

# Computer Vision

## Image Filtering in Spatial Domain

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# Today's Agenda

- Image Filtering in Spatial Domain

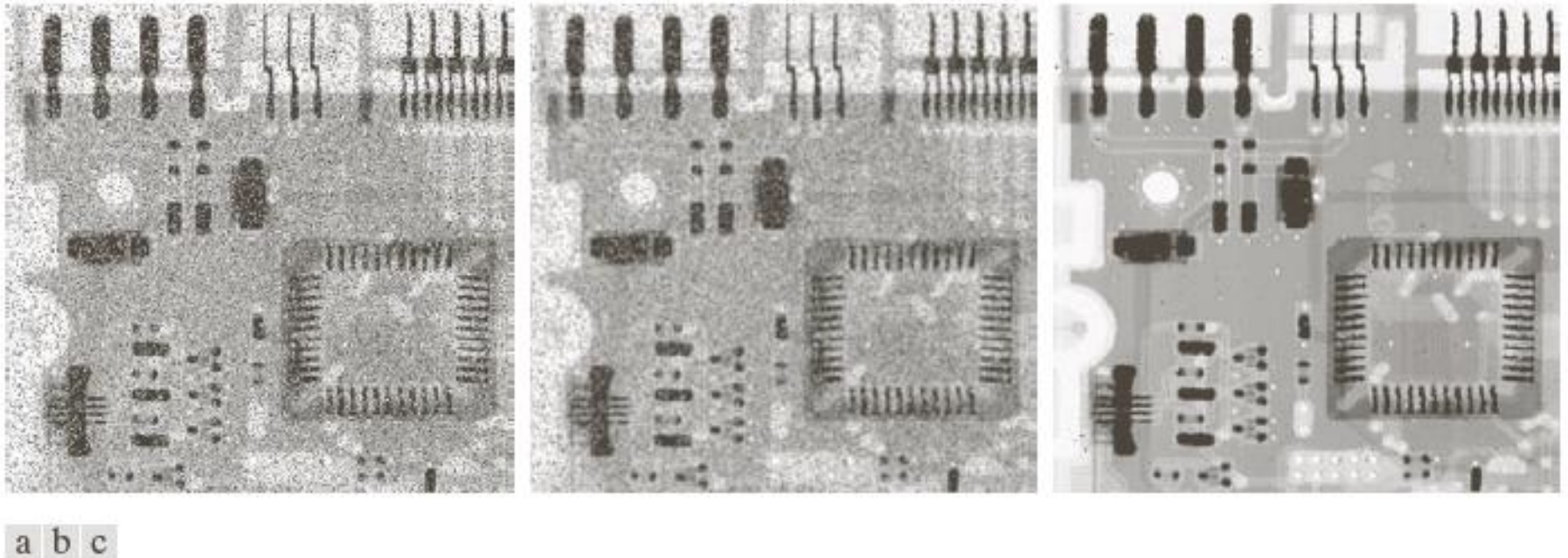
# Image Filtering in Spatial Domain

## Order-Statistic (Nonlinear) Filters

- ❑ Nonlinear
- ❑ Based on ordering (ranking) the pixels contained in the filter mask
- ❑ Replacing the value of the center pixel with the value determined by the ranking result
- ❑ E.g., median filter, max filter, min filter

# Image Filtering in Spatial Domain

## Example: Use of Median Filtering for Noise Reduction



**FIGURE 3.35** (a) X-ray image of circuit board corrupted by salt-and-pepper noise. (b) Noise reduction with a  $3 \times 3$  averaging mask. (c) Noise reduction with a  $3 \times 3$  median filter. (Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)

# Image Filtering in Spatial Domain

## Sharpening Spatial Filters

- ❑ Foundation
- ❑ Laplacian Operator
- ❑ Unsharp Masking and Highboost Filtering
- ❑ Using First-Order Derivatives for Nonlinear Image Sharpening
  - The Gradient

