# STATISTICAL DATA MINING – I HOMEWORK IV

NAME: SIDDIQ SYED

UB Person # 50291566

Class # 50

1) (20 points) (Exercise 7.9) For the prostate data of Chapter 3, carry out a bestsubset linear regression analysis, as in Table 3.3 (third column from the left). Compute the AIC, BIC, five- and tenfold cross-validation, and bootstrap .632 estimates of prediction error.

Exploratory analysis of the data

Loading the data in to R studio for which the column train has TRUE and FALSE values which says that the model that can be used for prediction should be of classification.

```
1cp gleason pgg45
 lcavol lweight age lbph svi
                                              lpsa train
1 -0.580
          2.77
               50 -1.39 0 -1.39
                                     6 0 -0.431 TRUE
2 -0.994
          3.32 58 -1.39 0 -1.39
                                     6
                                          0 -0.163 TRUE
                                     7
3 -0.511
         2.69 74 -1.39 0 -1.39
                                        20 -0.163 TRUE
4 -1.204
         3.28 58 -1.39 0 -1.39
                                     6
                                          0 -0.163 TRUE
5 0.751
         3.43 62 -1.39 0 -1.39
                                          0 0.372 TRUE
                                     6
         3.23 50 -1.39 0 -1.39
                                          0 0.765 TRUE
6 -1.050
                                     6
```

Figure 1: Head data for prostate dataset

The train column needs to be converted into numeric binary form for easy application of model building.

Building exhaustive subset model to check what are the most important parameters that are required to train the best model for the given dataset.

(1)	lcavol	lweight		]bph		]cp	gleason ""	pgg45	lpsa ""
(2)								п <sub>ф</sub> п	
(1)							пфп	n <sub>†</sub> n	
(2)			$\mathbf{u}_{\frac{1}{N}}\mathbf{u}$	п <sub>ф</sub> п					
(1)			"*"		" "	" "	n* n	n & n	
(2)			" "		" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(1)			$^{\rm H} \otimes^{\rm H}$		" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(2)			$^{\rm H} \otimes^{\rm H}$	n & n	" "	" "	n <sub>†</sub> n	n & n	
(1)			$^{\rm H} \otimes^{\rm H}$	n & n	" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(2)	" n		$\mathbf{u}_{\frac{1}{N}}\mathbf{u}$	n <sub>&amp;</sub> n	" "	" "	n <sub>†</sub> n	n & n	
(1)		n <sub>†</sub> n	п <sub>ф</sub> п	n & n	" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(2)	"#"		п <sub>ф</sub> п	n & n	" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(1)		n <sub>†</sub> n	п <sub>ф</sub> п	n & n	" * "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(2)	n & n	n <sub>†</sub> n	п <sub>ф</sub> п	n & n	" "	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(1)	n & n	n <sub>†</sub> n	$^{\rm H} \times ^{\rm H}$	n & n	п <sub>ф</sub> п	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	
(2)		n <sub>†</sub> n	$^{\rm H} \otimes^{\rm H}$	n & n	п <sub>ф</sub> п	п <sub>ф</sub> п	n <sub>†</sub> n	n & n	n & n
(1)	n & n	"*"	$\mathbf{u}_{\frac{1}{N}}\mathbf{u}$	n & n	" * "	***	"*"	n & n	n & n
Indiana Zan									

From the above image it is to be seen that the column age and pgg45 are the best single parameter models for the dataset. And like wise for 2,3.. can be observed in the above image.

Observing the training and test errors for the dataset with different combinations for the above obtained important parameters.

