

**Siddhi Singh**

**17BIT0028**

**Lab 3**

# ADDERS

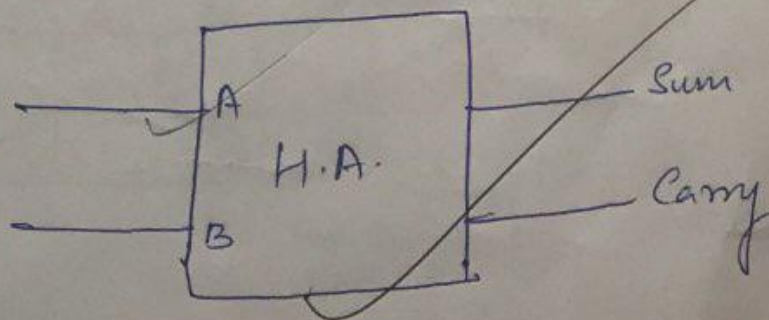
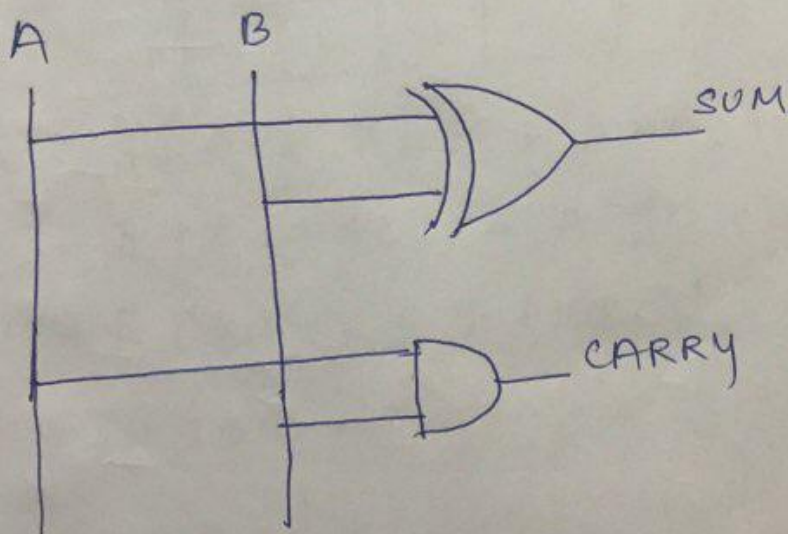
Exp-3.

## HALF ADDER

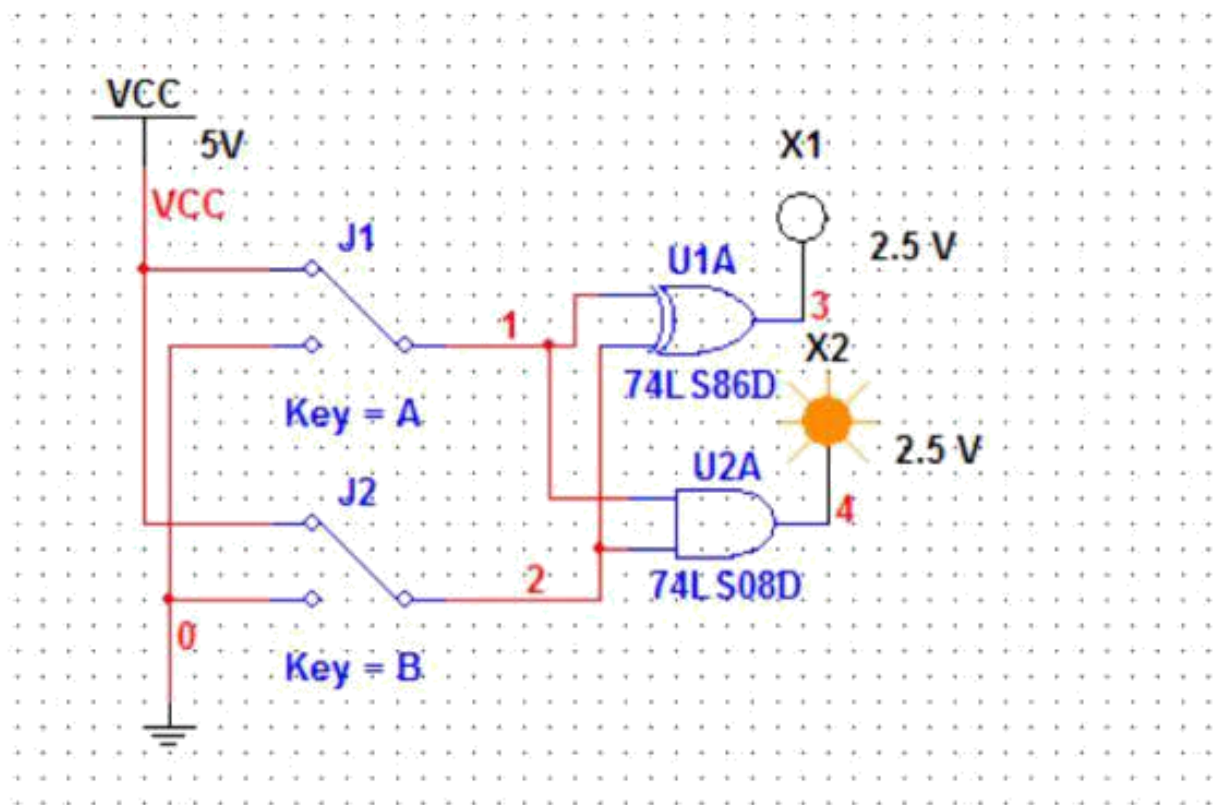
A	B	Carry	Sum
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