# Image Filtering in Spatial Domain

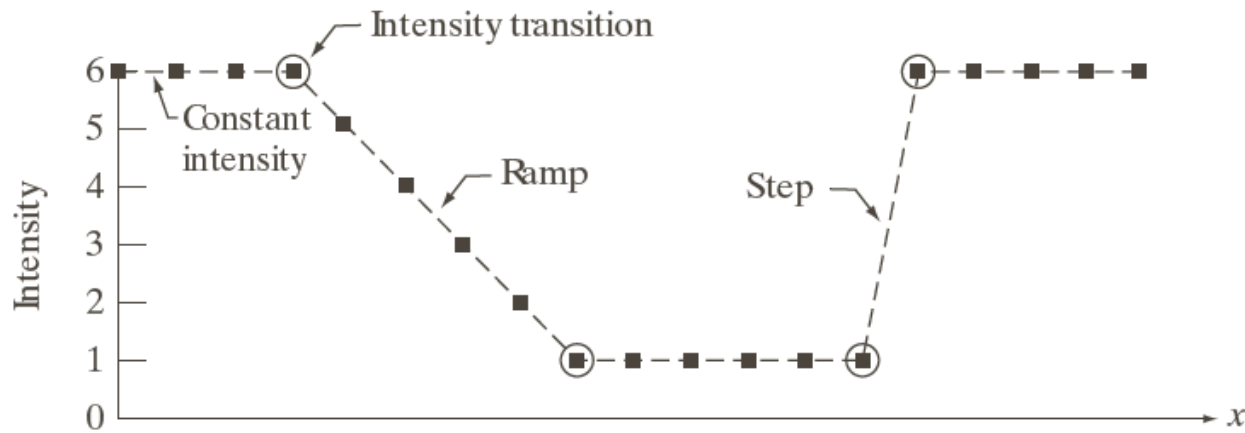
## Sharpening Spatial Filters: Foundation

- The first-order derivative of a one-dimensional function  $f(x)$  is the difference

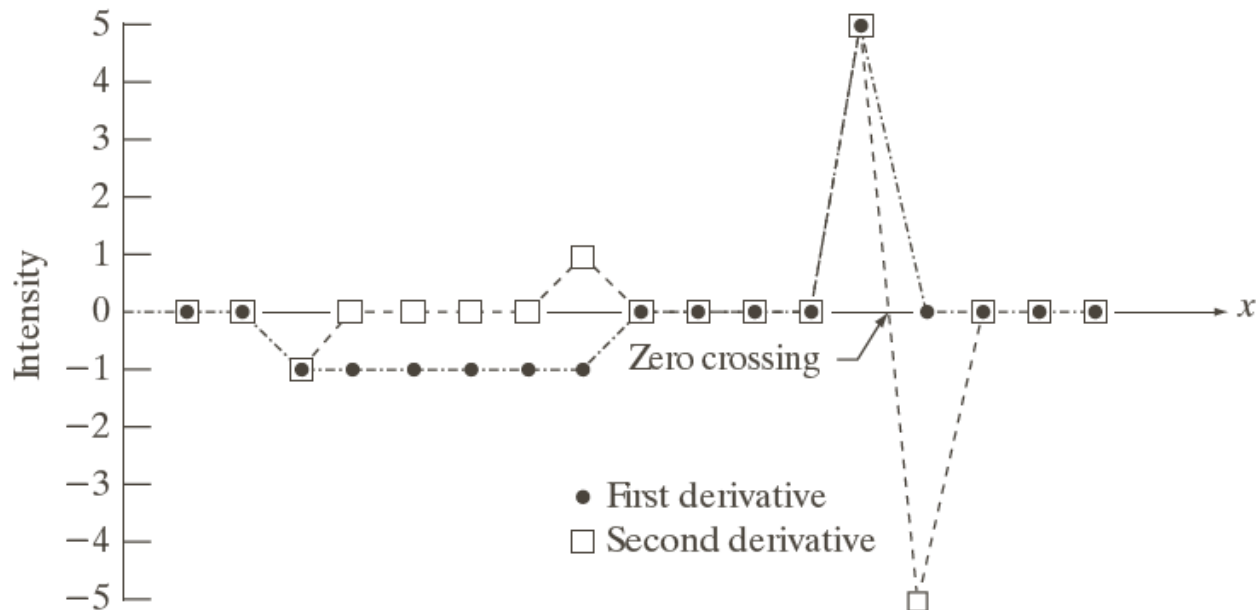
$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