It is observed below that for age, gleason and pgg45 parameters used for model building with linear regression below are the errors obtained.

```
> test.error_lm
[1] 0.164
> train.error_lm
[1] 0.21
```

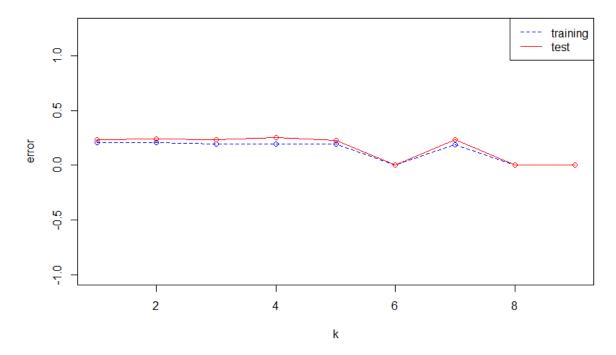
And for 4 best subset model below are the errors obtained.

```
> test.error_lm
[1] 0.159
> train.error_lm
[1] 0.209
```

Which is evident that the error rate has been decreased.

Applying 5 fold cross-validation for the model building of each best subset linear regression model we can see the below graph between error and number of parameters.

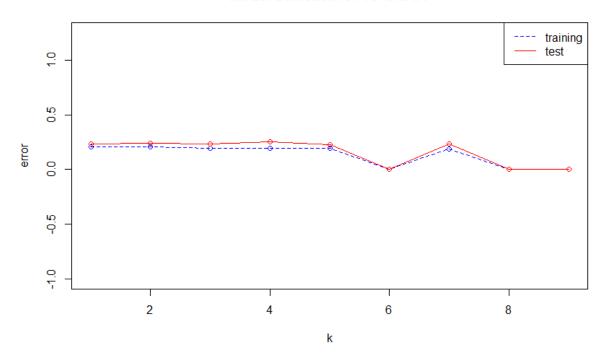
#### Model Selection for 5 fold CV



From the above plot it is evident that the error is very least for 6 8 and 9 parameters.

Let's see for the 10 fold CV of the same.

#### Model Selection for 10 fold CV



From the two graphs it is evident that the error rate is same for both 5 and 10 folds.

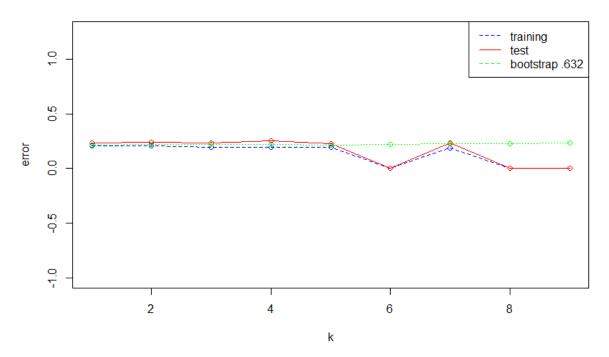
Looking at the CP and BIC values for the exhaustive subset model for increasing number of parameters.

```
> my_summary$cp
[1] -0.150 -0.238  0.567  1.629  2.835  4.431  6.157  8.073  10.000
> my_summary$bic
[1]  6.44  8.54  11.58  14.87  18.32  22.21  26.24  30.48  34.74
> which.min(my_summary$cp) #Cp says  2 variables is best
[1]  2
> which.min(my_summary$bic)
[1]  1
```

Above values clearly says that the 2 and 1 parameter models are the best. As per the cross validation errors 6, 8 and 9 were the lowest error rate models.

From bootstrap .632 prediction error which is plotted below.

#### **Model Selection**



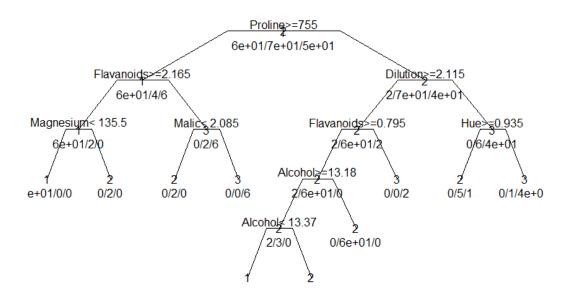
The green line which has almost the constant rate of prediction error which for this dataset is not able to perform effectively with bootstrap .632 prediction errors.