$$\begin{aligned} \text{SUM} &= \bar{A}B + A\bar{B} \\ &= A \oplus B \end{aligned}$$

$$\text{CARRY} = AB$$



# 1 ) HALF ADDER



# FULL ADDER

A	B	CARRY IN	CARRY OUT	SUM
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

SUM :-  $\Sigma (1, 2, 4, 7)$

	BC	00	01	11	10
A	0		1		1
	1	1		1	

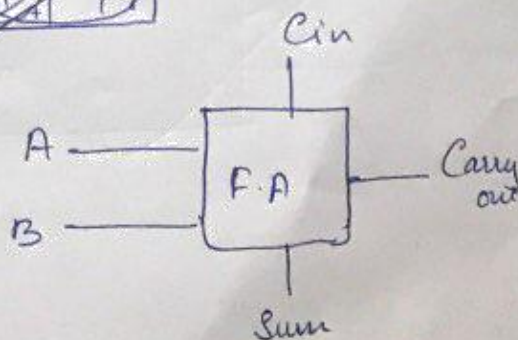
$$\begin{aligned}
 \text{SUM} &= \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC \\
 &= \bar{A}(\bar{B}C + B\bar{C}) + A(\bar{B}\bar{C} + BC) \\
 &= \bar{A}(B \oplus C) + A(B \oplus C)' \\
 &= A \oplus B \oplus C
 \end{aligned}$$

CARRY :-  $\Sigma (3, 5, 6, 7)$

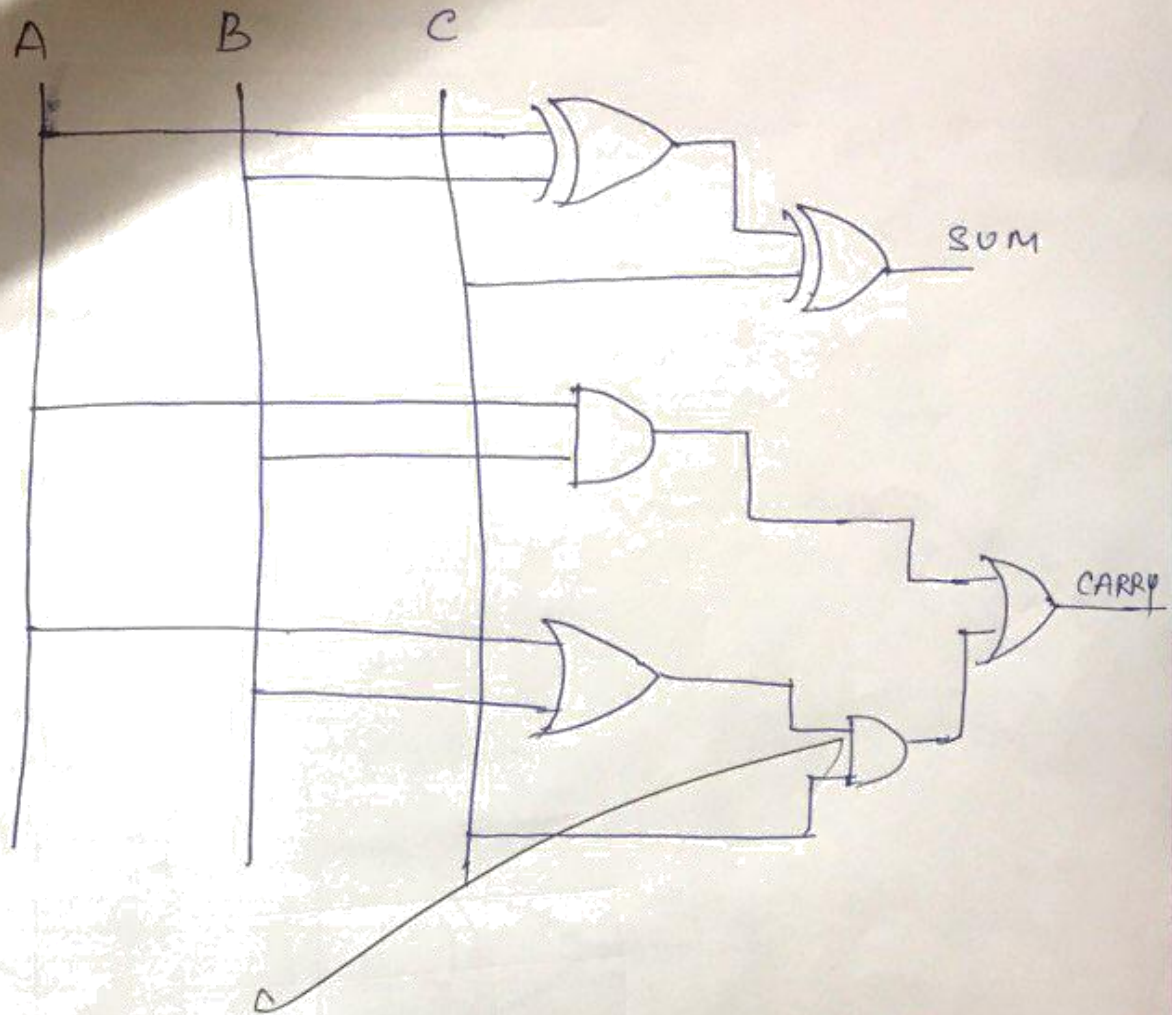
	BC	$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	$BC$
A	$\bar{A}$		1	1	
	A	1	1	1	1