- The second-order derivative of  $f(x)$  as the difference

$$\frac{\partial^2 f}{\partial x^2} = f(x+1) + f(x-1) - 2f(x)$$



Scan line	6	6	6	6	5	4	3	2	1	1	1	1	1	1	6	6	6	6	6	$x$
1st derivative	0	0	0	-1	-1	-1	-1	-1	0	0	0	0	0	0	5	0	0	0	0	
2nd derivative	0	0	0	-1	0	0	0	0	1	0	0	0	0	0	5	-5	0	0	0	



a  
b  
c

**FIGURE 3.36** Illustration of the first and second derivatives of a 1-D digital function representing a section of a horizontal intensity profile from an image. In (a) and (c) data points are joined by dashed lines as a visualization aid.

# Image Filtering in Spatial Domain

## Sharpening Spatial Filters: Laplacian Operator

The second-order isotropic derivative operator is the Laplacian for a function (image)  $f(x, y)$

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

$$\frac{\partial^2 f}{\partial x^2} = f(x+1, y) + f(x-1, y) - 2f(x, y)$$

$$\frac{\partial^2 f}{\partial y^2} = f(x, y+1) + f(x, y-1) - 2f(x, y)$$

$$\begin{aligned} \nabla^2 f &= f(x+1, y) + f(x-1, y) + f(x, y+1) + f(x, y-1) \\ &\quad - 4f(x, y) \end{aligned}$$



# Image Filtering in Spatial Domain

## Sharpening Spatial Filters: Laplacian Operator

0	1	0	1	1	1
1	-4	1	1	-8	1
0	1	0	1	1	1

0	-1	0	-1	-1	-1
-1	4	-1	-1	8	-1
0	-1	0	-1	-1	-1

a	b
c	d

**FIGURE 3.37**

(a) Filter mask used to implement Eq. (3.6-6).

(b) Mask used to implement an extension of this equation that includes the diagonal terms. (c) and (d) Two other implementations of the Laplacian found frequently in practice.

# Image Filtering in Spatial Domain

## Sharpening Spatial Filters: Laplacian Operator

Image sharpening in the way of using the Laplacian:

$$g(x, y) = f(x, y) + c \left[ \nabla^2 f(x, y) \right]$$

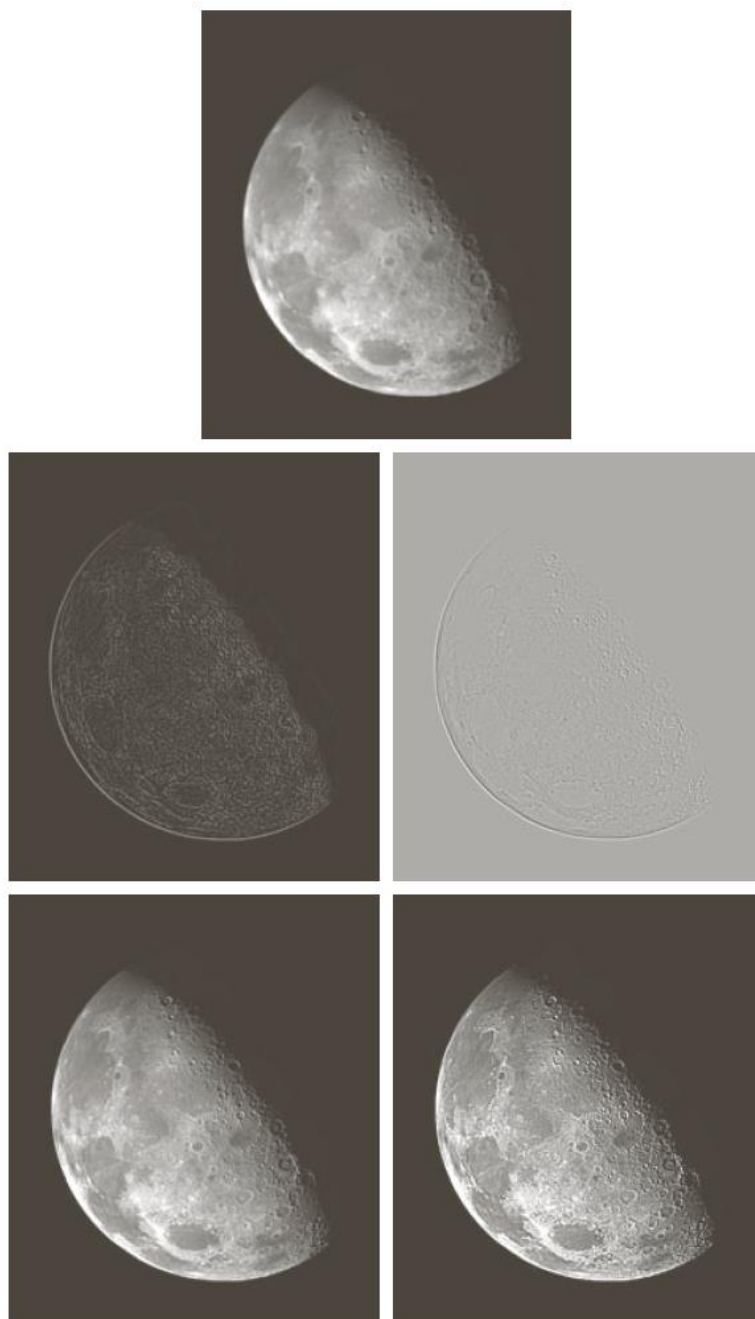
where,

$f(x, y)$  is input image,

$g(x, y)$  is sharpened images,

$c = -1$  if  $\nabla^2 f(x, y)$  corresponding to Fig. 3.37(a) or (b)

and  $c = 1$  if either of the other two filters is used.



a	
b	c
d	e

### FIGURE 3.38

(a) Blurred image of the North Pole of the moon.

(b) Laplacian without scaling.

(c) Laplacian with scaling. (d) Image sharpened using the mask in Fig. 3.37(a).

(e) Result of using the mask in Fig. 3.37(b).

(Original image courtesy of NASA.)

# Image Filtering in Spatial Domain

## Unsharp Masking and Highboost Filtering

### □ Unsharp masking

Sharpen images consists of subtracting an unsharp (smoothed) version of an image from the original image

e.g., printing and publishing industry

### □ Steps

- I. Blur the original image
- II. Subtract the blurred image from the original
- III. Add the mask to the original

