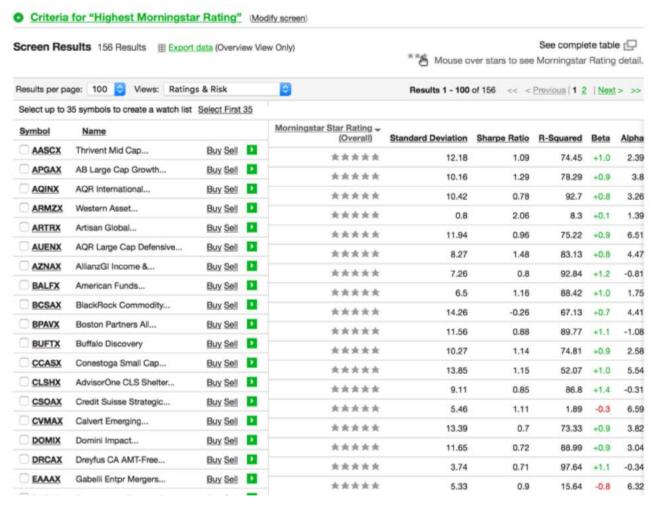
# VaR analysis for Mutual Funds

**Siddharth Chakravarty** 

## Morningstar Rating process



- Introduced in 1985
- Rating based on a scale of 1-5 stars
- Evaluates how the fund has performed adjusting for risk and cost compared to funds in the same category
- Separate ratings for 3,5 and 10 years which combined into an overall rating
- Ratings are graded on a curve
  - ✓ Top 10% 5 stars
  - ✓ Bottom 10% 1 star
- Based entirely on a mathematical evaluation of past performance
- Publishes Analyst rating which is forward looking

### **KEY POINTS – Measures of Risk**

- There is no general agreement, however, about how best to measure and compare fund performance and on what information funds should disclose to investors.
- Firms face many different kinds of risks, including market risks, credit risks, liquidity risks, operational risks and legal risks.
- VaR is perhaps the most well-known risk measure. It is a single estimate of the amount by which an institution's position in a risk category could decline because of general market movements during a given holding period
- A VAR statistic has three components:
  - 1. A time period
  - 2. A confidence level
  - 3. Loss amount (or loss percentage).

Keep these three parts in mind as I give some examples of variations of the question that VAR answers:

## Risk approaches

#### Traditional

- Mean variance monthly data 10/31/2017 (5 year)
  - 1. Sharpe ratio risk adjusted return compared risk/reward per unit of risk
  - 2. Alpha Excess return
  - 3. Beta Market risk

#### VaR

- 1. Normal assumes normal distribution
- 2. Historical VaR
- 3. Extreme Value Var (General pareto distribution)
  - Block Maxima approach
  - Peak over threshold
- 4. Monte Carlo Simulation VaR

#### **FUND SELECTION**

#### Oppenheimer Global Opportunities A OPGIX | ★★★★★



Morningstar Analyst Rating

1-Day Total Return \$69.68 **↑**0.35%

USD | NAV as of 30 Nov 2017 | 1-Day Return as of 30 Nov 2017

TTM Yield 0.18%	<b>Total Assets</b> \$ 6.9 bil	 Fee Level Below Average	Turnover 18%	Status Open	Min. Inv. \$ 1,000

III Mid Growth

World Small/Mid Stock

#### Asset Allocation OPGIX



Sector Weightings OPGIX		
	% Stocks	
<b>∱</b> Cyclical		
🟯 Basic Materials	1.13	
Consumer Cyclical	16.39	
Financial Services	2.90	
neal Estate	1.52	
<b>✓</b> Sensitive		
Communication Services	0.44	
Energy	0.00	
Industrials	12.06	
Technology	32.53	

#### - Defensive

Consumer Defensive	3.40
Healthcare	29.63
Utilities	0.00

As of 10/31/2017

### **FUND SELECTION**

#### T. Rowe Price Growth Stock PRGFX | ★★★★★

Morningstar Analyst Rating

NAV 1-Day Total Return \$71.38 **↑**1.00%

USD | NAV as of 30 Nov 2017 | 1-Day Return as of 30 Nov 2017

TTM Yield	Load	Total Assets	Expenses	Fee Level	Turnover	Status	Min. Inv.
0.06%	None	\$ 52.7 bil	0.68%	Below Average	44%	Open	\$ 2,500
30-Day SE	C Yield	Category Large Growt	h	Investment Style  Investment Style  Large Growth			

#### Asset Allocation PRGFX



Sector Weightings PRGFX		
	% Stocks	
<b>↓</b> Cyclical		
🔝 Basic Materials	0.00	
Consumer Cyclical	18.12	
Financial Services	13.74	
Real Estate	0.40	
Communication Services  Energy	3.65 0.00	
Energy	0.00	
Industrials	12.06	
Technology	30.24	
→ Defensive		
Consumer Defensive	3.24	
Healthcare	17.72	
Utilities	0.82	

#### **FUND SELECTION**

#### Fidelity® Select Semiconductors FSELX | ★★★★

FF Fund Family Data 🛗 Add to Portfolio Get E-mail Alerts 🗏 Print This Page 🗐 Data Definition ? Data Question

1-Day Total Return \$126.36 \(\daggered{\pi}0.52\)\footnote{1.52} 30-Day SEC Yield

