

Java Programming

2-6
Sorting and Searching



Overview

This lesson covers the following topics:

- Recognize the sort order of primitive types and objects
- Trace and write code to perform a simple Bubble Sort of integers
- Trace and write code to perform a Selection Sort of integers
- Trace and write code to perform a Binary Search of integers
- Compare and contrast search and sort algorithms
- Analyze the Big-O for various sort algorithms



Sorting Arrays

- There are many different algorithms for sorting arrays.
- Some are easier to code, and some have a faster computation time.
- When searching for elements in an array, it is beneficial to sort your array in lexicographical order to reduce time spent searching through the array.

An algorithm is a logical computational procedure that if correctly applied, ensures the solution to a problem.

Lexicographical order is an order based on the ASCII value of characters. The table of values can be found at http://www.asciitable.com/



Main Sorting Algorithms for Arrays

- There are many sorting algorithms for arrays.
- Some of the common algorithms are:
 - Selection sort
 - Bubble sort
 - Insertion sort
 - Merge sort
 - Quick sort



Selection Sort

- Selection sort is a simple sorting algorithm that works as follows:
 - Find the minimum value in the list.
 - Swap it with the value in the first position.
 - Repeat the steps above for the remainder of the list, starting at the second position and advancing each time.



Selection Sort

- This algorithm:
 - Is inefficient on large arrays because it has to iterate through the entire array each time to find the next smallest element.
 - Is preferred for smaller arrays because of its simplicity.



Steps to the Selection Sort Algorithm

To sort the following array:

- Step 1: Find the smallest value, which is 2.
- Step 2: Swap the value with the first position:

- Repeat steps 1 and 2. 3 is the next smallest number.
- When swapped for the next position, the array is:



Steps to the Selection Sort Algorithm

- These steps are repeated until the array is sorted, or to be more specific, when array.length -1 is reached.
- At that point, if the second last element was bigger than the last, it would swap and the array would be sorted.
- Otherwise, the array is sorted.

- Watch this Selection Sort video:
 - https://www.youtube.com/watch?v=Ns4TPTC8whw

Selection Sort Code Example

This example follows the rules of selection sort.

```
public class SelectionSortTester{
    public static void main(String[] args){
         int[] numbers = {40, 7, 59, 4, 1};
         int indexMin = 0; //the index of the smallest number
         for(int i = 0; i< numbers.length; i++){</pre>
              indexMin = i;
              for(int j = i + 1; j < numbers.length; j++){</pre>
                 if(numbers[j] < numbers[indexMin]){//if we find a smaller int, set it as the min</pre>
                    indexMin = j;
              } //we now have the index of the smallest int and can swap the values
              int temp = numbers[i]; //use temp to store the value
              numbers[i] = numbers[indexMin];
              numbers[indexMin] = temp;
         for(int i = 0; i< numbers.length; i++){</pre>
              System.out.print(numbers[i] + " ");
}
```

Bubble Sort

- Bubble sort, also known as exchange sort, is another sorting algorithm that is simple but inefficient on large lists.
- The algorithm works as follows:
 - Compare 2 adjacent values (those at indexes 0 and 1).
 - If they are in the wrong order, swap them.
 - Continue this with the next two adjacent values (those at indexes 1 and 2) and on through the rest of the list.
 - Repeat steps 1 through 3 until array is sorted.



Bubble Sort Video

- Watch this Bubble Sort video:
 - http://www.youtube.com/watch?v=lyZQPjUT5B4





Bubble Sort Example

To sort the following array:

```
{40, 7, 59, 4, 1}
```

First, compare and swap the first two values:

```
{7, 40, 59, 4, 1}
```

Then, compare and swap the next two values:

```
{7, 40, 59, 4, 1}
```

- Notice that the swap did not occur in the second comparison because they are already in correct order.
- Repeat these steps until the array is sorted.

```
{1, 4, 7, 40, 59}
```



Bubble Sort Array Example

Step by step, the array would look as follows.

```
{40, 7, 59, 4, 1} //Starting array
{7, 40, 59, 4, 1} //7 and 40 swapped
{7, 40, 59, 4, 1} //40 and 59 did not swap
{7, 40, 4, 59, 1} //59 and 4 swapped
{7, 40, 4, 1, 59} //1 and 59 swapped
//First pass through array is complete
{7, 40, 4, 1, 59} //7 and 40 did not swap
{7, 4, 40, 1, 59} //40 and 4 swapped
{7, 4, 1, 40, 59} //40 and 1 swapped
{7, 4, 1, 40, 59} //40 and 59 did not swap
//Second pass is complete
{4, 7, 1, 40, 59} //7 and 4 swapped
{4, 1, 7, 40, 59} //7 and 1 swapped
{4, 1, 7, 40, 59} //7 and 40 did not swap
//Third pass is complete
{1, 4, 7, 40, 59} //1 and 4 swapped
{1, 4, 7, 40, 59} //4 and 7 did not swap
//Fourth pass is complete and the array is sorted
```

