



HONORCODE ELT23-4-4774

# Siddhika Shukla

has successfully completed the course spanning over 12 modules. The training helps people in understanding energy, its generation, consumption , wastage, carbon footprint , impact on the environment, means to avoid and minimize energy usage, alternative energy solutions , ways to become carbon neutral, misconceptions on solar energy, and approach to adopt solar energy solutions . This training is a part of the "ENERGYLITERACYTRAINING" of the Energy Swaraj Foundation.

19-04-2023

Organization



Funding Partners

















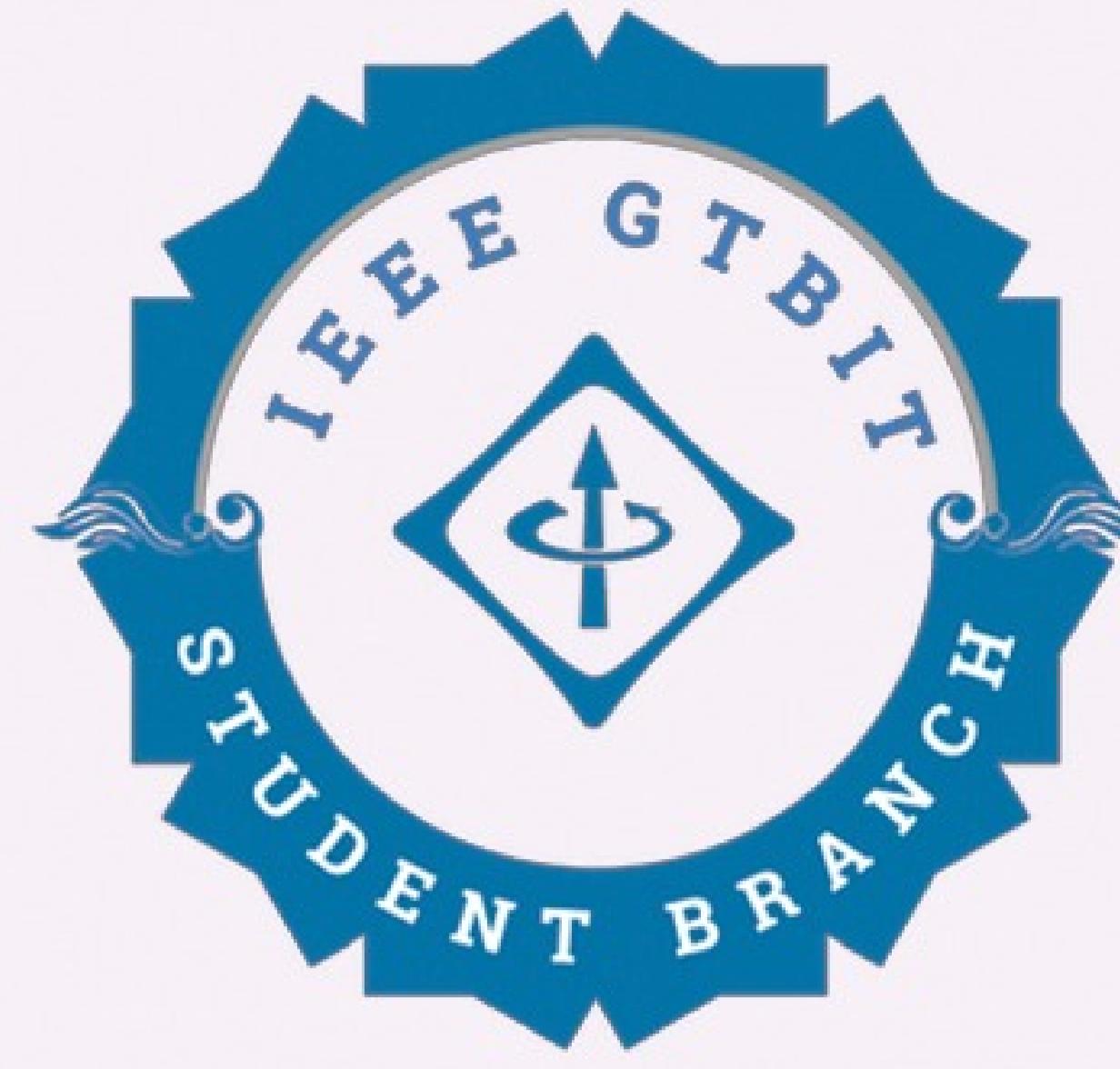








IEEE  
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# CERTIFICATE

OF PARTICIPATION

This certificate is awarded to

# Siddhika shukla

For participating in the event “ROADMAP TO WEB DEVELOPMENT” by  
IEEE GTBIT SB CS Chapter held on 10<sup>TH</sup> January 2022.