USD | NAV as of 30 Nov 2017 | 1-Day Return as of 30 Nov 2017

None

**Total Assets** \$ 3.4 bil

Technology

Category

Expenses Fee Level Low

110%

Min. Inv. \$ 2,500

**Investment Style** III Large Growth

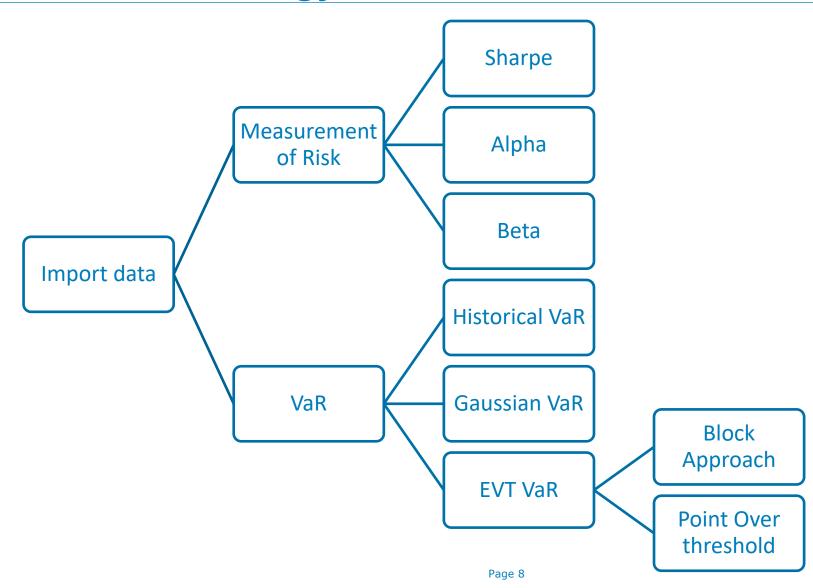
#### **Asset Allocation FSELX**



Sector Weightings FSELX				
	% Stocks			
<b>1</b> Cyclical				
🔝 Basic Materials	0.00			
Consumer Cyclical	0.00			
Financial Services	0.00			
Real Estate	0.00			
₩ Sensitive				
Communication Services	0.00			
Energy	0.00			
Industrials	0.00			
Technology	100.00			
→ Defensive				
Consumer Defensive	0.00			
Healthcare	0.00			
Utilities	0.00			

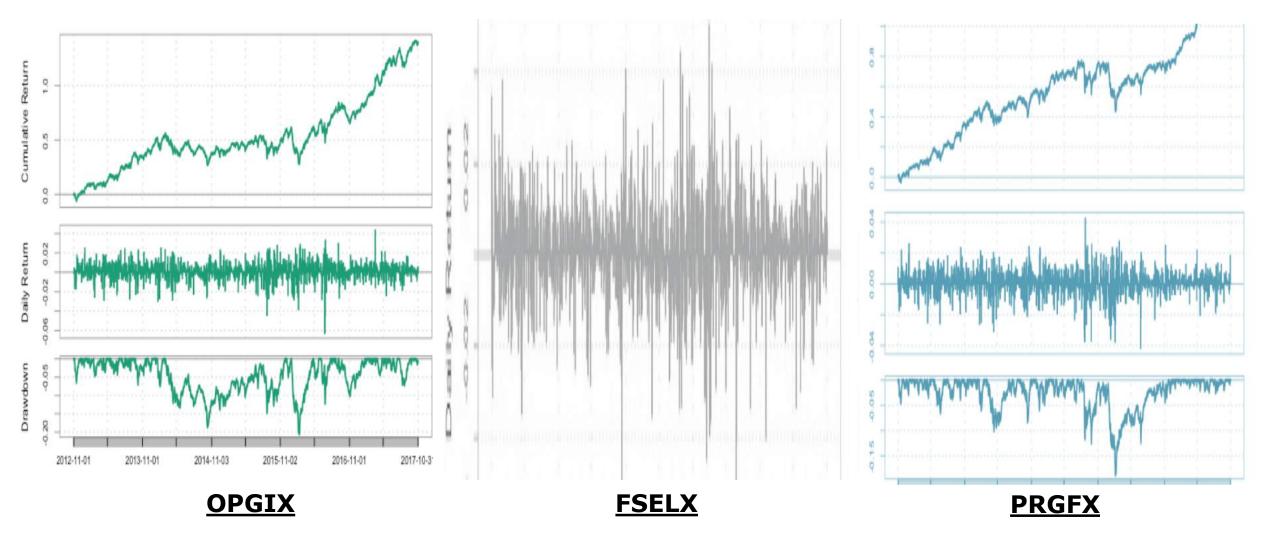
Sector Weightings ESELV

## Our Methodology

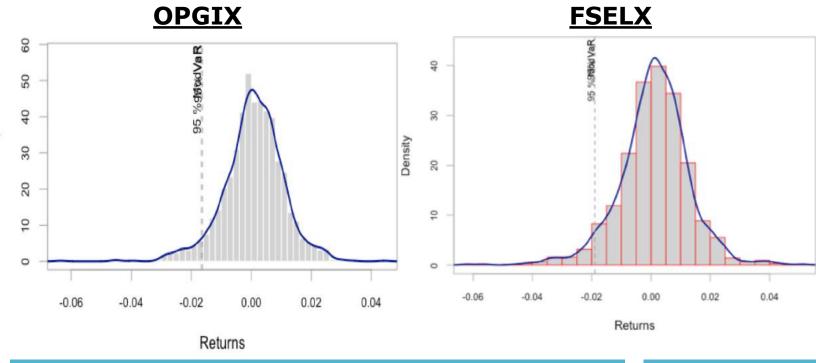


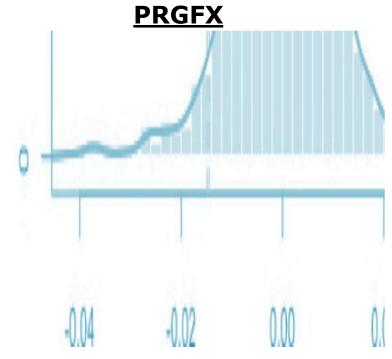
- Key R Packages used for analysis
  - library(xts)
  - library(timeSeries)
  - library(tseries)
  - library(TTR)
  - library(quantmod)
  - library(PerformanceAnalytics)
  - library(extRemes)
  - library(fExtremes)
  - library(evd)
  - library(ismev)
  - library(evir)
  - library(POT)

