

1.1

$$\theta_{1,1}^{(0)} = 0.3$$

$$\theta_{2,1}^{(0)} = 0.4$$

$$\beta_1^{(0)} = (1, 0, 0, 0)$$

$$\beta_2^{(0)} = (0, 0.4, 0.3, 0.3)$$

$$P(z=1 | A, d_1) = \frac{\beta_{1,A}^{(0)} \theta_{1,1}^{(0)}}{\sum_{z'} \beta_{z',A}^{(0)} \theta_{1,z'}^{(0)}} = \frac{1 \cdot 0.3}{1 \cdot 0.3 + 0 \cdot 0.7} = \boxed{1}$$

$$P(z=1 | B, d_1) = \frac{\beta_{1,B}^{(0)} \theta_{1,1}^{(0)}}{\sum_{z'} \beta_{z',B}^{(0)} \theta_{1,z'}^{(0)}} = \frac{0 \cdot 0.3}{0 \cdot 0.3 + 0.4 \cdot 0.7} = \boxed{0}$$

$$P(z=1 | C, d_1) = \frac{\beta_{1,C}^{(0)} \theta_{1,1}^{(0)}}{\sum_{z'} \beta_{z',C}^{(0)} \theta_{1,z'}^{(0)}} = \frac{0 \cdot 0.3}{0 \cdot 0.3 + 0.3 \cdot 0.7} = \boxed{0}$$

$$P(z=1 | D, d_1) = \frac{\beta_{1,D}^{(0)} \theta_{1,1}^{(0)}}{\sum_{z'} \beta_{z',D}^{(0)} \theta_{1,z'}^{(0)}} = \frac{0 \cdot 0.3}{0 \cdot 0.3 + 0.3 \cdot 0.7} = \boxed{0}$$

1.2

$$\beta_{1A}^{(1)} = \frac{\sum_d P(z=1|A,d) c(A,d)}{\sum_{w,d} P(z=1|w,d) c(w,d)} = \frac{1 \cdot 4 + 1 \cdot 2}{1 \cdot 4 + 1 \cdot 2 + 0 + 0 + 0 + 0 + 0 + 0} = \boxed{1}$$

$$\beta_{1B}^{(1)} = \frac{\sum_d P(z=1|B,d) c(B,d)}{\sum_{w,d} P(z=1|w,d) c(w,d)} = \frac{0 \cdot 3 + 0 \cdot 2}{1 \cdot 4 + 1 \cdot 2 + 0 + 0 + 0 + 0 + 0 + 0} = \boxed{0}$$

$$\theta_{11}^{(1)} = \frac{\sum_w P(z=1|w, d_1) c(w, d_1)}{N_{d_1}} = \frac{1 \cdot 4 + 0 \cdot 3 + 0 \cdot 2 + 0 \cdot 1}{10} = \boxed{0.4}$$

$$\theta_{12}^{(1)} = \frac{\sum_w P(z=2|w, d_1) c(w, d_1)}{N_{d_1}} = \frac{0 \cdot 4 + 1 \cdot 3 + 1 \cdot 2 + 1 \cdot 1}{10} = \boxed{0.6}$$