MR. MUKESH SAHU

BRANCH COUNSELLOR, IEEE GTBIT



## APPLIED MATHEMATICS – I

Mid-Term Examination

First Semester (B. Tech.)

Maximum Marks: 30

Paper code: ETMA-101

Time: 1Hr

Note: Question no. 1 to 20 carry 1 mark each.

Q1: If  $V = (x^2 + y^2)^{m/2}$ . Find the value of m which will make  $\frac{\partial^2 V}{\partial x^2} + \frac{\partial^2 V}{\partial y^2} = 0$ .

- I.  $m = -1$
- II.  $m = 0$
- III.  $m = 1$
- IV.  $m = 2$

Q2: If  $u = \tan^{-1}\left(\frac{x^3+y^3+z^3}{ax+by+cz}\right)$  Find the value of  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} + z \frac{\partial u}{\partial z}$ .

- I.  $-\sin 2u$
- II.  $\cos 2u$
- III.  $\sin 2u$
- IV.  $\sin u$

Q3: If  $(\cos y)^x - (\sin x)^y = 0$ . Then value of  $\frac{dy}{dx}$ .

- I.  $\frac{\log \cos y - y \cot x}{x t \any + \log \sin x}$
- II.  $\frac{\log \cos y + y \cot x}{x t \any + \log \sin x}$
- III.  $\frac{\log \cos y - y \cot x}{x t \any - \log \sin x}$
- IV.  $\frac{\log \cos y + y \cot x}{x t \any - \log \sin x}$

Q4: For the transformation  $u = a(x + y), v = b(x - y)$  and

$x = r^2 \sin 2\theta, y = r^2 \cos 2\theta$ . Find the Value of  $\frac{\partial(u,v)}{\partial(r,\theta)}$ .

- I.  $-8ab r^3$
- II.  $8ab r^3$
- III.  $-8ab r^2$
- IV.  $8ab r^2$

Q5: Solve  $-y dx + x dy = 0$

- I.  $\frac{y}{x} = c$
- II.  $\frac{x}{y} = c$
- III.  $\frac{y^2}{x} = c$
- IV.  $-\frac{x^2}{y} = c$

Q6: Examine the function  $f(x, y) = x^3 e^{-x^2-y^2}$  for maximum and minimum.

- a)  $f(x, y)$  is maximum at point  $(\frac{\sqrt{3}}{2}, 0)$
- b)  $f(x, y)$  is minimum at point  $(\frac{-\sqrt{3}}{2}, 0)$

Which of the following statement is true?

- I. Option a) is true and Option b) is false.
- II. Option a) is and Option b) both are true.
- III. Option a) is and Option b) both are false.
- IV. Option a) is false and Option b) is true.

Q7: Find the stationary value of  $a^3x^2 + b^3y^2 + c^3z^2$  subject to the fulfilment of the condition  $\frac{1}{x} + \frac{1}{y} + \frac{1}{z} = 1$ .

- I.  $(-a - b - c)^3$
- II.  $(a - b - c)^3$
- III.  $(a - b + c)^3$
- IV.  $(a + b + c)^3$

Q8: Solve  $y' - 1 = y^2$

- I.  $y = \tan(x+2)$
- II.  $y = \tan(x+1)$
- III.  $y = \tan x$
- IV.  $y = -\tan(x+1)$

Q9: Using Jacobian, Find  $\frac{\partial u}{\partial x}$  If  $u^2 - xy^2 + xy = 0$  and  $u^2 - uvx - v^2 = 0$

- I.  $\frac{v}{2y}$
- II.  $\frac{u}{2y}$
- III.  $-\frac{u}{2x}$
- IV.  $-\frac{v}{2x}$

Q 10: Given the family S of the curves given by

$F(x, y, c) = \frac{1}{2}x^2 + y^2 = c$  which is a family of ellipses, determine the family T of orthogonal trajectories.