## Historical returns



### Return Distribution

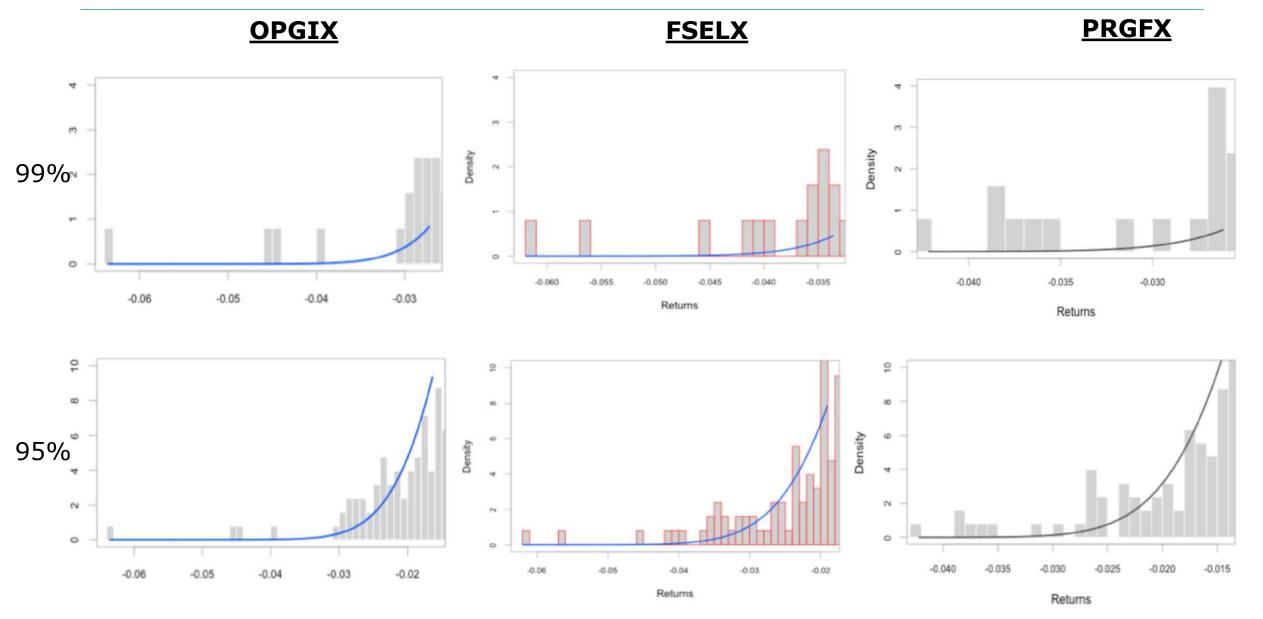




	OPGIX	FSELX	PRGFX
Annualized return	19%	31.53%	18.16%
Sharpe (Rf=1.2%, p=95%)	1.25	1.45	1.5
Alpha	10.8	14.71	4.42
Beta	0.85	1.12	0.69

	OPGIX	FSELX	PRGFX
Kurtosis	2.55	2.27	2.21
Skew	-0.51	-0.34	-0.47
Std. Dev	0.010	0.012	0.009
Mean	0.0007	0.0011	0.0007