# Image Filtering in Spatial Domain

## Unsharp Masking and Highboost Filtering

Let  $\bar{f}(x, y)$  denote the blurred image, unsharp masking is

$$g_{mask}(x, y) = f(x, y) - \bar{f}(x, y)$$

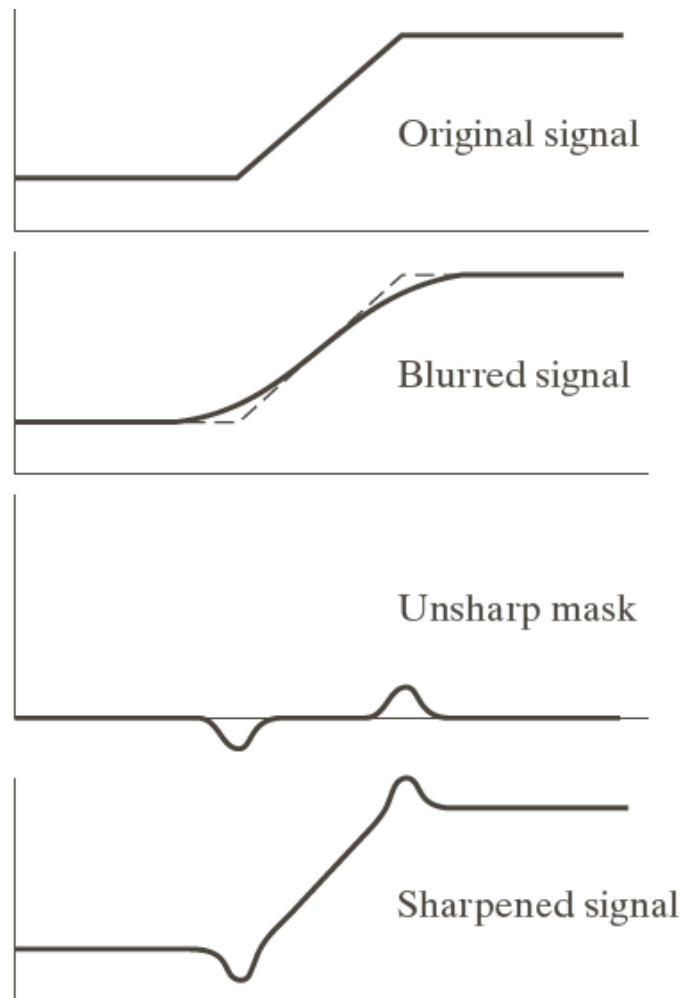
Then add a weighted portion of the mask back to the original

$$g(x, y) = f(x, y) + k * g_{mask}(x, y) \quad k \geq 0$$

when  $k > 1$ , the process is referred to as highboost filtering.

# Image Filtering in Spatial Domain

## Unsharp Masking and Highboost Filtering



a  
b  
c  
d

**FIGURE 3.39** 1-D illustration of the mechanics of unsharp masking. (a) Original signal. (b) Blurred signal with original shown dashed for reference. (c) Unsharp mask. (d) Sharpened signal, obtained by adding (c) to (a).

# Image Filtering in Spatial Domain

## Unsharp Masking and Highboost Filtering: Example



a  
b  
c  
d  
e

**FIGURE 3.40**

(a) Original image.

(b) Result of blurring with a Gaussian filter.

(c) Unsharp mask. (d) Result of using unsharp masking.

(e) Result of using highboost filtering.

# Image Filtering in Spatial Domain

## Image Sharpening based on First-Order Derivatives

For function  $f(x, y)$ , the gradient of  $f$  at coordinates  $(x, y)$  is defined as

$$\nabla f \equiv \text{grad}(f) \equiv \begin{bmatrix} g_x \\ g_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}$$

The *magnitude* of vector  $\nabla f$ , denoted as  $M(x, y)$

Gradient Image  $M(x, y) = \text{mag}(\nabla f) = \sqrt{g_x^2 + g_y^2}$



# Image Filtering in Spatial Domain

## Image Sharpening based on First-Order Derivatives

The *magnitude* of vector  $\nabla f$ , denoted as  $M(x, y)$

$$M(x, y) = \text{mag}(\nabla f) = \sqrt{g_x^2 + g_y^2}$$

$$M(x, y) \approx |g_x| + |g_y|$$

$z_1$	$z_2$	$z_3$
$z_4$	$z_5$	$z_6$
$z_7$	$z_8$	$z_9$

$$M(x, y) = |z_8 - z_5| + |z_6 - z_5|$$

# Image Sharpening based on First-Order Derivatives

$z_1$	$z_2$	$z_3$
$z_4$	$z_5$	$z_6$
$z_7$	$z_8$	$z_9$

$-1$	$0$
$0$	$1$

$0$	$-1$
$1$	$0$

$-1$	$-2$	$-1$
$0$	$0$	$0$
$1$	$2$	$1$

$-1$	$0$	$1$
$-2$	$0$	$2$
$-1$	$0$	$1$

a	
b	c
d	e

**FIGURE 3.41**

A  $3 \times 3$  region of an image (the  $z$ s are intensity values).

(b)–(c) Roberts cross gradient operators.

