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Seat No.

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S.E. (Computer/IT Engineering) (Second Semester)

EXAMINATION, 2017

ENGINEERING MATHEMATICS III

(2015 Course)

Time: Two Hours

Maximum Marks: 50

- **N.B.** :— (i) Neat diagrams must be drawn wherever necessary.
 - (ii) Figures to the right indicate full marks.
 - Your answers will be valued as a whole. (iii)
 - Use of electronic pocket calculator is allowed. (iv)
 - Assume suitable data, if necessary. (v)
- (a) Solve any two: 1.

[8]

(i)
$$\frac{d^2y}{dx^2} + 3\frac{dy}{dx} + 2y = 2e^{e^x}$$
(ii)
$$(D^2 + 4D + 4)y = x^{-3} e^{-2x}$$

(ii) (D² + 4D + 4)
$$y = x^{-3} e^{-2x}$$

(iii)
$$x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$$

(*b*)

(iii)
$$(D^2 + 4D + 4)y = x^{-3} e^{-2x}$$

(iii) $x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$
Find the Fourier transform of: [4]
 $f(x) = 1, \qquad |x| \le 1$
 $= 0, \qquad |x| > 1$
and evaluate $\int_0^\infty \frac{\lambda \cos \lambda x}{\lambda} d\lambda$.
P.T.O.

- 2. (a) An inductor of 0.5 henries is connected in series with a registor of 6 ohms, a capacitor of 0.02 farads, a generator having alternative voltage given by 24 sin 10 t, t > 0 and switch k. Set up a differential equation for this circuit and find charge at time t. [4]
 - (b) Solve any one of the following: $(i) \quad \text{Find } z\{f(k)\}, \text{ where } f(k) = 3^k, k < 0$ $= 2^k, k \ge 0$
 - (ii) Find:

$$z^{-1}\left\{\frac{z^2}{z^2+1}\right\}$$

by using inversion integral method.

- (c) Solve the following difference equation: y(k + 2) 5y(k + 1) + 6y(k) = 36y(0) = y(1) = 0.
- 3. (a) Calculate the first four central moments from the following data and hence find β_1 and β_2 : [4]

x	0	1	2	3	4	5	6
f	5	15	17	25	19	14	5

(b) Fit a straight line to the following data by least square method: [4]

x	0	5	10	15	20	2 5
у	12	15	17	22 (24	30

- (c) The number of breakdowns of a computer in a week is a Poisson variable with $\lambda = np = 0.3$. What is the probability that the computer will operate: [4]
 - (i) with no breakdown and
 - (ii) at the most one breakdown in a week.

Or

- 4. (a) The average test marks in a particular class is 79 and standard deviation is 5. If the marks are normally distributed, how many students in a class of 200, did not receive marks between 75 and 82. Given z = 0.8, Area = 0.2881 and z = 0.6, Area = 0.2257.
 - (b) An insurance agent accepts policies of 5 men of identical age and in good health. The probability that a man of this age will be alive 30 years hence is 2/3. Find the probability that in 30 years:

 [4]
 - (i) all five men and
 - (ii) at least one man will be alive.
 - (c) The two variables x and y have regression lines: [4] 3x + 2y 26 = 0 and 6x + y 31 = 0

Find:

- (i) the mean values of x and y and
- (ii) correlation coefficient between x and y.
- **5.** (a) Find the directional derivative of a scalar point function $\phi = xy^2 + yz^3$ at (2, -1, 1) in the direction of a vector 4i + 2j + 4k.

[5252]-566 P.T.O.

(*b*) Show that the vector field:

$$\overline{F} = (6xy + z^3)i + (3x^2 - z)j + (3xz^2 - y)k$$

is irrotational and hence find a scalar potential function ϕ such that $\overline{F} = \nabla \phi$, [4]

Find the work done by the vector field: (c) [5] $\mathbf{F} = (x^2 - yz)i + (y^2 - zx)j + (z^2 - xy)k$

in moving a particle of unit mass from (1, 1, 1) to (2, -1, 2).

- Find the directional derivative of a scalar point function 6. $\phi = xy - z^2 + 2xz$ at (1, 0, 2) in the direction of 4i - j[4]
 - Show that (any one): (*b*)
 - w that (any *one*): [4] $\nabla \left(\frac{\overline{a}.\overline{r}}{r^{n}}\right) = \frac{\overline{a}}{r^{n}} \frac{n(\overline{a}.\overline{r})\overline{r}}{r^{n+2}}, \text{ where } \overline{a} \text{ is a constant vector.}$
 - Evaluate the integral $\int_{c}^{\overline{F}. d\overline{r}}$, along the curve x = 2t, (c) y = t, z = 3t from t = 0 to t = 1, where $\overline{F} = 3x^2i$ $u = -2xy + \frac{y}{x^2 + y^2},$ hat f(z) = u + i+ (2xz - y)j + zk.[5]
- 7. If:(a)

$$u = -2xy + \frac{y}{x^2 + y^2},$$

find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z. [4]

Evaluate $\oint_{C} \frac{e^{z}}{(z+1)(z+2)} dz$, where c is the contour (*b*)

$$|z+1| = \frac{1}{2}.$$
 [5]

Find the Bilinear transformation which maps the point (c) -i, 0, 2 + i of the z-plane onto the points 0, -2i, 4 of the [4]

8.

$$u = \frac{1}{2}\log(x^2 + y^2),$$

 $u = \frac{1}{2}\log(x^2 + y^2),$ find v such that f(z) = u + iv is analytic. Determine f(z) in terms of z. [4]

Evaluate $\oint_{\mathbb{C}} \frac{\sin \pi z^2 + 2z}{(z-1)(z-2)} dz$, where c is the circle |z| = 4. (*b*)

[5]

Find the image of the circle $(x - 3)^2 + y^2 = 2$ under the (c) And the state of t transfromation $w = \frac{1}{z}$.