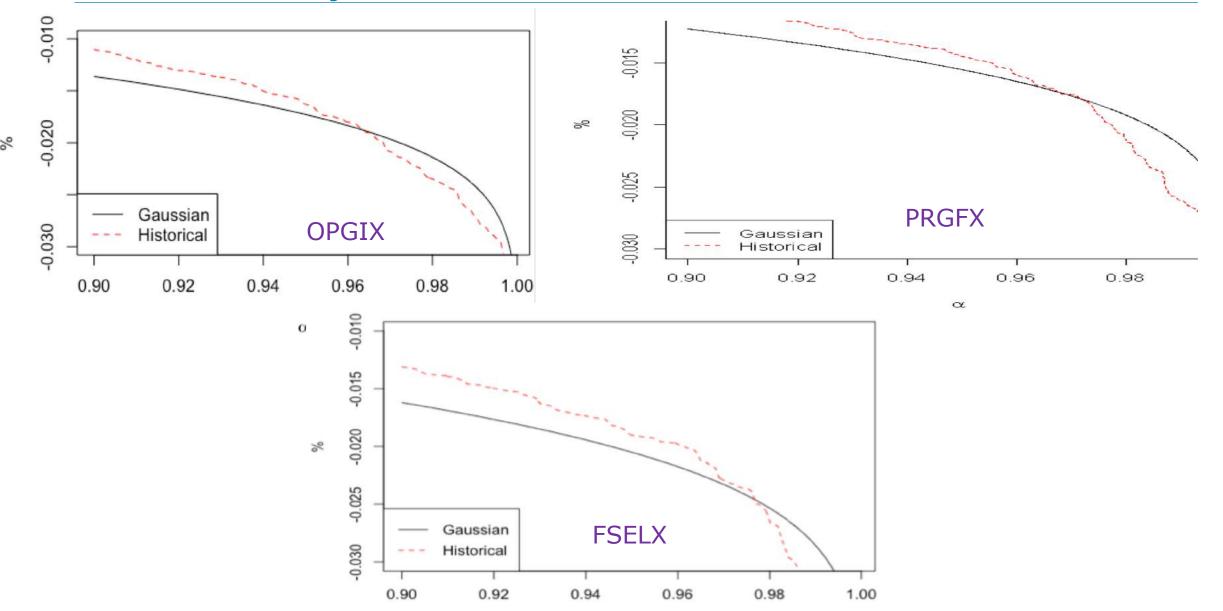
### Tail Distribution at 99% & 95%



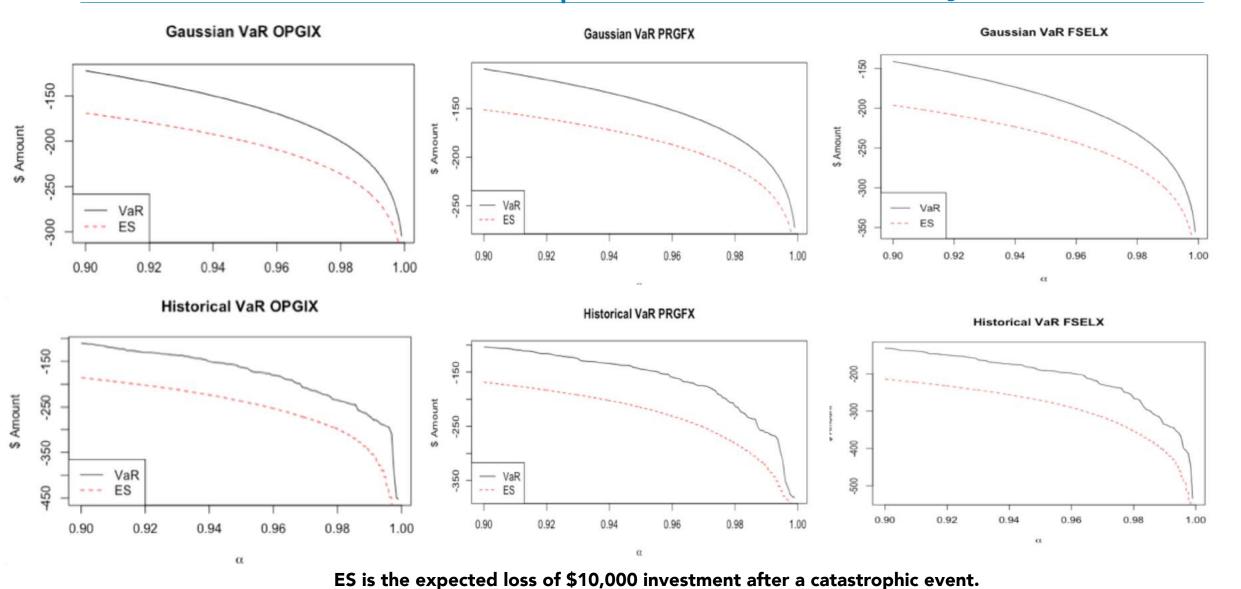
## VaR Analysis

- Value at risk (VaR) is a statistical technique used to measure and quantify the level of financial risk within a firm or investment portfolio over a specific time frame.
- Example:
- What is the most I can with a 95% or 99% level of confidence expect to lose in dollars over the next month?
- What is the maximum percentage I can with 95% or 99% confidence expect to lose over the next year?
- Different methodologies
- Variance/ Covariace
- Monte Carlo simulation
- Historical simulation