$$\text{Carry} = AC + BC + AB$$

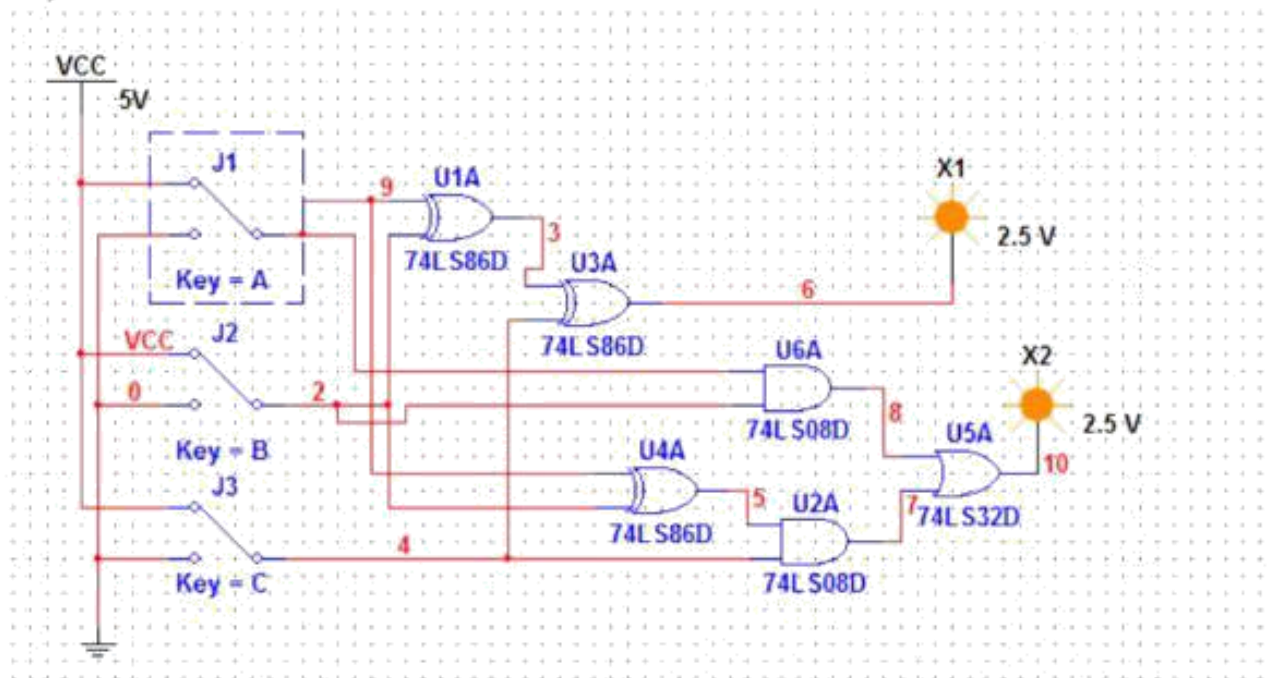
$$= C(A + B) + AB$$







## 2 ) FULL ADDER

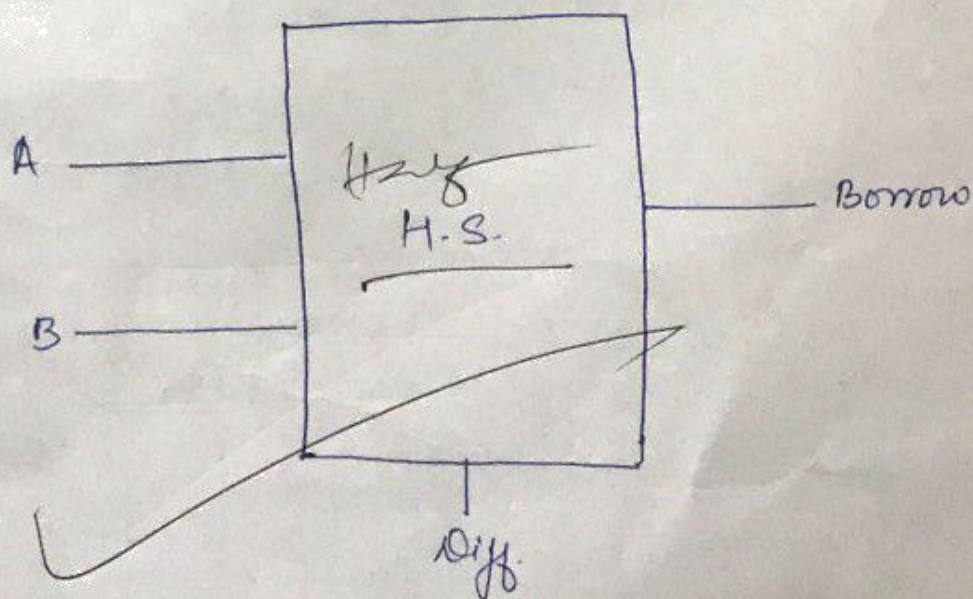
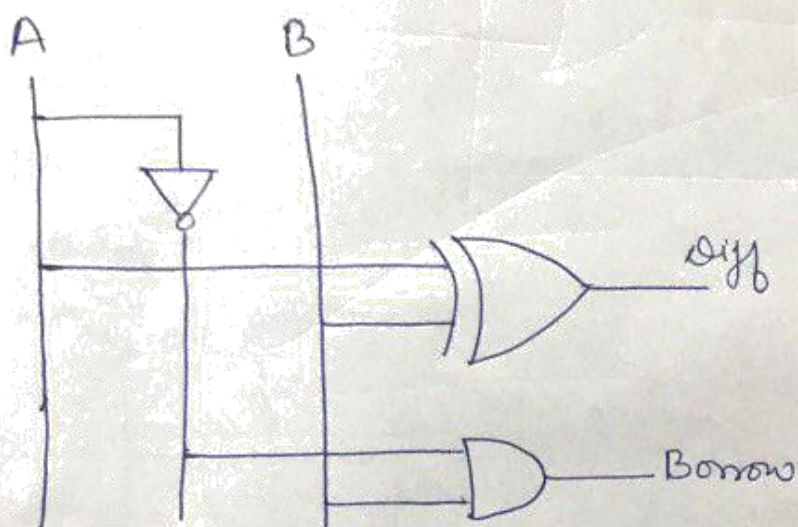


# HALF SUBTRACTOR

A	B	Borrow	Diff
0	0	0	0
0	1	1	1
1	0	0	1
1	1	0	0

$$\begin{aligned}\text{Diff} &= \bar{A}B + A\bar{B} \\ &= A \oplus B\end{aligned}$$

$$\text{Borrow} = \bar{A}B$$









# FULL SUBTRACTOR

A	B	C (Borrow in)	Borrow (out)	diff
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	1	0
1	0	0	0	1
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

$$\text{diff} :- \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}C + ABC$$

$$= \Sigma(1, 2, 4, 7)$$

A \ BC				
	$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	$BC$
$\bar{A}$		1		1
A	1		1	

