



INDIAN INSTITUTE OF TECHNOLOGY ROPAR
CSL603

Decision Tree Learning

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1 Decision Tree Model and Analysis

This is Report for Decision Tree Learning through Algorithm ID3. In this Assignment we have to Classify Movie Reviews using Word Sentiments as Features taken from <http://ai.stanford.edu/amaas/data/sentiment/index.html>.

I have Sampled 1000 random subset from Train Data Set and Test Data Set and Selected top 2500 positive sentiment Attributes and bottom 2500 negative sentiments Attributes and created Feature vector in TrainSet.txt and TestSet.txt and selected Features in selected-features-indices.txt . All the Results for Analysis and Accuracy has been Discussed below.

2 Basic Analysis of Decision Tree Created

This Analysis is conducted for Binary Splitting of Nodes and Selection of Attribute on basis of Information Gain.

Formulas Used for calculation of Entropy and Information Gain :

Let Entropy = E and p_i = Probability of i^{th} class.

$$E = \sum_{i=1}^c p_i * \log(p_i)$$

Let Information Gain w.r.t to A = Gain(S,A)

$$Gain(S, A) = Entropy(S, A) - \sum_{i=1}^v \frac{|S_i|}{|S|} * Entropy(S_i, A)$$

$$WeightedEntropy(S, A) = \sum_{i=1}^v \frac{|S_i|}{|S|} * Entropy(S_i, A)$$

$$AttributeSelection = \min_{\forall A_i \in A} WeightedEntropy(S, A_i)$$

2.1 Accuracy and Analysis for Decision Trees

Early stopping Criteria Used are :

1. Weighted Entropy :- 6th Column Corresponds to stopping Criteria on Entropy to Train model.
2. Height of Tree :- 7th Column corresponds to Height as stopping criteria.
 - 2.a Max Height = 180 for 5000 Attributes
 - 2.b Max Height = 100 for 3000 Attributes
 - 2.c Max Height = 40 for 2000 Attributes

| | Sample | Train Acc | Test Acc | Height | Weighted Entropy | Stopping Height |
|-------------------|--------|-----------|----------|--------|-------------------|-----------------|
| Attributes = 5000 | 1 | 89.1 | 73.8 | 216 | $\leq 0.1 - 75.0$ | 73.8 |
| | 2 | 89.9 | 71.2 | 208 | $\leq 0.2 - 71.8$ | 72.0 |
| | 3 | 87.1 | 67.0 | 221 | $\leq 0.3 - 71.3$ | 67.0 |
| | 4 | 89.6 | 68.7 | 216 | $\leq 0.4 - 72.4$ | 69.0 |
| Attributes = 3000 | 1 | 82.9 | 73.8 | 148 | $\leq 0.1 - 73.9$ | 73.8 |
| | 2 | 84.0 | 73.6 | 157 | $\leq 0.2 - 74.1$ | 73.9 |
| | 3 | 83.4 | 69.3 | 153 | $\leq 0.3 - 69.3$ | 69.3 |
| | 4 | 83.3 | 70.3 | 158 | $\leq 0.4 - 71.7$ | 70.3 |
| Attributes = 2000 | 1 | 75.4 | 69.3 | 104 | $\leq 0.1 - 69.3$ | 68.4 |
| | 2 | 74.2 | 70.6 | 103 | $\leq 0.2 - 71.1$ | 69.4 |
| | 3 | 76.6 | 69.4 | 116 | $\leq 0.3 - 69.4$ | 68.8 |
| | 4 | 75.9 | 70.0 | 122 | $\leq 0.4 - 70.0$ | 69.3 |

| 5000 Attributes | | 3000 Attributes | | 2000 Attributes | |
|-----------------|-----------|-----------------|-----------|-----------------|-----------|
| words | Frequency | words | Frequency | words | Frequency |
| poor | 10 | avoid | 8 | pathetic | 5 |
| avoid | 6 | terrible | 5 | garbage | 5 |
| dull | 6 | poorly | 5 | crap | 5 |
| horrible | 6 | laughable | 5 | terrible | 5 |
| terrible | 5 | insult | 5 | costs | 4 |
| poorly | 5 | mess | 5 | waste | 3 |
| dumb | 5 | trash | 5 | unfunny | 3 |
| disgusting | 5 | stupid | 4 | insulting | 3 |
| painful | 5 | horrible | 4 | appalling | 3 |
| wasted | 4 | lame | 4 | sucks | 3 |

2.2 Accuracy and Analysis for Decision Trees after Addition of Noise

In this step of Analysis Various percent of noise are added. Train Data Labels are randomly changed. Various Observation are Observed as follows :

- Height of Tree remains or small increase is observed. As Decision Tree is robust for noise. But due to noise it may overfit the data and reduce accuracy on test set.
- Due to bias partition on attribute value less data may be misclassified. So height changes very small.

