

1 Linear Convolution

Write a matlab code for linear convolution of two signals. Then

1. Generate the causal signals

$$\begin{aligned}x_1[n] &= \{-2, 2, 3, 1, 12\} \\&\quad \uparrow \\x_2[n] &= \{1, -1, 4, -2\} \\&\quad \uparrow \\h[n] &= \{3, -2, -5, 1, -4\} \\&\quad \uparrow\end{aligned}$$

Now, determine the output of the given systems

$$\begin{aligned}y_1[n] &= (x_1[n] + x_2[n]) * h[n] \\y_2[n] &= x_1[n] * h[n] + x_2[n] * h[n]\end{aligned}$$

- (a) Perform the calculations using your matlab code and verify the results using the inbuilt function *conv* and on-paper calculations.
- (b) Verify if the outputs $y_1[n]$ and $y_2[n]$ are identical or not.
- (c) Using the *stem* function, plot the signals $x_1[n]$, $x_2[n]$, $h[n]$, $y_1[n]$ and $y_2[n]$.

```
n=0:10;
x1=zeros(size(n));
x2=zeros(size(n));
h=x1;
y1=h;
x1(n==0)=-2;
x1(n==1)=2;
x1(n==2)=3;
x1(n==3)=1;
x1(n==4)=12;
x1(n==5)=0;
x1(n==6)=0;
x1(n==7)=0;
x1(n==8)=0;
x2(n==0)=1;
x2(n==1)=-1;
x2(n==2)=4;
x2(n==3)=-2;
```

```

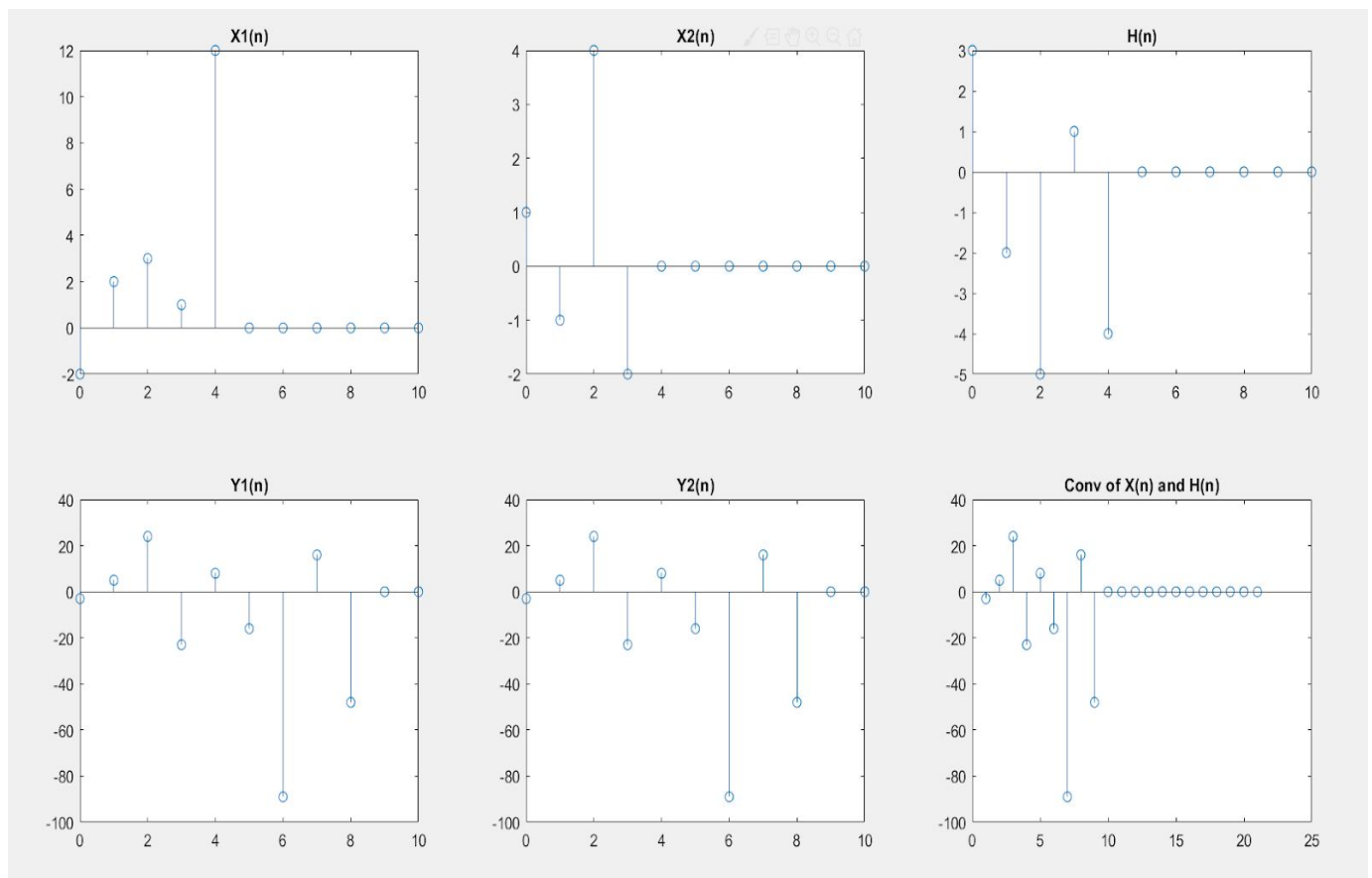
x2(n==4)=0;
x2(n==5)=0;
x2(n==6)=0;
x2(n==7)=0;
x2(n==8)=0;
h(n==0)=3;
h(n==1)=-2;
h(n==2)=-5;
h(n==3)=1;
h(n==4)=-4;
h(n==5)=0;
h(n==6)=0;
h(n==7)=0;
x=x1+x2;
y1=zeros(size(n));
for l=1:10
    y1(l)=0;
    for k=1:l
        y1(l)=y1(l)+h(k).*x(l-k+1);
    end
end
ya=zeros(size(n));
for l=1:10
    ya(l)=0;
    for k=1:l
        ya(l)=ya(l)+h(k).*x1(l-k+1);
    end
end
yb=zeros(size(n));
for l=1:10
    yb(l)=0;
    for k=1:l
        yb(l)=yb(l)+h(k).*x2(l-k+1);
    end
end
y2=ya+yb;
z=conv(x,h);
subplot(231);
stem(n,x1);
title('X1(n)');
subplot(232);
stem(n,x2);
title('X2(n)');