$$= \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}C + ABC$$

$$= \bar{A} \{ \bar{B}C + B\bar{C} \} + A \{ \bar{B}\bar{C} + BC \}$$

$$= \bar{A} \{ B \oplus C \} + A \{ B \oplus C \}$$

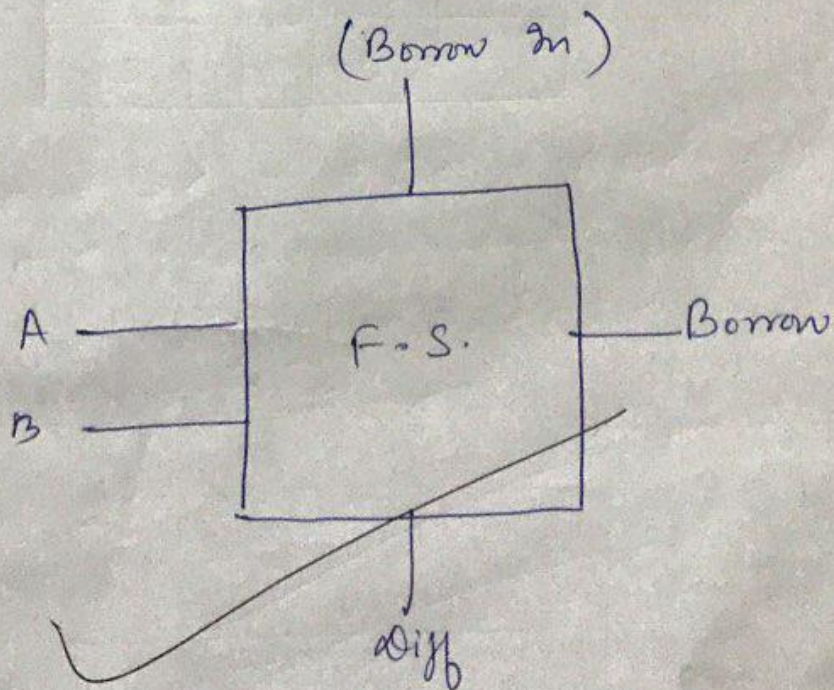