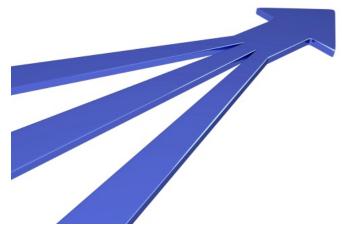
Bubble Sort Code Example

- Trace through this code on paper.
- Do you see all of the same steps as shown previously?

```
int[] numbers = {40, 7, 59, 4, 1};
for(int j =0 ; j < numbers.length; j++){</pre>
     for(int i = 0; i < numbers.length-1; i++){</pre>
          //if the numbers are not in order
         if(numbers[i] > numbers[i+1]){
                //swap the numbers
                int temp = numbers[i];
                numbers[i] = numbers[i+1];
                numbers[i+1] = temp;
```

Merge Sort

- Merge sort:
 - Is more complex than the previous two sorting algorithms.
 - Can be more efficient because it takes advantage of parallel processing.
 - Takes on a "divide and conquer" technique, which allows it to sort arrays with optimal speed.



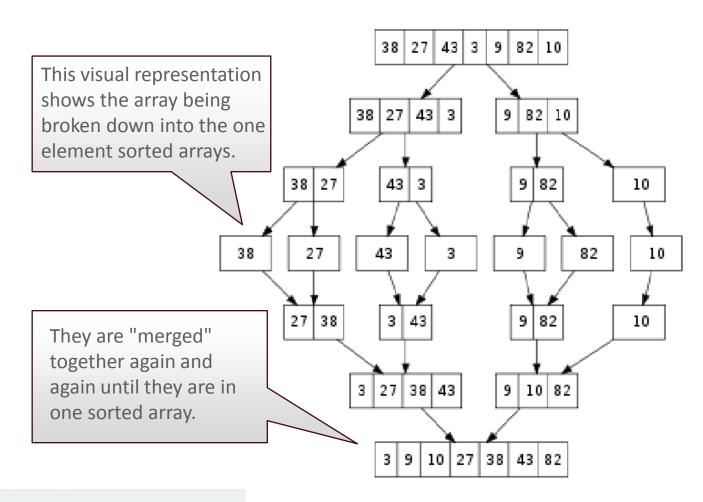


Merge Sort Algorithm

- The algorithm works as follows:
 - Divide the unsorted list into sub-lists, each containing one element (a list of one element is considered sorted).
 - Repeatedly merge sub-lists to produce new sub-lists until there is only one sub-list remaining.
 - This will be the sorted list.



Visual Representation of Merge Sort





Learn More About Merge Sort

- This lesson focuses on the theory of merge sort since it is so complex.
- Watch the following Merge Sort video:
 - https://www.youtube.com/watch?v=XaqR3G NVoo

Searching Through Arrays

- Sorting an array makes searching faster and easier.
- There are two basic searching methods:
 - Sequential/Linear searches
 - Binary searches
- For example, in a sorted array of student names, you want to know if Juan is in your class.
- You could search the array, or find out exactly where his name is in alphabetical order with the other students.

Searching Through Arrays Sequentially

- A sequential search is an iteration through the array that stops at the index where the desired element is found.
- If the element is not found, the search stops after all elements of the list have been iterated through.
- This method works for unsorted or sorted arrays, but is not efficient on larger arrays.
- However, a sequential search is not more efficient if the list is sorted.
- Since we know that our array of student names is sorted, we could use a much more efficient searching method: A binary search.



Using Binary Search With Sorted Arrays

- Binary searches can only be performed on sorted data.
- To see how a binary search works:
 - Search for the target value 76 in the array.
 - Step 1: Identify the low, middle, and high elements in the array.
 - Low is 0, high is array.length -1 = 10, middle is (high low)/2 = 5
 - Step 2: Compare the target value with the middle value.
 - 76 is greater than 56.

Index	0	1	2	3	4	5	6	7	8	9	10
Value	2	10	16	34	37	56	57	76	81	83	85



Using Binary Search With Sorted Arrays

- To see how a binary search works:
 - Step 3: Since the target value is greater than the middle value, it is to the right of the middle. Set the low index to middle + 1, then calculate the new middle index.
 - Middle is ((5 + 1) + 10)/2 = 8
 - Step 4: Compare the target value with the middle value.
 - 76 is less than 81.

Index	0	1	2	3	4	5	6	7	8	9	10
Value	2	10	16	34	37	56	57	76	81	83	85

Using Binary Search With Sorted Arrays

- To see how a binary search works:
 - Step 5: Since the target value is less than the middle value, it is to the left of the middle. Set the high index to middle - 1 then calculate the new middle index.
 - Middle is ((8-1)+6)/2=7
 - Step 6: Compare the target value with the middle value.
 - 76 is equal to 76.
 - Step 7: The target value has been found at index 7.