| | | Sample | Before Adding Noise | | | After Adding Noise | | |
|--------------|-------------------|--------|---------------------|------------|--------|--------------------|------------|--------|
| | | | Training Error | Test Error | Height | Training Error | Test Error | Height |
| Noise = 0.5% | Attributes = 5000 | 1 | 88.7 | 71.3 | 204 | 88.3 | 71.1 | 204 |
| | | 2 | 88.7 | 67.7 | 189 | 88.4 | 67.6 | 189 |
| | Attributes = 3000 | 1 | 83.5 | 73.2 | 159 | 83.1 | 73.3 | 164 |
| | | 2 | 82.6 | 71.7 | 151 | 82.6 | 71.7 | 151 |
| | Attributes = 2000 | 1 | 76.5 | 70.1 | 135 | 76.3 | 69.9 | 135 |
| | | 2 | 76.4 | 67.9 | 129 | 76.4 | 67.9 | 129 |
| Noise = 1% | Attributes = 5000 | 1 | 89.4 | 67.9 | 225 | 89.0 | 68.3 | 222 |
| | | 2 | 88.7 | 66.8 | 196 | 87.7 | 65.6 | 193 |
| | Attributes = 3000 | 1 | 81.9 | 72.0 | 149 | 81.6 | 71.6 | 153 |
| | | 2 | 83.0 | 68.4 | 170 | 82.6 | 68.4 | 170 |
| | Attributes = 2000 | 1 | 75.2 | 68.5 | 104 | 74.9 | 68.5 | 104 |
| | | 2 | 78.6 | 66.7 | 138 | 78.5 | 66.9 | 138 |
| Noise = 10% | Attributes = 5000 | 1 | 89.8 | 71.1 | 181 | 84.3 | 70.3 | 200 |
| | | 2 | 90.3 | 68.2 | 194 | 83.6 | 67.3 | 212 |
| | Attributes = 3000 | 1 | 84.0 | 70.7 | 153 | 79.9 | 68.5 | 157 |
| | | 2 | 83.7 | 72.0 | 154 | 80.3 | 71.2 | 150 |
| | Attributes = 2000 | 1 | 77.2 | 70.4 | 125 | 75.1 | 70.3 | 125 |
| | | 2 | 75.9 | 70.8 | 121 | 73.7 | 70.1 | 125 |

3 Pruning of Trees

In this step of Analysis we Use Post-Pruning Strategy to learn the Tree. In Post-Pruning we learn decision tree without Early Stopping and Prune Tree to get Optimal Solution of Tree. For Different number of Attributes Observations are :

- With Pruning Height of Tree Decreases considerably.
- Accuracy on Test Data Increases and Training Error is constant or increases.
- Observation has been Absorbed on various samples and on different attributes.

| | Sample | Without Pruning | | | With Pruning | | |
|-------------------|--------|-----------------|----------|--------|--------------|----------|--------|
| | | Train Acc | Test Acc | Height | Train Acc | Test Acc | Height |
| Attributes = 5000 | 1 | 88.5 | 68.8 | 209 | 88.5 | 72.0 | 89 |
| | 2 | 88.7 | 67.2 | 207 | 88.7 | 68.5 | 95 |
| | 3 | 89.6 | 71.2 | 197 | 89.6 | 71.8 | 94 |
| | 4 | 89.8 | 69.5 | 216 | 89.8 | 73.8 | 87 |
| Attributes = 3000 | 1 | 85.0 | 72.1 | 141 | 85.0 | 72.1 | 71 |
| | 2 | 82.7 | 73.5 | 160 | 82.7 | 75.0 | 76 |
| | 3 | 83.4 | 71.5 | 190 | 83.4 | 72.0 | 81 |
| | 4 | 83.1 | 69.5 | 159 | 83.1 | 72.1 | 80 |
| Attributes = 2000 | 1 | 77.0 | 68.9 | 128 | 77.0 | 69.3 | 115 |
| | 2 | 75.9 | 69.0 | 114 | 75.9 | 69.3 | 57 |
| | 3 | 77.0 | 71.8 | 112 | 77.0 | 71.8 | 63 |
| | 4 | 76.3 | 66.7 | 111 | 76.3 | 66.8 | 67 |

4 Feature Bagging

In this step of Analysis we Randomly select some number of Attributes and Train model of Decision Tree as Number of Trees as Parameter. Various Observation are as follows :

- In feature Bagging we are selecting 2000 attributes Randomly So Decision Tree may not get well train.
- As Tree number increases Accuracy increases as more Trees are trained and classified well.
- For small number of forest size , accuracy is less than original accuracy.

Number of Attributes Selected = 2000

Before Random Forest Training Accuracy = 89.4

Before Random Forest Testing Accuracy = 68.6

| No. of Trees | Training Accuracy | Testing Accuracy |
|--------------|-------------------|------------------|
| 5 | 79.8 | 68.3 |
| 10 | 78.3 | 67.6 |
| 20 | 81.2 | 69.0 |
| 30 | 82.1 | 69.2 |
| 50 | 84.0 | 71.0 |