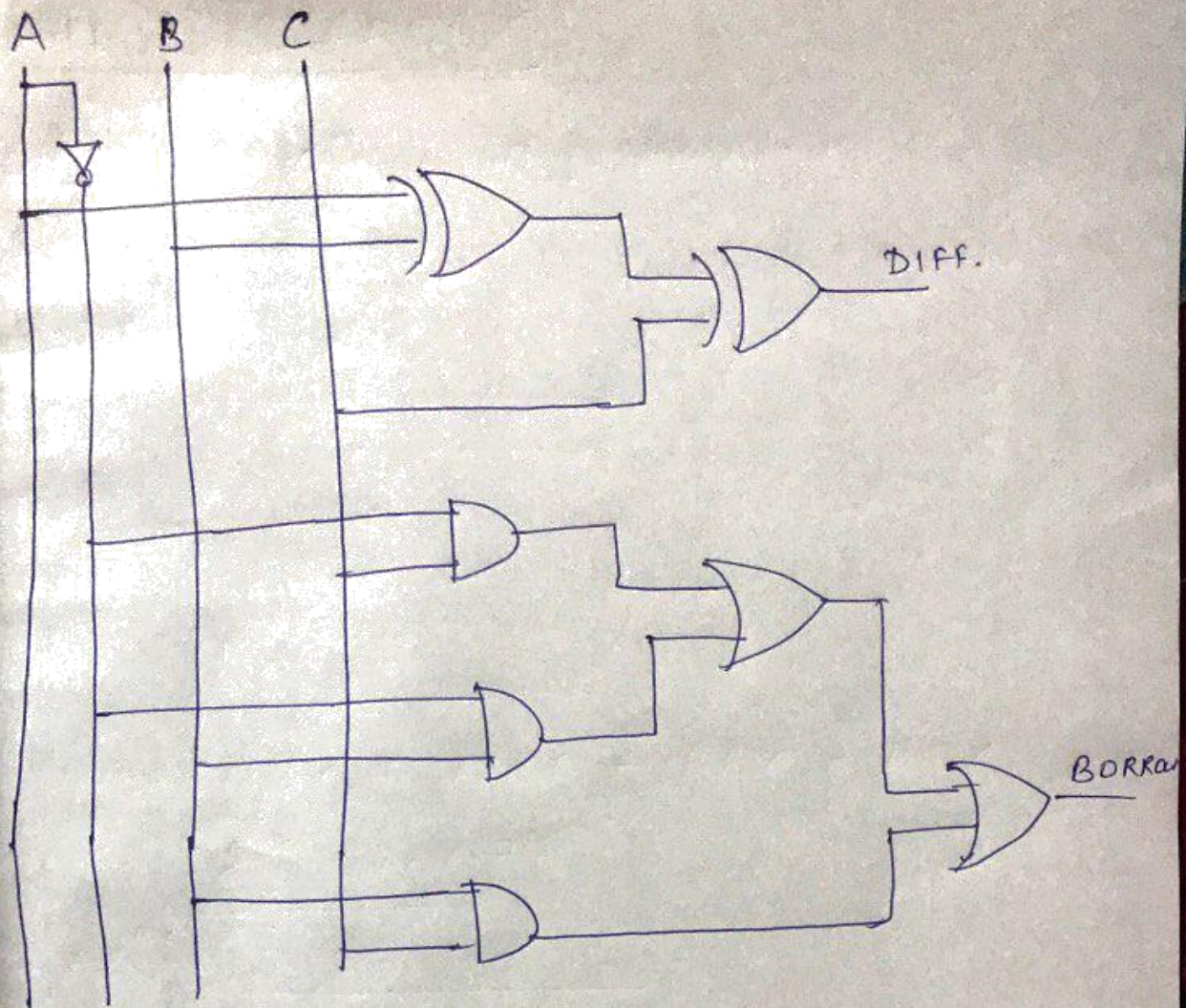
$$= A \oplus B \oplus C$$

Borrow:  $\Sigma(1, 2, 3, 7)$

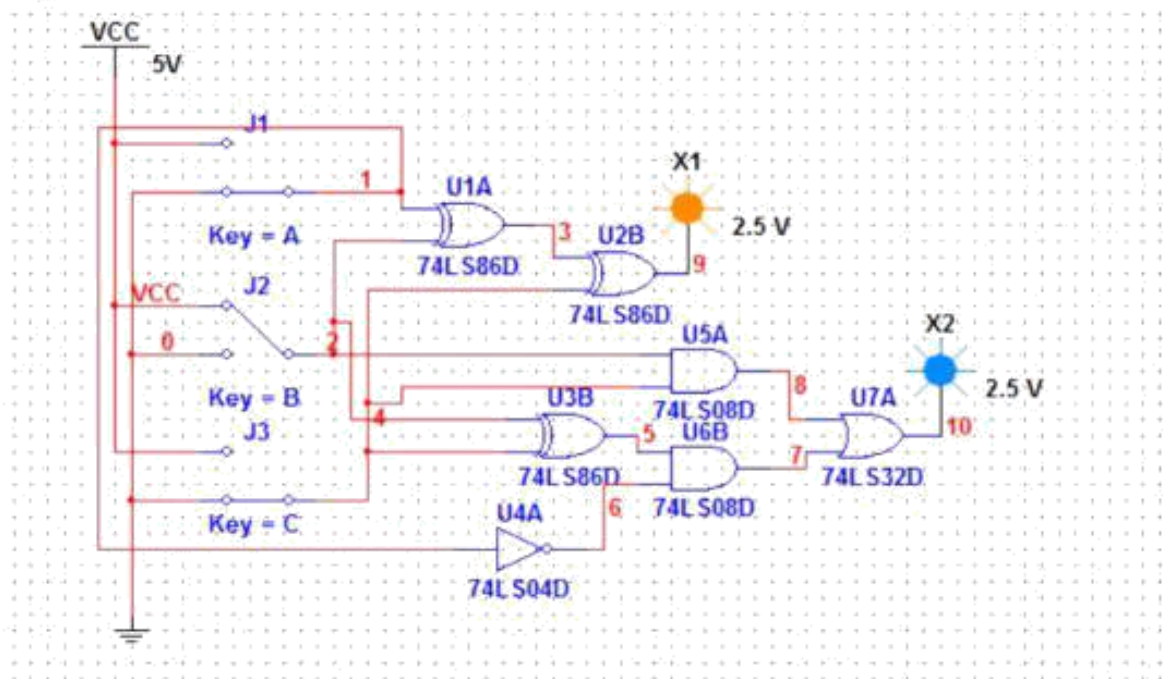
A \ BC				
	$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	$BC$
$\bar{A}$		1	1	1
A			1	