2) (10 points) A access the wine data from the UCI machine learning repository (https://archive.ics.uci.edu/ml/datasets/wine). These data are the results of a chemical analysis of 178 wines grown over the decade 1970-1979 in the same region of Italy, but derived from three different cultivars (Barolo, Grignolino, Barbera). The Babera wines were predominately from a period that was much later than that of the Barolo and Grignolino wines. The analysis determined the quantities MalicAcid, Ash, AlcAsh, Mg, Phenols, Proa, Color, Hue, OD, and Proline. There are 50 Barolo wines, 71 Grignolino wines, and 48 Barbera wines. Construct the appropriate-size classification tree for this dataset. How many training and testing samples fall into each node? Describe the resulting tree and your approach.

The wine dataset has been loaded and looking at the summary below.

```
summary(wine_data)
Type
1:59
                                                          Alcalinity
in. :10.6
          Alcohol
                            Malic
                                             Ash
                                                                          Magnesium
                                                                                            Pheno1s
                                                                                                           Flavanoids
       Min.
                                                        Min.
               :11.0
                       Min.
                               :0.74
                                        Min.
                                               :1.36
                                                                               : 70.0
                                                                                         Min.
                                                                                                :0.98
                                                                                                         Min.
                                                                        Min.
                                                                                                                 :0.34
                                                        1st Qu.:17.2
       1st Qu.:12.4
                        1st Qu.:1.60
                                            Qu.:2.21
                                                                        1st Qu.:
                                                                                  88.0
                                                                                         1st Qu.:1.74
                                                                                                         1st Qu.:1.21
3:48
       Median :13.1
                       Median :1.86
                                        Median :2.36
                                                        Median :19.5
                                                                        Median :
                                                                                 98.0
                                                                                         Median :2.36
                                                                                                         Median :2.13
                                                                                 99.7
       Mean
                               :2.34
                                        Mean
                                                               :19.5
                                                                        Mean
                                                                                         Mean
                                                                                                :2.30
                                                                                                         Mean
               :13.0
                       Mean
                                               :2.37
                                                        Mean
       3rd Qu.:13.7
                        3rd Qu.:3.08
                                        3rd Qu.:2.56
                                                        3rd Qu.:21.5
                                                                        3rd Qu.:107.0
                                                                                         3rd Qu.:2.80
                                                                                                          3rd Qu.:2.88
                               :5.80
                                       мах.
       мах.
               :14.8
                       мах.
                                                :3.23
                                                        мах.
                                                               :30.0
                                                                        мах.
                                                                                :162.0
                                                                                         Max.
                                                                                                 :3.88
                                                                                                         Max.
                                                                        Dilution
Nonflavanoids
                                                                                        Proline
                 Proanthocvanins
                                       Color
                                                        Hue
                                                                     Min.
                                                                                     Min.
       :0.130
                 Min.
                        :0.41
                                  Min.
                                          : 1.28
                                                   Min.
                                                           :0.480
                                                                            :1.27
1st Qu.:0.270
                 1st Qu.:1.25
                                  1st Qu.: 3.22
                                                   1st Qu.:0.782
                                                                     1st Qu.:1.94
                                                                                     1st Qu.:
                                                                                              500
Median :0.340
                 Median :1.55
                                  Median: 4.69
                                                   Median :0.965
                                                                     Median :2.78
                                                                                     Median :
                                                                                              674
                                            5.06
       :0.362
                         :1.59
                                                           :0.957
                                                                            :2.61
Mean
                 Mean
                                  Mean
                                                   Mean
                                                                     Mean
                                                                                     Mean
3rd Qu.: 0.438
                                  3rd Qu.: 6.20
                                                    3rd Qu.:1.120
                                                                     3rd Qu.:3.17
                                                                                     3rd Qu.:
                                                                                              985
                                                   мах.
Max.
       :0.660
                 Max.
                         :3.58
                                  Max.
                                          :13.00
                                                           :1.710
                                                                     Max.
                                                                            :4.00
                                                                                     Max.
```

