

Assignment No. 04

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Title: Expression tree creation & traversal

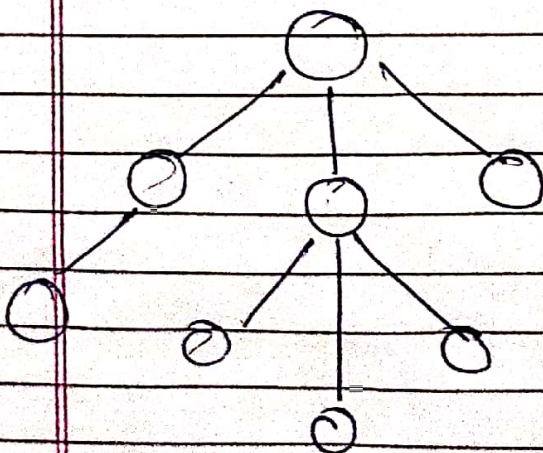
Aim: To implement a expression tree using Stack data structure.

Problem Statement: Construct an expression tree for postfix expression ~~tree~~ for post^{fix} perform recursive and non-recursive inorder, preorder & postorder traversal

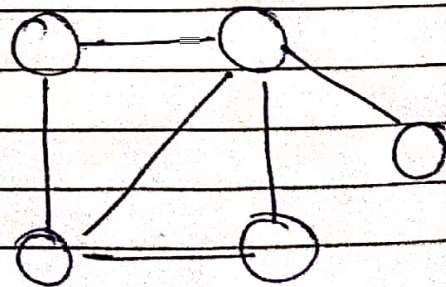
Theory:

concept of non-linear data structure with ex:

- ① Data structure where data elements are not arranged linearly or sequentially are called non-linear data structures
- ② In Non-linear data structure, singly level is not evolved, therefore we can't traverse all the elements in single runs only.
- ③ But it utilizes computer memory efficiently in comparison to linear data structures



Tree



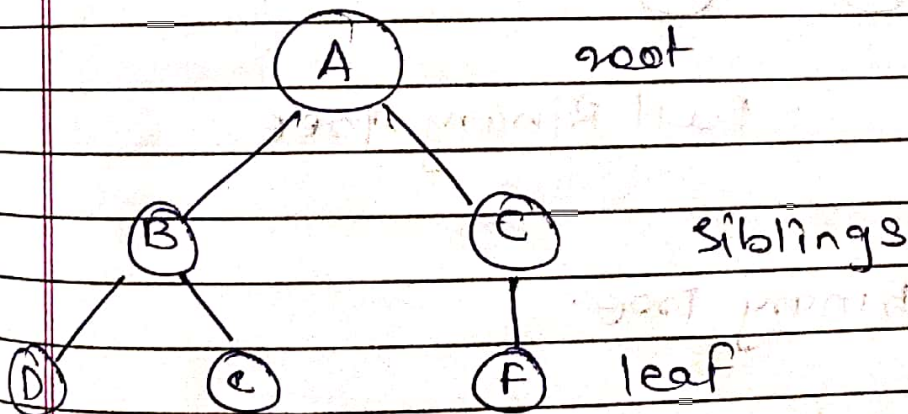
graph

Binary Tree :

Tree in which any node can have at most two branches, i.e. at most two children is a binary tree

Defination :

A binary tree is a finite set of nodes that is either empty or consist of root and two disjoint binary trees called 'left subtree' & 'right subtree'

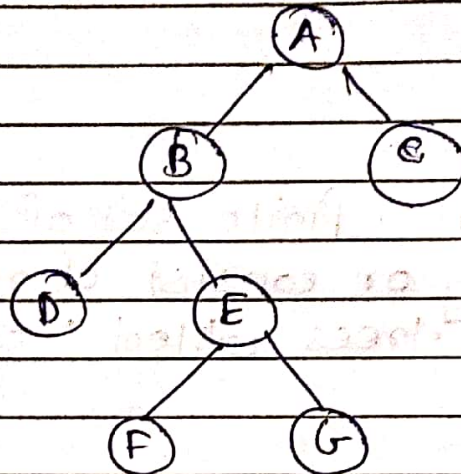


Terminologies:

- 1) Root: Node without parent
- 2) Sibling: Nodes share same parents
- 3) Internal Nodes: Nodes with at least one child
- 4) External Nodes: Nodes without children
- 5) Ancestors of node: Parent, grandparent.
- 6) Depth of node: Number of edges from root node
- 7) Height of tree: Maximum depth of any node

Full Binary Tree:

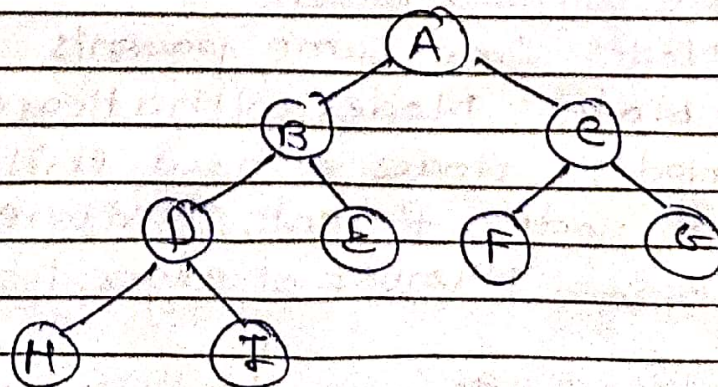
A binary tree is full binary tree if every node has zero or two children



Full Binary Tree

Complete Binary Tree:

A complete binary tree is a binary tree which is completely filled with the possible exception of bottom level which is filled left to right



Complete Binary tree

Binary Tree ADT:

Structure Binary tree is a set of nodes either or consisting of root, left binary tree & right binary tree.

Operations

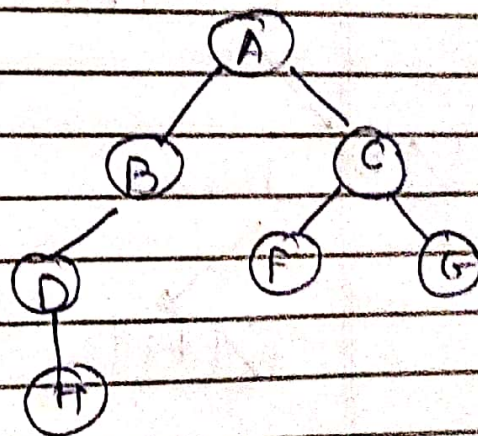
Realization of ADT with binary:

If binary tree with 'n' nodes is represented sequentially, then for any node with index i , $1 \leq i \leq n$, we have:

parent is at $\lceil i/2 \rceil$

left child is at $2i$

right child is at $2i+1$



Array Representation:

0	1	2	3	4	5	6
A	B	C	D	E	F	G

Realization of ADT with linked list:

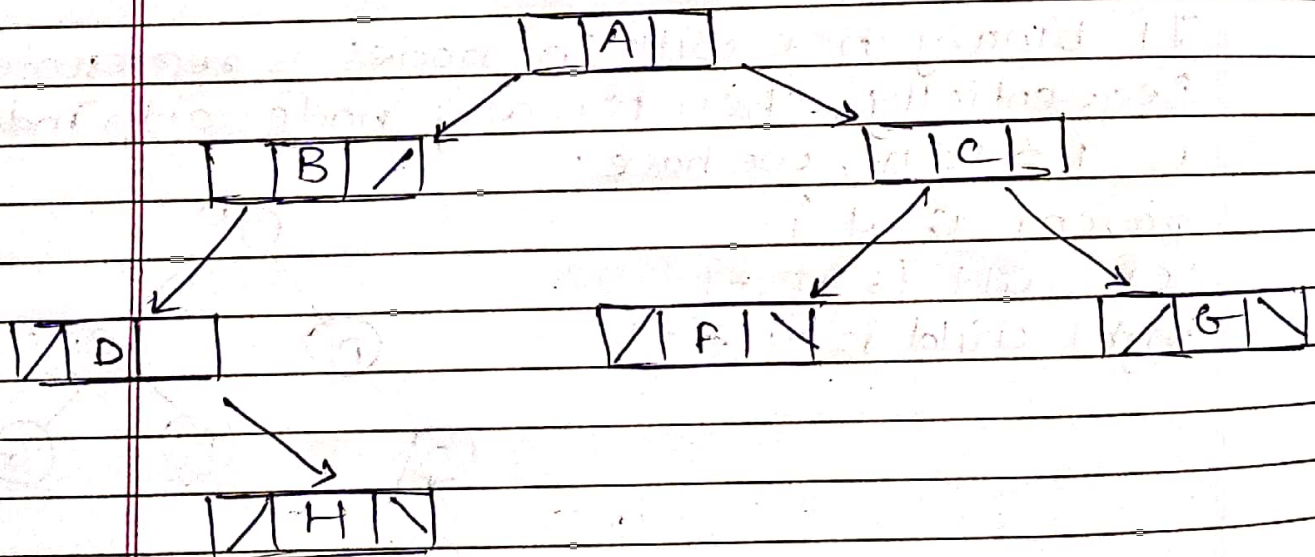
Binary Tree is called linked list representation are stored in memory as linked list. These list are linked to each other through parent child relationship associate with trees.