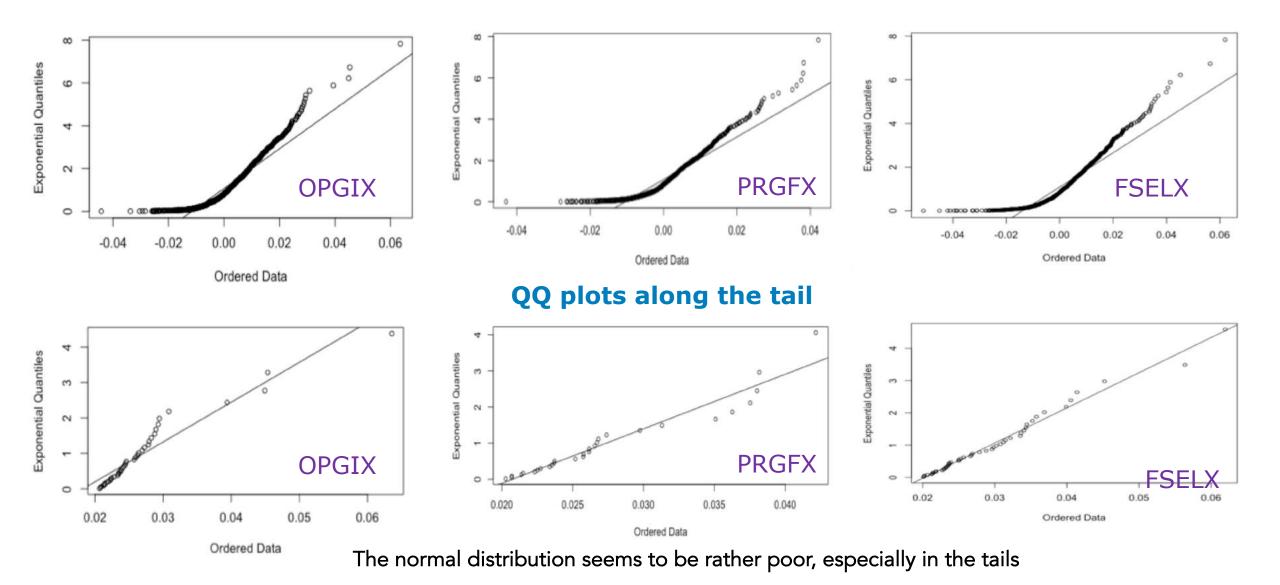
## VaR Sensitivity



# Simulation of Risk and Expected shortfall analysis

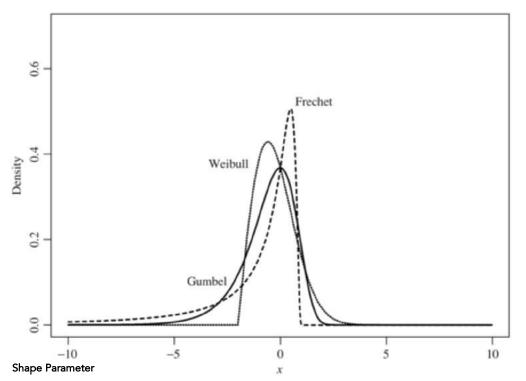


# QQplot – for normality check



### Introduction to EVT

- Standard VaR methods, such as variance-covariance method or historical simulation, can fail when the return distribution is fat tailed.
- This problem is aggravated when long-term VaR forecasts are desired.
- Extreme Value Theory (EVT) is proposed to overcome these problems



- A main objective of the EVT is to make inferences about sample extrema (maxima or minima) .
- In this context the so called Generalized Extreme Value distribution (GEV) and General Pareto distribution play a central role (GPD).

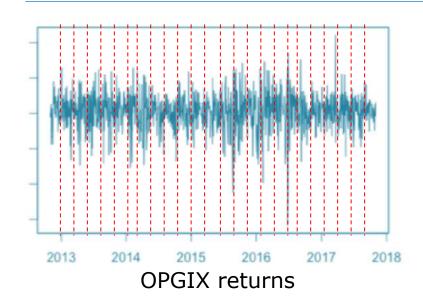
$$\mathsf{GEV}$$
 
$$\xi \neq 0 \qquad G(y) = \exp\left(-\left[1 + \xi\left(\frac{y - \mu}{\sigma}\right)\right]^{-1/\xi}\right)$$
 
$$\xi = 0 \qquad G(y) = \exp\left(-\exp\left(-\frac{y - \mu}{\sigma}\right)\right)$$
 
$$G(y) = \exp\left(-\frac{y - \mu}{\sigma}\right)$$
 
$$G(y) = \exp\left(-\frac{y -$$

 $\xi$ >0 giving the heavy-tailed (Frechet) case

**ξ**<0 giving the bounded-tailed (Weibull) case

 $\xi$ =0 giving the light-tailed (Gumbel) case

### **Block Maxima**



Child Distribution of the blocks

Select the length of the sub period *n* 



Obtain the maximum likelihood estimates of  $\mu$ ,  $\sigma$ , and  $\xi$ 



Check the adequacy of the fitted extreme value model



Apply equation to calculate VaR.

 Block Maxima approach divides the sample into subsamples and applies the EVT to the subsamples. For daily returns, n = 21 corresponds approximately to the number of trading days in a month and n = 63 denotes the number of trading days in a

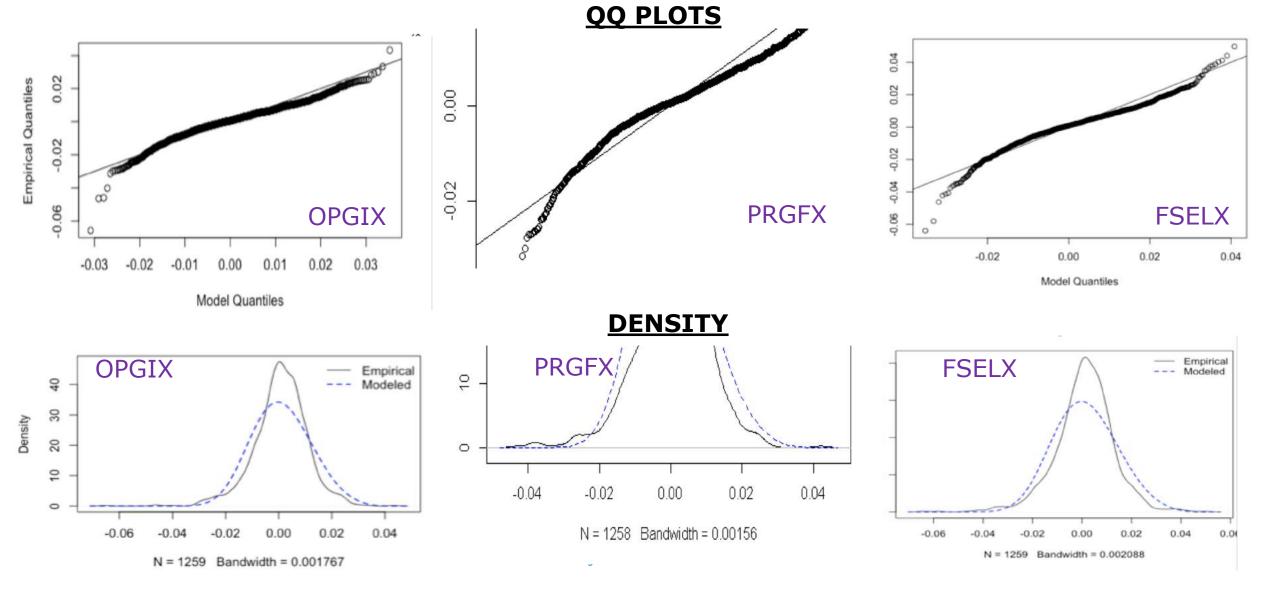
 $\text{VaR} = \begin{cases} \mu_n - \frac{\sigma_n}{\xi_n} \left\{ 1 - \left[ -n \ln(1-p) \right]^{-\xi_n} \right\} & \text{if } \xi_n \neq 0 \\ \mu_n - \sigma_n \ln[-n \ln(1-p)] & \text{if } \xi_n = 0, \end{cases}$ 

The distribution contains three parameters.