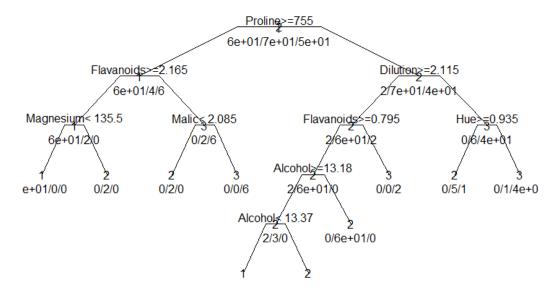
It is indicated that 1 is Barolo wine 2 is Grignolino wines and 3 is Barbera wines. Now building a tree for the given dataset



From which we can observe that the parameter Proline is prominently dependent and then the parameters Flavanoids and Dilutions the classification is dependent.

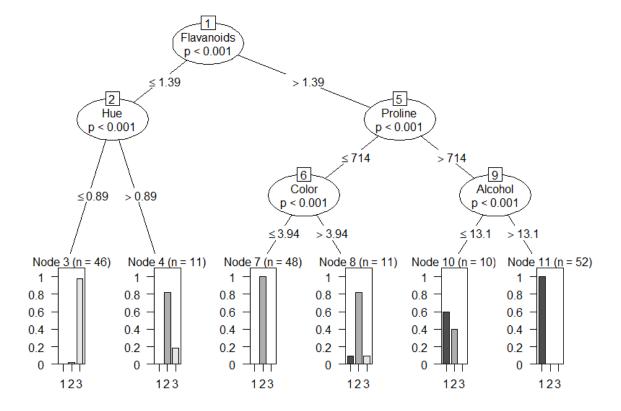
Upon further pruning the dataset to find the appropriate size classification tree we can see that the dataset forms the tree below.

### **Pruned Tree**



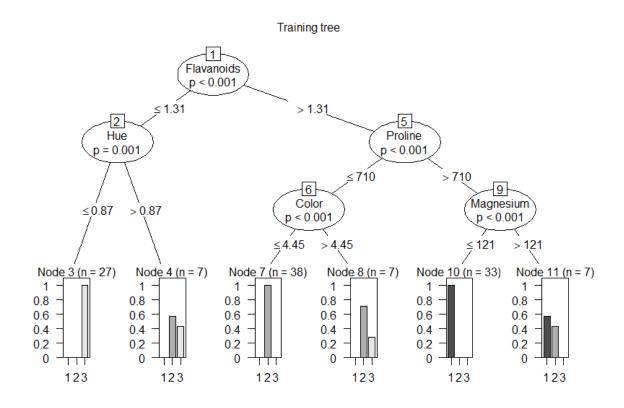
Even upon pruning the tree remains the same for the given dataset, which says that the appropriate size of the same is as obtained in the above tree.

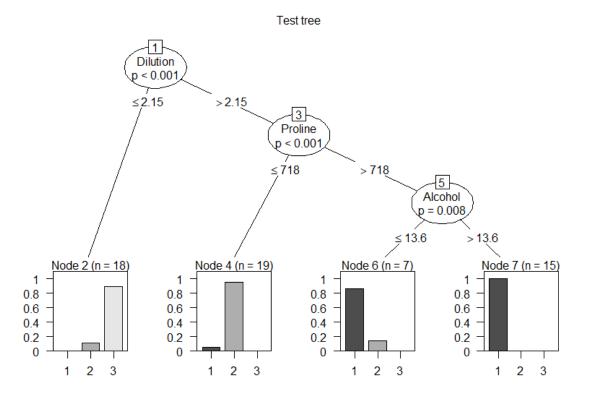
Now let us see the try to visualize the conditional interference trees for the given dataset.



From the above tree visualization we can actually see the number of nodes that this dataset is required to classify the wines type. It is about 11 nodes that are required to classify the same. Also the parameters that are influencing the classification has also been changed with the conditional approach.

Let's look at the training and testing samples trees.