$$= \bar{A}C + \bar{A}B + BC$$





#### 4) FULL SUBTRACTOR





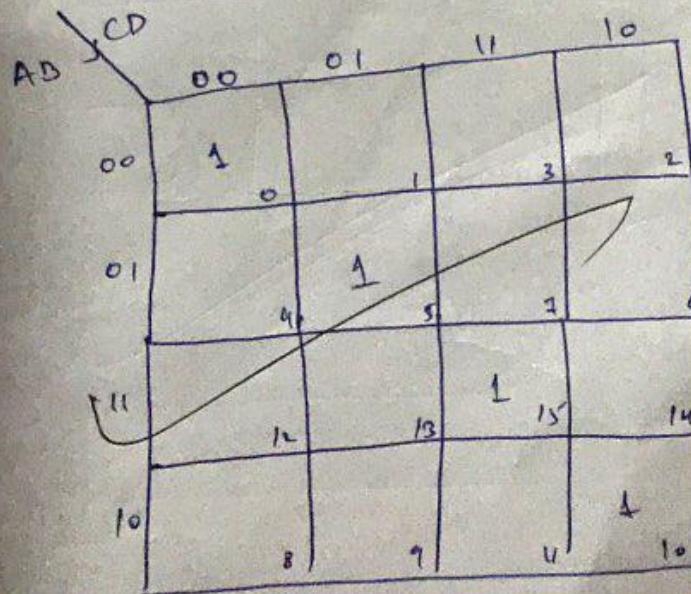
Exp-4.

# MAGNITUDE COMPARATOR

(2 bit Magnitude Comparator)

A		B				
A <sub>0</sub>	A <sub>1</sub>	B <sub>0</sub>	B <sub>1</sub>	A = B	A > B	A < B
0	0	0	0	1	0	0
0	0	0	1	0	0	1
0	0	1	0	0	0	1
0	0	1	1	0	0	1
0	1	0	0	0	1	0
0	1	0	1	1	0	0
0	1	1	0	0	0	1
0	1	1	1	0	0	1
1	0	0	0	0	1	0
1	0	0	1	0	1	0
1	0	1	0	1	0	0
1	0	1	1	0	1	0
1	1	0	0	0	1	0
1	1	0	1	0	1	0
1	1	1	0	0	1	0
1	1	1	1	1	0	0

For A = B :  $\Sigma (0, 5, 10, 15)$



$$= \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D$$

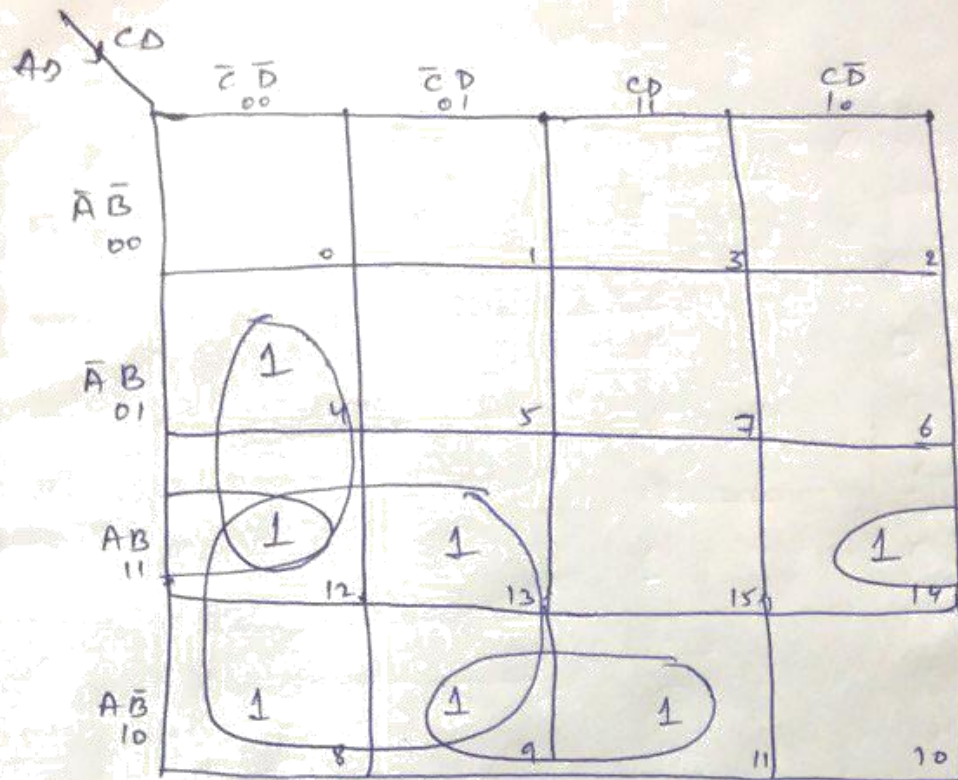
$$= \bar{A}\bar{C}(\bar{B}\bar{D} + BD) + A\bar{C}(B\bar{D} + \bar{B}D)$$