```

```

subplot(233);
stem(n,h);
title('H(n)');
subplot(234);
stem(n,y1);
title('Y1(n)');
subplot(235)
stem(n,y2);
title('Y2(n)');
subplot(236)
stem(z);
title('Conv of X(n) and H(n)');

```



$Y1(n)=Y2(n)=\text{Conv of } X(n) \text{ and } H(n)=\{-3, 5, 24, -23, 8, -16, -89, 16, -48\}$

$$\begin{aligned}
 x_1[n] &= \{-2, 2, 3, 1, 1, 2\} \\
 x_2[n] &= \{1, -1, 4, -2\} \\
 x[n] &= x_1 + x_2 \\
 x[n] &= \{-1, 1, 7, -1, 1, 2\} \\
 h[n] &= \{3, -2, -5, 1, -4\} \\
 y[n] &= x[n] * h[n]
 \end{aligned}$$

$x \backslash h$	-1	1	7	-1	1	2
3	-3	3	21	-3	3	6
-2	2	-2	-14	2	-2	4
-5	5	-5	-35	5	-5	10
1	-1	1	7	-1	1	2
-4	4	-4	-28	4	-4	8

$$y[n] = \{-3, 5, 24, -23, 8, -46, 16, -48\}$$

2. Next, generate the translated signals

$$x[n] = \{3, 3, \underset{\uparrow}{1}, 2, 3, \}$$

$$h[n] = \{1, 2, \underset{\uparrow}{3}, 2, 1\}$$

Now, determine the output of the given system

$$y[n] = x[n] * h[n]$$

- Perform the calculations using your matlab code and verify the results using the inbuilt function *conv* and on-paper calculations.
- Using the *stem* function, plot the signals $x[n]$, $h[n]$, and $y[n]$.

```

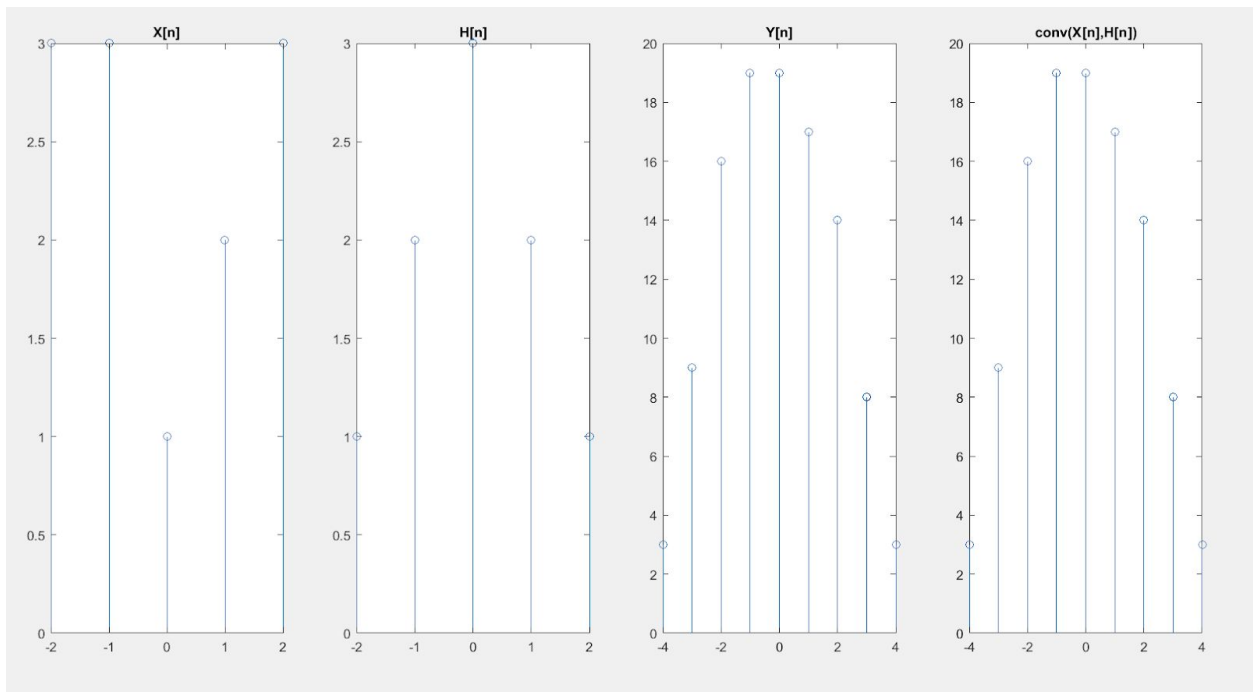
N=-2:1:2;
x=X(N);
h=H(N);
l=size(x')+size(h')-1;

```

```

he=zeros(l);
xe=zeros(l);
he(1:size(h'))=h;
xe(1:size(x'))=x;
y=zeros(l);
for n=1:1:l
    y(n)=0;
    for k=1:1:n
        y(n)=y(n)+he(k).*xe(n-k+1);
    end
end
y=y'
N1=-4:1:-4+l-1;
subplot(141);
stem(N,x);
title('X[n]');
subplot(142);
stem(N,h);
title('H[n]');
subplot(143);
stem(N1,y);
title('Y[n]');
co=conv(x,h);
subplot(144);
stem(N1,co);
title('conv(X[n],H[n])');
function a=X(n)
a=zeros(size(n));
a(n== -2)=3;
a(n== -1)=3;
a(n== 0)=1;
a(n== 1)=2;
a(n== 2)=3;
end
function a=H(n)
a=zeros(size(n));
a(n== -2)=1;
a(n== -1)=2;
a(n== 0)=3;
a(n== 1)=2;
a(n== 2)=1;
end

