

Analysis

The non-recursive steps takes $O(n)$ time including finding median and other statements.

for recursive calls, we are dividing the space into two halves, using a linear so our $T(n)$ becomes

$$T(n) = \begin{cases} C & \text{if } n < 2 \\ 2T(n/2) + cn & \text{if } n \geq 2 \end{cases}$$

for some constant c
solving recurrence

$\begin{matrix} & \text{level } cm \\ & cn \\ & \nearrow \\ 2 & \times \\ \text{CD:} & \\ \frac{cn}{2} & \end{matrix} \rightarrow \frac{cn}{2} + \frac{cn}{2} = cn$

so at every level, the level cm remains constant which means.

so tight bound is root * depth.

Depth of the tree is $\log n$ and root is n

$$\boxed{O(n \log n)}$$

hence the running time is $O(n \log n)$

This running time is achieved because at every level we are splitting the space into two halves using the median as the dividing line.