Index	0	1	2	3	4	5	6	7	8	9	10
Value	2	10	16	34	37	56	57	76	81	83	85

Decide What to Return in a Binary Search Method

- When writing a binary search method you will have to decide what to return.
- Index
- Boolean
- Value
 - Entire object
 - One field of the object
- What would you return if the value was not found?



Binary Search Example 1

 The example method will return true if the value is found in the array and false if it is not found.

```
public boolean binarySearch(int target, int[] data){
       int low = 0;
       int high = data.length - 1;
       while(high >= low){
          int middle = (low + high)/2; // Middle index
          if(data[middle] == target){
             return true; // Target value was found
          if(data[middle] < target){</pre>
             low = middle + 1;
          if(data[middle] > target){
             high = middle - 1;
      return false; // The value was not found
```

Binary Search Example 2

 What would need to be changed to return the index of where the target value was found?

```
public boolean binarySearch(int target, int[] data){
       int low = 0;
       int high = data.length - 1;
       while(high >= low){
          int middle = (low + high)/2; // Middle index
          if(data[middle] == target){
             return true; // Target value was found
          if(data[middle] < target){</pre>
             low = middle + 1;
          if(data[middle] > target){
             high = middle - 1;
      return false; // The value was not found
```

Comparison of Sorting Algorithms

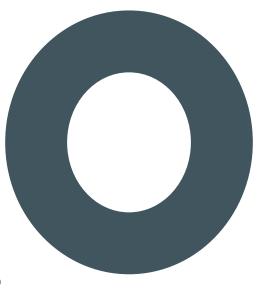
From https://en.wikipedia.org/wiki/Big O notation

Name ♦	Best ♦	Average \$	Worst \$	Memory ♦	Stable +	Method ♦	
Quicksort	$n \log n$	$n \log n$	n^2	$\log n$	Depends	Partitioning	
Merge sort	$n \log n$	$n \log n$	$n\log n$ Depends; worst case is n		Yes	Merging	
In-place Merge sort	_	_	$n\left(\log n\right)^2$	1	Yes	Merging	
Heapsort	$n \log n$	$n \log n$	$n \log n$	1	No	Selection	
Insertion sort	n	n^2	n^2	1	Yes	Insertion	
Introsort	$n \log n$	$n \log n$	$n \log n$	$\log n$	No	Partitioning & Selection	
Selection sort	n^2	n^2	n^2	1	No	Selection	
Timsort	n	$n \log n$	$n \log n$	n	Yes	Insertion & Merging	
Shell sort	n	$n(\log n)^2$ or $n^{3/2}$	Depends on gap sequence; best known is $n(\log n)^2$	1	No	Insertion	
Bubble sort	n	n^2	n^2	1	Yes	Exchanging	
Binary tree sort	n	$n \log n$	$n \log n$	n	Yes	Insertion	
Cycle sort	_	n^2	n^2	1	No	Insertion	
Library sort	_	$n \log n$	n^2	n	Yes	Insertion	
Patience sorting	_	_	$n \log n$	n	No	Insertion & Selection	
Smoothsort	n	$n \log n$	$n \log n$	1	No	Selection	
Strand sort	n	n^2	n^2	n Yes		Selection	
Tournament sort	_	$n \log n$	$n \log n$	$n^{\scriptscriptstyle{[5]}}$		Selection	
Cocktail sort	n	n^2	n^2	1 Yes Ex		Exchanging	
Comb sort	n	$n \log n$	n^2	1	No	Exchanging	
Gnome sort	n	n^2	n^2	1	Yes	Exchanging	
Bogosort	n	$n \cdot n!$	$n \cdot n! \to \infty$	1	No	Luck	



Big-O Notation

- Big-O Notation is used in Computer Science to describe the performance of Sorts and Searches on arrays.
- The Big-O is a proportion of speed or memory usage to the size of the array.
- In the previous slide, Big-O examples are:
 - n
 - n log n
 - -n2
- Compare the values of these sorts.
 - Which sort(s) is/are quickest when n is 100?
 - Which sort(s) is/are quickest when n is 1 Billion?



Terminology

Key terms used in this lesson included:

- Array
- Binary search
- Bubble Sort
- Lexicographical order
- Merge Sort
- Selection Sort
- Sequential search



Summary

In this lesson, you should have learned how to:

- Recognize the sort order of primitive types and objects
- Trace and write code to perform a simple Bubble Sort of integers
- Trace and write code to perform a Selection Sort of integers
- Trace and write code to perform a Binary Search of integers
- Compare and contrast search and sort algorithms
- Analyze the Big-O for various sort algorithms