```



$Y_2(n) = \text{Conv of } X(n) \text{ and } H(n) = \{3, 9, 16, 19, 19, 17, 14, 8, 3\}$

$x[n] = \{3, 3, 1, 2, 3\}$
 $h[n] = \{1, 2, 3, 2, 1\}$
 $y[n] = x[n] * h[n]$

n	3	3	1	2	3
1	3	3	1	2	3
2	6	6	2	4	6
3	9	9	3	6	9
2	6	6	2	4	6
1	3	3	1	2	3

$y[n] = \{3, 9, 16, 19, 19, 17, 14, 8, 3\}$

3. Next generate the signals

$$\begin{aligned}x[n] &= \{ \underset{\uparrow}{2}, -1, 4, -7, 5 \} \\h[n] &= \{ \underset{\uparrow}{2}, 4, 2, 4, 1 \}\end{aligned}$$

Now, compute the output of the given systems

$$\begin{aligned}y_1[n] &= x[n] * h[-n] \\y_2[n] &= x[3-n] * h[n]\end{aligned}$$

- (a) Perform the calculations using your matlab code and verify the results using the inbuilt function *conv* and on-paper calculations.
- (b) Using the *stem* function, plot the signals $x[n]$, $h[n]$, $y_1[n]$ and $y_2[n]$.

```
N=-4:1:4;
x1=X(N,1,0);
h1=H(N,-1,0);
x2=X(N,-1,3);
h2=H(N,1,0);
l=size(x1')+size(h1')-1;
he=zeros(l);
xe=zeros(l);
he(1:size(h1'))=h1
xe(1:size(x1'))=x1
y1=zeros(l);
y2=zeros(l);
for n=1:1:l
    y1(n)=0;
    for k=1:1:n
        y1(n)=y1(n)+he(k).*xe(n-k+1);
    end
end
y1=y1'
xe(12)
he(1:size(h2'))=h2;
xe(1:size(x2'))=x2;
for n=1:1:l
```

```

        y2(n)=0;
        for k=1:1:n
            y2(n)=y2(n)+he(k).*xe(n-k+1);
        end
    end
    y2=y2'
    N1=-8:1:-1-8;
    subplot(2,4,1);
    stem(N,x1);
    title('X[n]');
    subplot(2,4,2);
    stem(N,h1);
    title('H[-n]');
    subplot(2,4,3);
    stem(N1,y1);
    title('Y1[n]');
    co1=conv(x1,h1);
    subplot(2,4,4);
    stem(N1,co1);
    title('conv(X[n],H[-n])');
    subplot(2,4,5);
    stem(N,x2);
    title('X[3-n]');
    subplot(2,4,6);
    stem(N,h2);
    title('H[n]');
    subplot(2,4,7);
    stem(N1,y2);
    title('Y2[n]');
    co2=conv(x2,h2);
    subplot(2,4,8);
    stem(N1,co2);
    title('conv(X[3-n],H[n])');
    function a=X(n,c,d)
    a=zeros(size(n));
    a(n==d)=2;
    a(n==c+d)=-1;
    a(n==(2*c)+d)=4;
    a(n==(3*c)+d)=-7;
    a(n==(4*c)+d)=5;
    end
    function a=H(n,c,d)
    a=zeros(size(n));

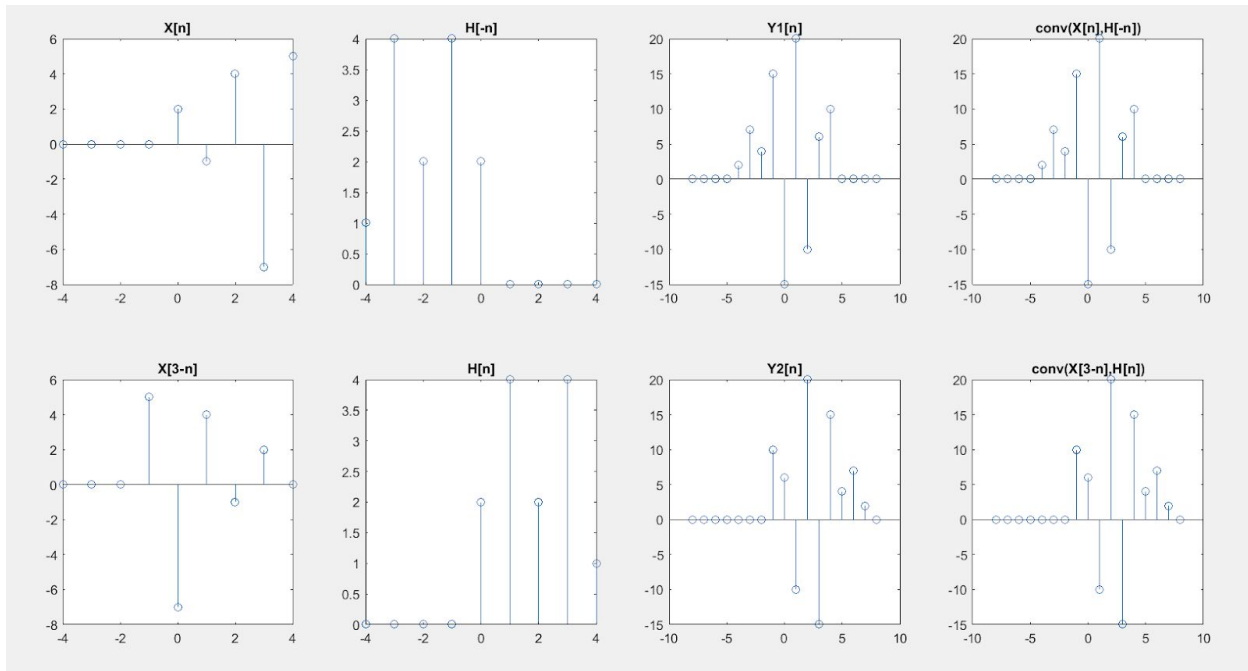
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```

a(n==d)=2;
a(n==c+d)=4;
a(n==(2*c)+d)=2;
a(n==(3*c)+d)=4;
a(n==(4*c)+d)=1;
end