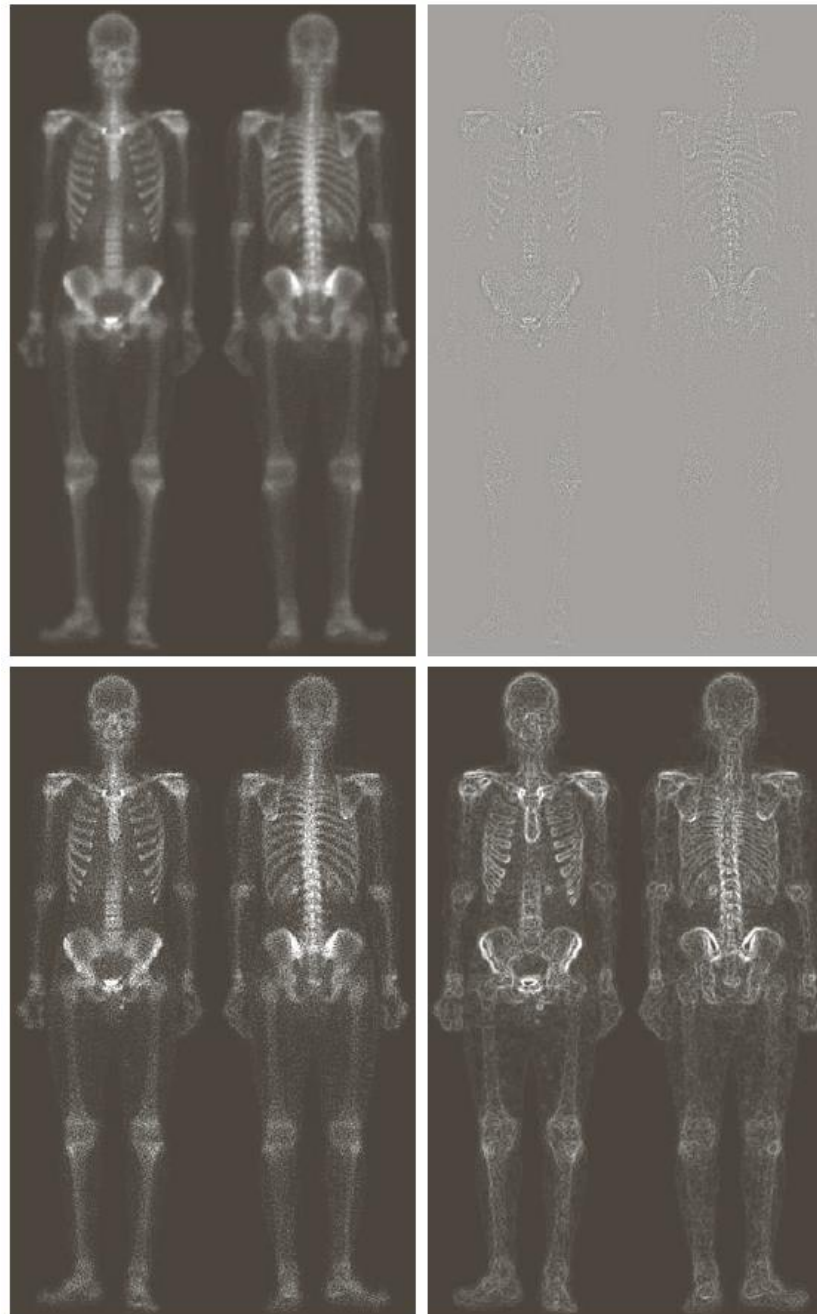
(d)–(e) Sobel operators. All the mask coefficients sum to zero, as expected of a derivative operator.

## Example

Combining  
Spatial  
Enhancement  
Methods

### Goal:

Enhance the  
image by  
sharpening it  
and by bringing  
out more of  
the skeletal detail



a	b
c	d

**FIGURE 3.43**

(a) Image of whole body bone scan.