- 1. Shape parameter  $\xi$
- Location parameter µ
- 3. Scale  $\sigma$ .

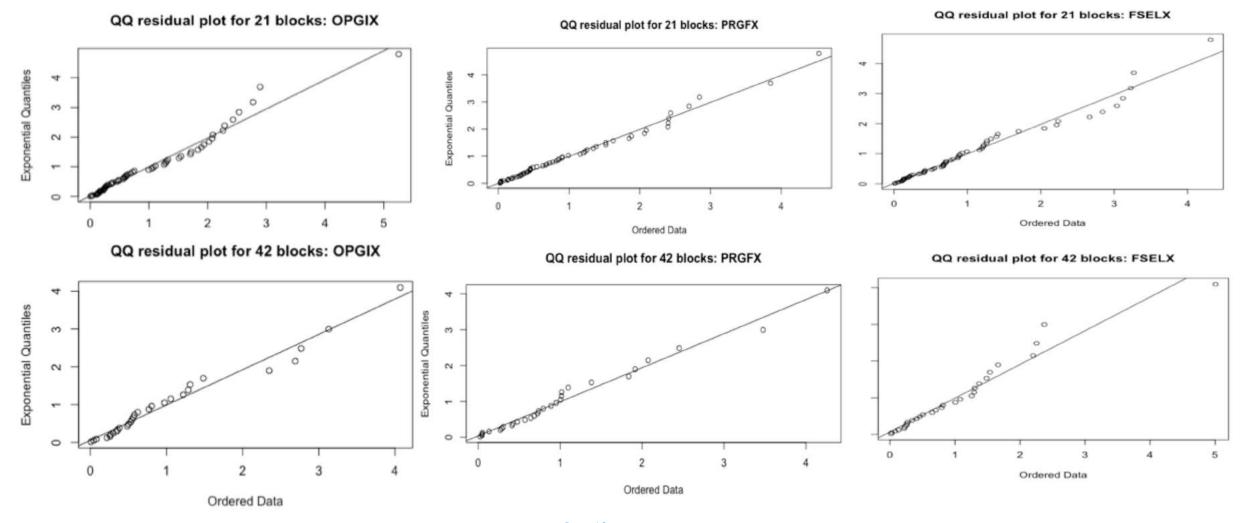
where n is the length of subperiods.

## Fitting to GEV distribution



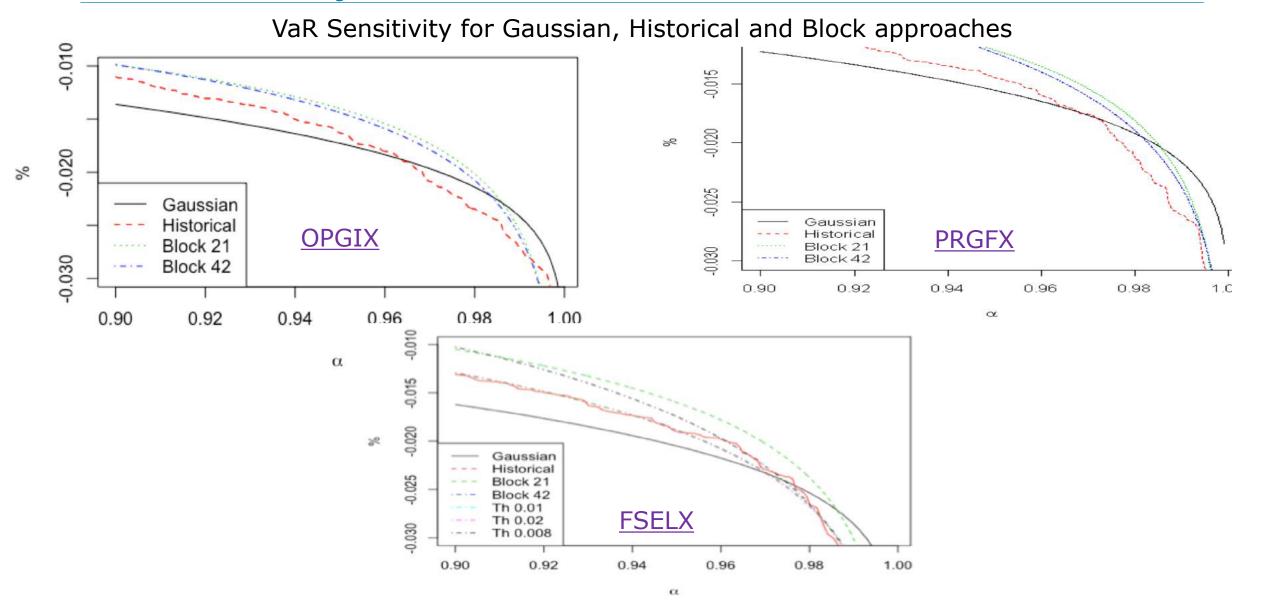
### **BLOCK MAXIMA APPROACH**

Parameter -shape parameter  $\xi$ , the location parameter  $\mu$ , and the scale  $\sigma$ 