```



$Y1(n) = \text{Conv of } X(n) \text{ and } H(-n) = \{0, 0, 0, 0, 2, 7, 4, 15, -15, 20, -10, 6, 10, 0, 0\}$

$Y2(n) = \text{Conv of } X(3-n) \text{ and } H(n) = \{0, 0, 0, 0, 0, 0, 0, 10, 6, -10, 20, -15, 15, 4, 7, 2, 0\}$

$$x[n] = \{ \underset{\uparrow}{2}, -1, 4, -7, 5 \}$$

$$h[n] = \{ \underset{\uparrow}{2}, 4, 2, 4, 1 \}$$

$$x[3-n] = \{ 5, -7, \underset{\uparrow}{4}, -1, 2 \}$$

$$h[-n] = \{ 1, \underset{\uparrow}{4}, 2, 4, 2 \}$$

$$y_2[n] = x[n] * h[-n] \quad \uparrow$$

$$= \sum_{k=-\infty}^{\infty} x[k] h[-(n-k)]$$

$$= \sum_{k=0}^{\infty} x[k] h[-n+k]$$

$$y_1[n] = x[0]h[-n] + x[1]h[-n+1] + \dots + x[4]h[-n+4]$$

$$= 2h[-n] - h[-n+1] + 4h[-n+2] +$$

$$h[-n+3] + 2h[-n+4]$$

$$y_1[n] = \{ 0, 0, 0, 0, \underset{\uparrow}{2}, 7, 4, 15, -15, 20, -10, 6, 13 \}$$

$$y_2[n] = x[3-n] * h[n] = \sum_{k=-\infty}^{\infty} x[3-n+k] h[k]$$

$$y_2[n] = 2x[3-n] + 4x[4-n] + 2x[5-n] +$$

$$4x[6-n] + x[7-n]$$

$$y_2 = \{ 0, 0, 0, 0, 0, 0, 0, \underset{\uparrow}{10}, 6, -10, 20, -15, 15, 4, 7, 2, 0 \}$$