Each node has these three path

- ① Data element.
- ② pointer that points towards left node.
- ③ pointer that points towards right node

left child	data	right child
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Linked list representation:



Binary tree Applications:

- 1) A binary tree is useful data structure when to way decisions must be made at each point in process.

Ex. Finding duplicates in list of members

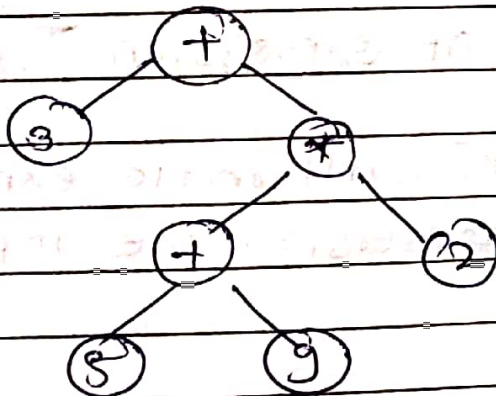
- 2) A binary tree can be used for representation of expression containing operands (leaf) and operator (internal node)

Expression Tree concepts:

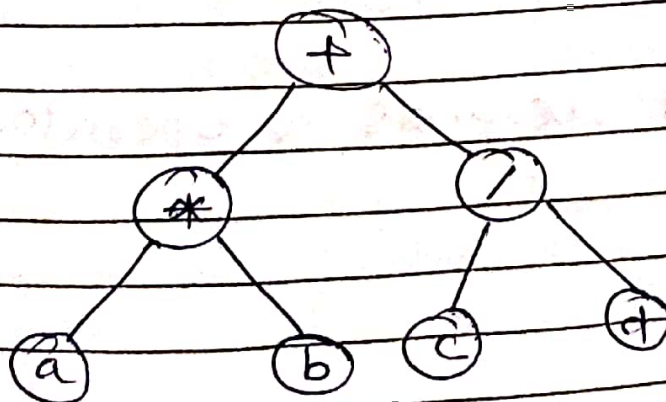
An expression tree is a representation of expression arrange in a tree like data structure

It is binary tree in which internal nodes corresponding to the operator and each leaf node corresponds to the operators

eg Infix $3 + ((5 + 9) * 2)$

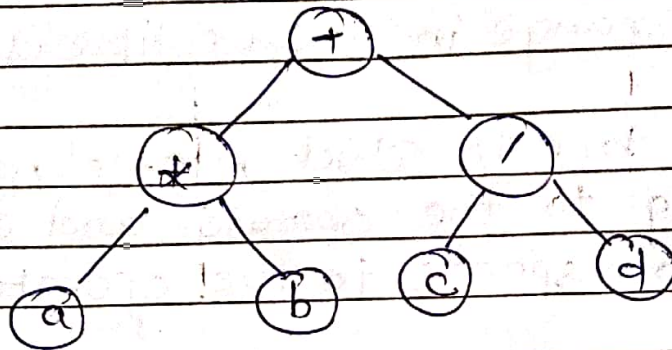


Example of prefix expression
 $+ * ab / cd$



Example of postfix expression :

$ab * cd / +$



Applications of expression Tree :

- 1) Evaluation of arithmetic expression
- 2) Expression conversion i.e. infix to postfix or prefix

Test cases / validations :

- 1) validation :

Number of operands & operators relationship

- 2) Test cases :

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Infix Expression	postfix Expression	Prefix Expression
1) $A + B * C$	$ABC * +$	$+ A * CB$
2) $A * B - C$	$AB * C -$	$- * ACB$
3) $A \wedge B - C$	$AB \wedge C -$	$- \wedge ABC$
4) $A + B \rightarrow C \wedge E$	$ABCE \wedge * +$	$+ A * B \wedge CE$
5) $A - B * C + A$	$ABC * - A +$	$- + A * BCA$
6) $(A + B) / (C + D) \wedge E \wedge F$	$AB + CD + EF \wedge \wedge /$	$/ + AB + CD \wedge EF *$
7) $- D * F - D$	$- D -$	$D F D$
8) $A + B + C$	$AB + C +$	$+ + ABC$
9) $A * B / C$	$AB * C /$	$/ * ACD$
10) $A \wedge B \wedge C$	$ABC \wedge \wedge$	$\wedge \wedge ABC$

Conclusion :

Using Binary tree it is possible to build an expression tree. Transversal or tree gives expression in various forms i.e Inorder traversal for prefix expression preorder traversal for prefix expression, postorder traversal for