Above tree diagrams clearly says that the samples will have various parameters as influential one's as the samples of training and testing changes. Hence for the same the prediction and error calculation rates will be highly fluctuating. Hence for the same prediction of one test value is feasible and then a set of testing values will always end up unpredictable.

3) (10 points) Apply bagging, boosting, and random forests to a data set of your choice (not one used in the committee machines labs). Fit the models on a training set, and evaluate them on a test set. How accurate are these results compared to more simplistic (non-ensemble) methods (e.g., logistic regression, kNN, etc)? What are some advantages (and disadvantages) do committee machines have related to the data set that you selected?

For the dataset chosen below is the summary of the same.

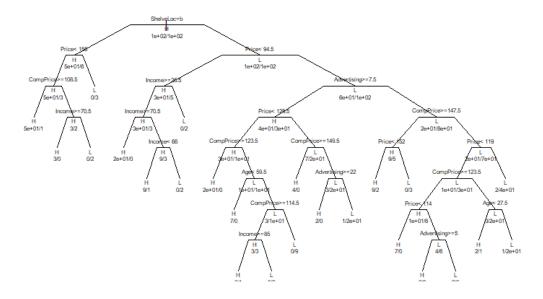
		Tocomo	Advonticina	Donulation	Price	ShelveLoc	4.00
Sales	CompPrice	Income	Advertising	Population	Price	SHETVELOC	Age
Min. : 0.00	Min. : 77	Min. : 21.0	Min. : 0.00	Min. : 10	Min. : 24	Bad : 96	Min. :25.0
1st Qu.: 5.39	1st Qu.:115	1st Qu.: 42.8	1st Qu.: 0.00	1st Qu.:139	1st Qu.:100	Good : 85	1st Qu.:39.8
Median : 7.49	Median :125	Median : 69.0	Median : 5.00	Median :272	Median :117	Medium:219	Median :54.5
Mean : 7.50	Mean :125	Mean : 68.7	Mean : 6.63	Mean :265	Mean :116		Mean :53.3
3rd Qu.: 9.32	3rd Qu.:135	3rd Qu.: 91.0	3rd Qu.:12.00	3rd Qu.:398	3rd Qu.:131		3rd Qu.:66.0
Max. :16.27	Max. :175	Max. :120.0	Max. :29.00	Max. :509	Max. :191		Max. :80.0
Education	Urban U						
Min. :10.0		:142					
	Yes:282 Yes	:258					
Median :14.0							
Mean :13.9							
3rd Qu.:16.0							
Max. :18.0							

From which Sales data has to be predicted.

Let's convert the column to classification by ranging the values above 7 as high and below 7 as low. Splitting the data in training and test sets.

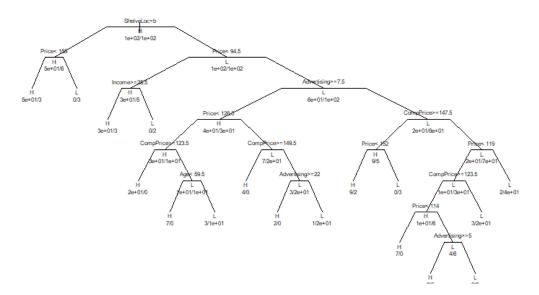
Below is the tree for the dataset taken. '

# Main Tree



Upon pruning the above model for the single tree we obtain the below Pruned tree.

## **Pruned Tree**



Computing the test error for the above tree model.

```
> miss_class_tree
[1] 0.256
```

Similarly looking at the test error for the

It is clear that the for the given dataset Boosting performs very well with low error rate and the random forests and then Bagging.

Let's check to compare with logistic regression and KNN methods.

> log\_test\_err
The error obtained using logistic regression is [1] 0.0902

For us to surprise logistic regression performs better with this dataset. But when discussed on paper the Boosting rates should be low. This is completely dependent on the type of dataset. For larger set of data Boosting is expected to perform very well. But for the dataset that we have performed logistic regression works fine. For every data set depending on its type simplistic model can have advantages of having more accurate and redundant results. Where as Boosting and RF have their advantages in their suitable types of datasets.