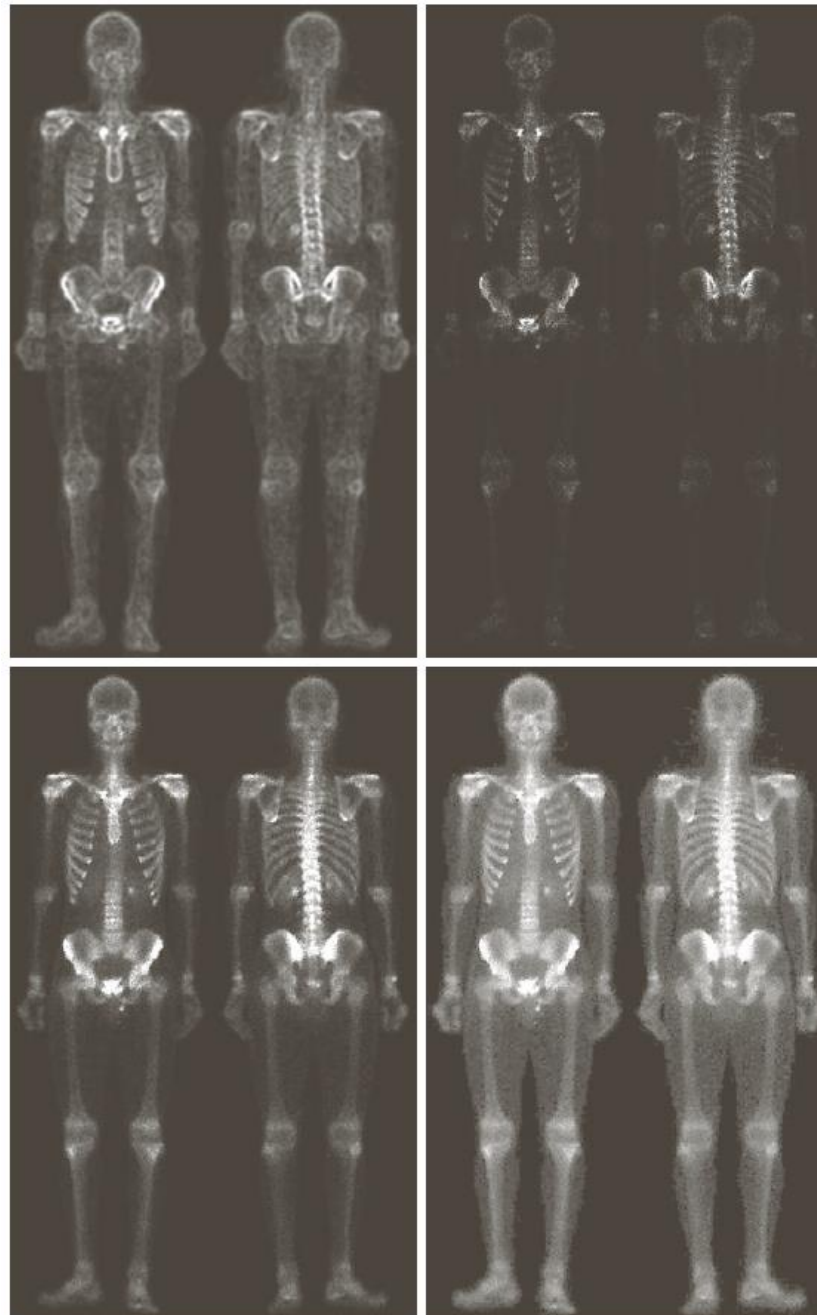
(b) Laplacian of (a). (c) Sharpened image obtained by adding (a) and (b). (d) Sobel gradient of (a).

## Example

### Combining Spatial Enhancement Methods

#### Goal:

Enhance the image by sharpening it and by bringing out more of the skeletal detail



e f  
g h

**FIGURE 3.43**

*(Continued)*

(e) Sobel image smoothed with a  $5 \times 5$  averaging filter. (f) Mask image formed by the product of (c) and (e).

(g) Sharpened image obtained by the sum of (a) and (f). (h) Final result obtained by applying a power-law transformation to (g). Compare (g) and (h) with (a). (Original image courtesy of G.E. Medical Systems.)

**Thank you: Question?**