- I.  $y = c^*x^2$
- II.  $y = cx$
- III.  $y = c(x+a)$
- IV.  $y = ax + by$

Q11: Solve  $y' + y \tan x = \sin 2x$

- I.  $y = c \cos x - 2\cos^2 x$
- II.  $y = c \sin x - 2\cos^2 x$
- III.  $y = c \cos x - 2\sin^2 x$
- IV.  $y = c \sin x - 2\sin^2 x$

Q12: Solve the following Differential Equation

$$y'' + 0.4y' + 9.04y = 0$$

- I.  $y = e^{-0.2x}(A\cos 3x + B\sin 2x)$
- II.  $y = e^{-0.2x}(A\cos 3x + B\sin 3x)$
- III.  $y = e^{-0.2x}(A\cos 3x - B\sin 3x)$
- IV.  $y = e^{-0.2x}(A\cos 2x + B\sin 3x)$

Q13: Find an Integrating Factor of the following Initial Value problem

$$(e^{x+y} + ye^y)dx + (xe^y - 1)dy = 0, y(0) = -1$$

- I.  $e^y$
- II.  $-e^{-y}$
- III.  $e^{-y}$
- IV.  $-e^y$

Q14: Solve  $\cos(x+y)dx + (3y^2 + 2y + \cos(x+y))dy = 0$  and find the solution  $u(x, y)$

- I.  $u(x, y) = \sin(x+y) + y^3 + y^2$
- II.  $u(x, y) = \sin(x+y) - y^3 + y^2$
- III.  $u(x, y) = \sin(x+y) + y^3 - y^2$
- IV.  $u(x, y) = \sin(x+y) - y^3 - y^2$

Q15: Evaluate  $\int_0^1 \frac{x^a - 1}{\log x} dx$ ,  $a \geq 0$

- I.  $F(a) = \log(1-a)$
- II.  $F(a) = \log(1+ka)$
- III.  $F(a) = \log(1-ka)$
- IV.  $F(a) = \log(1+a)$

Q16: What is the characteristic shape of a curve illustrating logistic growth?

- I. *J-Shaped*
- II. *U-Shaped*
- III. *S-Shape*
- IV. *L-Shaped*

Q17: Solve the differential equation  $x^2y'' - 5xy' + 9y = 0$ .

- I.  $(c_1 + c_2 \ln x)x^3$
- II.  $(c_1 - c_2 \ln x)x^3$
- III.  $(c_1 - c_2 \ln x)x^{-3}$
- IV.  $(c_1 + c_2 \ln x)x^{-3}$

Q18: Find the Wronskian. If the functions  $y_1 = \cos \omega x$  and  $y_2 = \sin \omega x$  are solutions of  $y'' + \omega^2 y = 0$

- I.  $\omega^2$
- II.  $\omega$
- III.  $\omega^3$
- IV.  $\omega^4$

Q19: Solve  $(x^2y^3 + 2y)dx + (2x - 2x^3y^2)dy = 0$

- I.  $x = cy^2 e^{\frac{1}{x^2y^2}}$
- II.  $x = ce^{\frac{1}{x^2y^2}}$
- III.  $x = cy^2 e^{-(\frac{1}{x^2y^2})}$
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Q20: Solve  $\frac{dy}{dx} - \frac{\tan y}{1+x} = (1+x)e^x \sec y$

- I.  $\sin y = (1+x)(e^x + c)$
- II.  $\sin y = (1-x)(e^x + c)$
- III.  $\sin y = (1+x)(-e^x + c)$
- IV.  $\sin y = (1-x)(e^x - c)$

Attempt any two Questions. Question 21, 22 and 23 carry 5 marks each.

Q21: Sketch the direction field for the following differential equation  $y' = y - x$

What are direction fields used for?

Q22: By the method of Variation of parameter. Solve  $\frac{d^2y}{dx^2} - y = \frac{2}{1+e^x}$

Q23: Find the maximum and minimum values of

$$f(x, y) = (x^3 + 3xy^2 - 15x^2 - 15y^2 + 72x)$$

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