$$= (\bar{B}\bar{D} + BD) + (\bar{A}\bar{C} + AC)$$

$$= (B \oplus D)' + (A \oplus C)$$

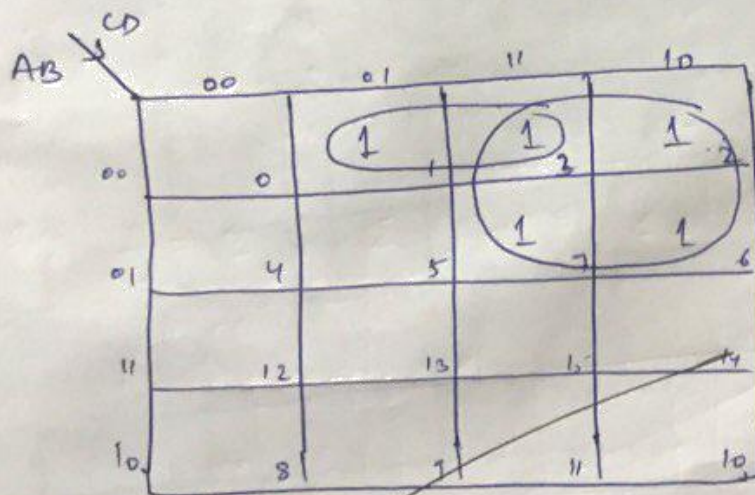


For  $A > B : \Sigma(4, 8, 9, 11, 12, 13, 14)$

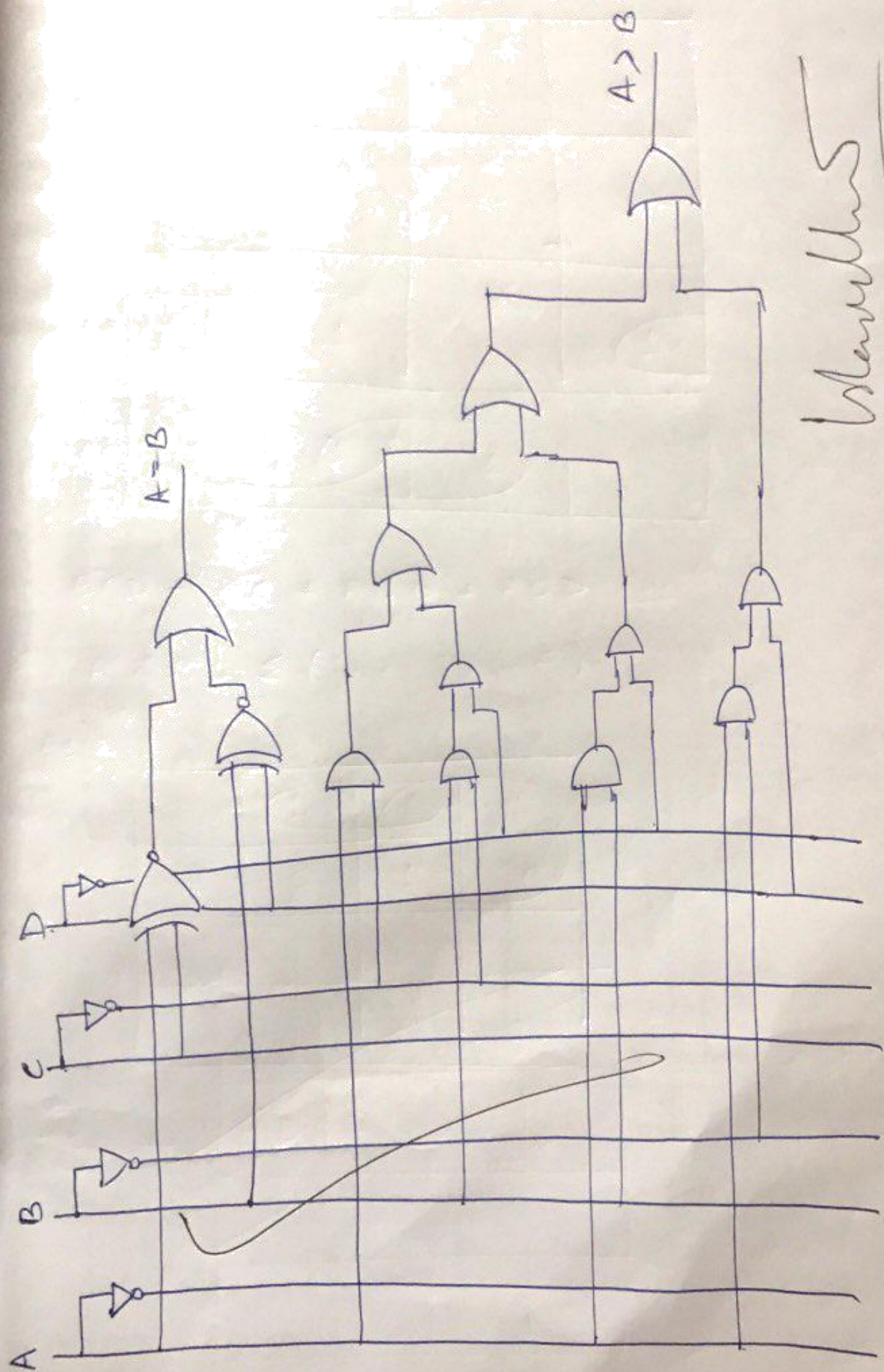


$$\overline{B}\overline{C}\overline{D} + A\overline{C} + AB\overline{D} + A\overline{B}D \text{ ans.}$$

For  $A < B : \Sigma(1, 2, 3, 6, 7)$

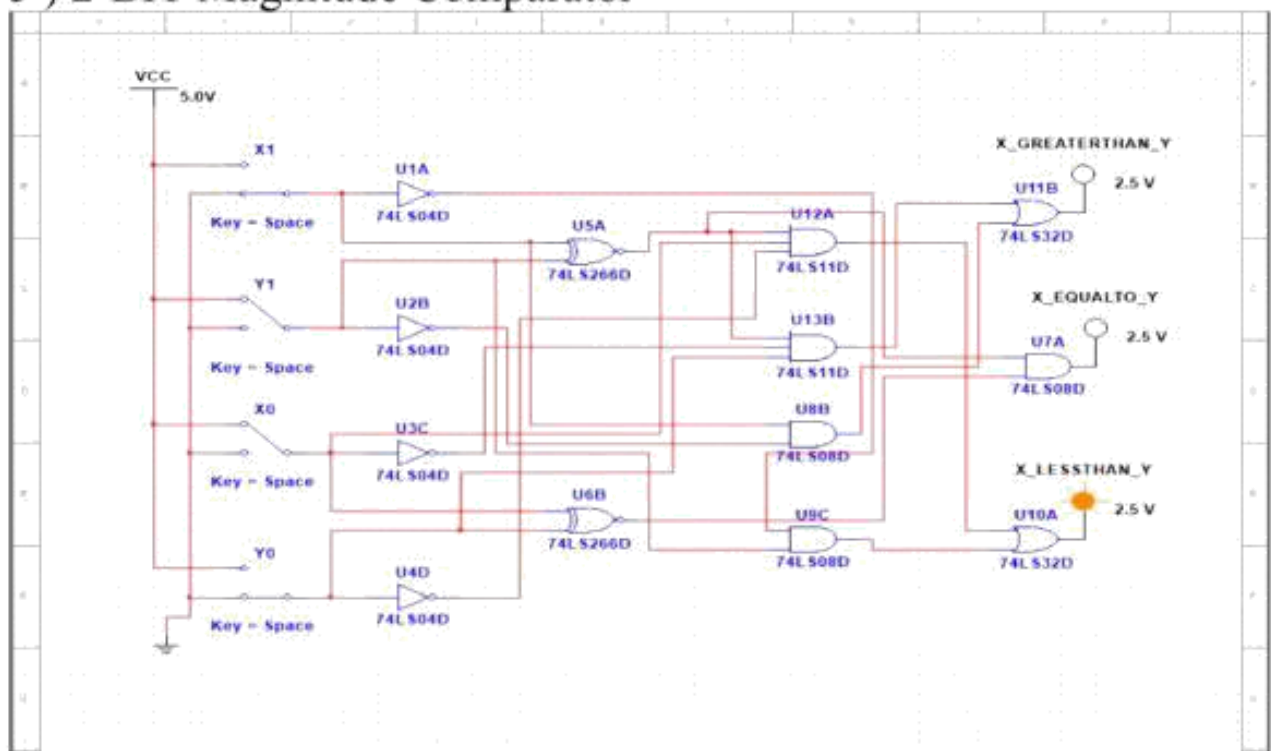


$$\overline{A}\overline{B}D + A\overline{B}D + AC \text{ ans.}$$



Wanvllus

## 5 ) 2-BIT Magnitude Comparator





# (4-bit Magnitude Comparator)

Using 4, 1-bit magnitude comparators  
for 1 bit magnitude comparator

A	B	$A < B$	$A > B$	$A = B$
0	0	0	0	1
0	1	1	0	0
1	0	0	1	0
1	1	0	1	1

$$F(A < B) = \bar{A}B, \quad F(A > B) = A\bar{B}, \quad F(A = B) = A \oplus B$$