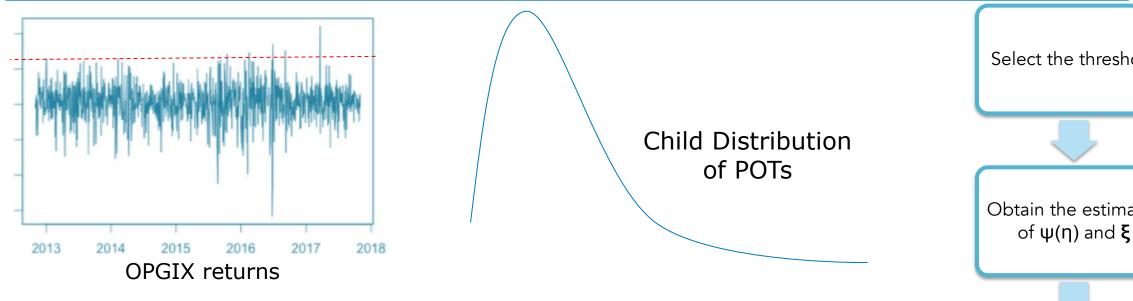


Page 19

## VaR Sensitivity

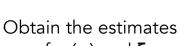


### Peaks over threshold



- The traditional EVT approach to risk calculation encounters some difficulties in the choice of subperiod length *n* is not clearly defined
- POT approach focuses on exceedances of the loss over some high threshold and the times at which the exceedances occur. Different choices of the threshold leads to different estimates of the shape parameter  $\xi$ . The choice of threshold depends on the observed returns.
  - \* For a stable return series,  $\eta = 2.5\%$  may fare well for a long position.
  - $\diamond$  For a volatile return series (e.g., daily returns of a dot-com stock),  $\eta$  may be as high as 10%.

Select the threshold





Check the adequacy of the fitted extreme value model

## Fitting to GPD distribution - OPGIX

Threshold = 0.03, N = 2 Density 1-1 line Empirical 0.0340 regression line Modeled 0.034 95% confidence hand -0.0050.005 0.015 0.034 0.038 0.042 0.035 0.037 0.039 Threshold = 0.02, N = 330.050 1-1 line 0.020 Density 20 Empirical gression line 0.020 Modeled confidence band 0.020 0.025 0.030 0.035 0.020 0.030 0.040 0.000 0.020 0.010 Model Quantiles Threshold = 0.01, N = 187 Density 0.010 Empirical 100 egression line Modeled 0.010 0 0.010 0.020 0.030

