Graph Search/Traversal

- 1. Demonstrate Breadth-first search (BFS) on a graph, such as the one shown in Figure 2.
- 2. Demonstrate Depth-first search (DFS) on a graph, such as the one shown in Figure 2.
- 3. What is the main difference between the implementation of BFS and DFS algorithms?

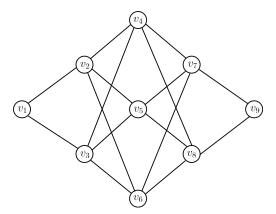


Figure 2: Graph Search

Section 4: Minimum Spanning Trees

- 1. Demonstrate Kruskal's algorithm on the graph, such as the one shown in Figure 3.
- 2. Demonstrate Prim's algorithm on the graph, such as the one shown in Figure 3.
- 3. Explain why dynamic programming is not a good approach to find minimum spanning trees?
- 4. State the primary difference between Kruskal's and Prim's algorithms?

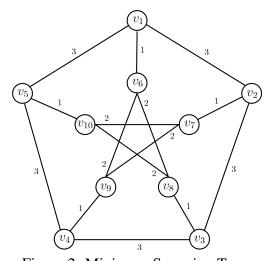


Figure 2: Minimum Spanning Trees