0.030

0.040

0.010

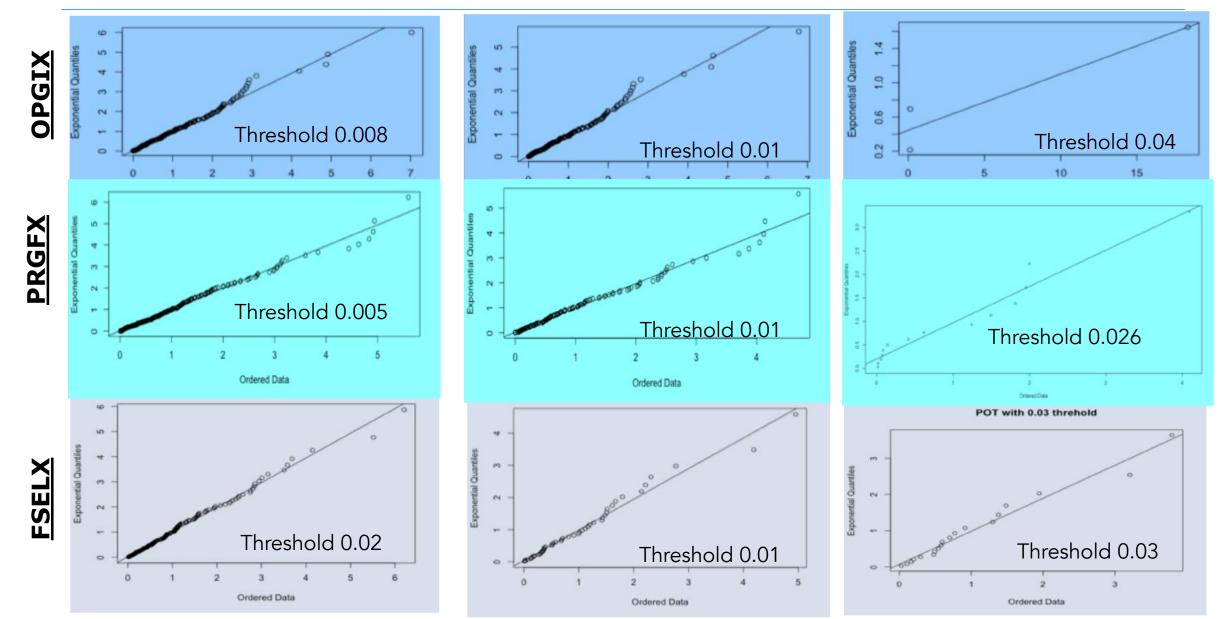
0.03

0.02

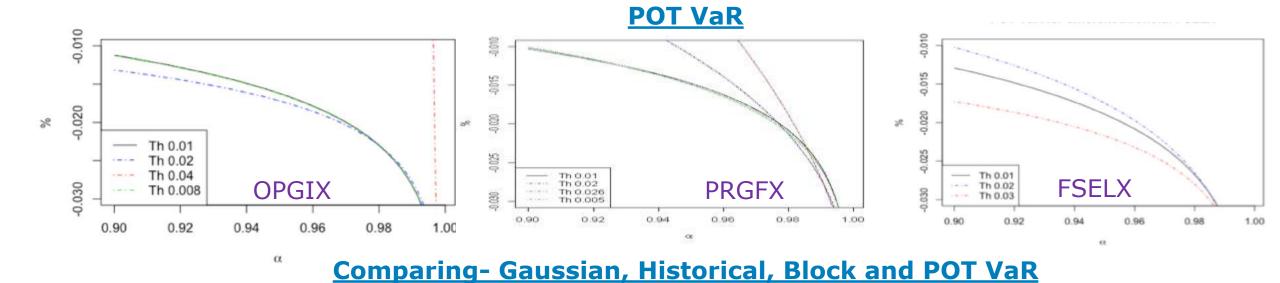
0.00

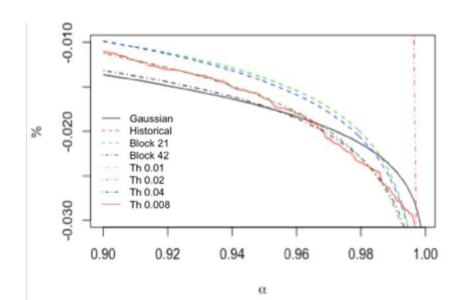
0.01

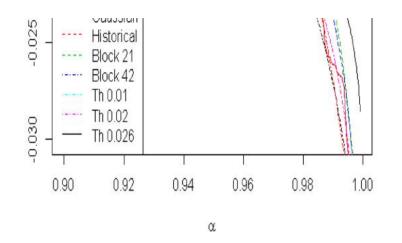
### Model fit for different threshold values



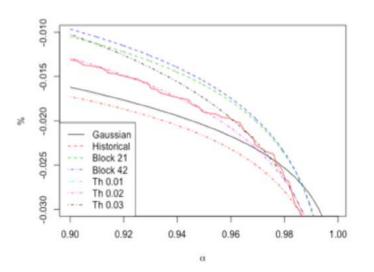
## VaR Sensitivity



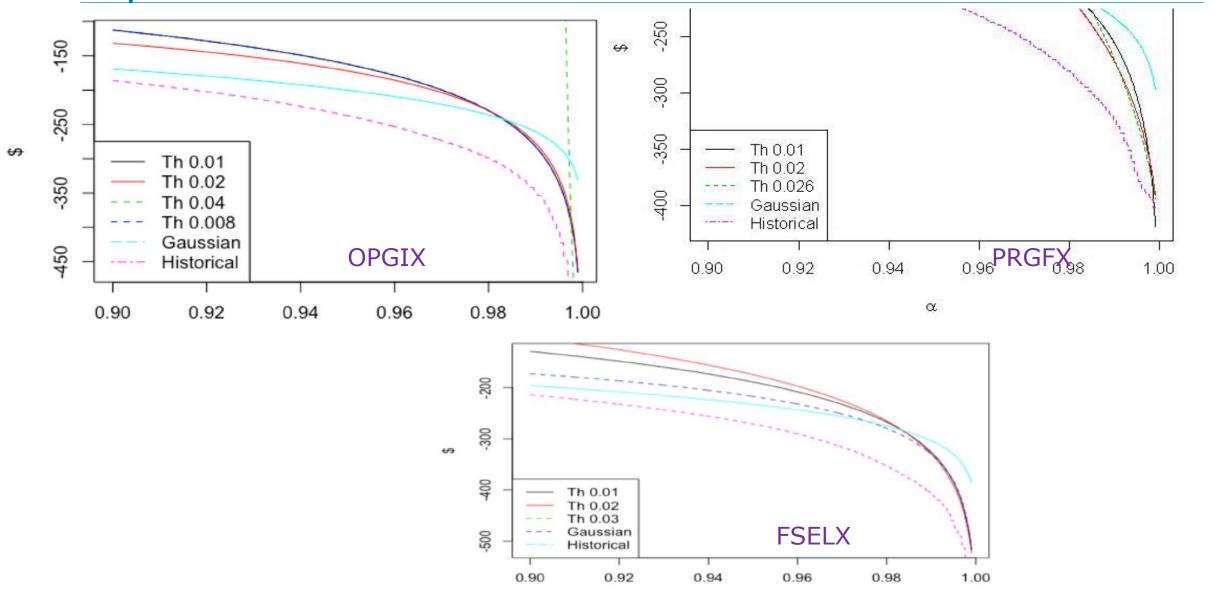




rage 24



# **Expected Shortfall**



### Conclusion

#### • Pros:

- VaR models can be used to estimate the loss of capital due to market risk
- It can measure the risk of stocks and bonds, commodities, foreign exchange, and structured prod- ucts such as asset-backed securities and collateralized mortgage obligations (CMOs), as well as off-balance- sheet derivatives such as futures, forwards, swaps, and options.
- It is particularly useful for a multi-asset-class portfolio and needs to measure its exposure to a variety of risk factors.
- VaR is useful to plan sponsors who have their portfolios managed by a variety of external asset managers and need to compare their performance on a risk-adjusted basis.

#### • Cons:

- The concept of VaR is very simple but this is also one of the main sources of critique.
- It underestimates the frequency of "extreme events," such as outcomes several standard deviations away from the mean
- All VaR approaches cannot be applied directly
- For EVT VaR either the threshold or block values need to be calculated
- VaR has also problems in estimating risk figures accurately for longer time horizons as the results quickly deteriorate when moving e.g. from monthly to annual measures.

VaR estimates should therefore always be accompanied by other risk management techniques, such as stress testing, sensitivity analysis and scenario analysis in order to obtain a wider view of surrounding risks.